# DEVELOPMENT OF A POWER-SPECTRAL GUST DESIGN PROCEDURE FOR CIVIL AIRCRAFT

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TECHNICAL REPONT



JANUARY, 1968

by

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Lockheed-California Company

Burbank, California

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for
Federal Aviation Agency
Aircraft Development Service



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#### DEVELOPMENT OF A POWER-SPECTRAL GUST DESIGN PROCEDURE FOR CIVIL AIRCRAFT

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ADS-53

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Frederic M. Hoblit, Neil Paul, Jerry D. Shelton, and Francis E. Ashford

January, 1966

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Lockheed-California Company Burbank, California

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#### SUMMARY

Three alternate forms of gust loads criterion based on power-spectral concepts are developed. These include a mission analysis criterion. a design envelope criterion, and a criterion combining advantages of each. The latter is recommended for design use. Design levels are determined based on the strength of three existing satisfactory airplanes, the Lockheed Model 749 (Constellation) and Model 188 (Electra) and the Boeing Model 720B. The determination of a design load level involves dynamic gust analysis of the three sirplanes, taking into account the significant rigid body and elastic modes, for both vertical and lateral gust inputs, as well as detailed stress analysis to the resulting loads. The appropriate limit design frequency of exceedance (mission analysis criterion) is found to be  $2 \times 10^{-5}$  exceedances per hour. The appropriate limit design value of  $\sigma_{\mathbf{w}}\eta_{\mathbf{d}}$  (rms true gust velocity times ratio of design load to rms load, for use in a design envelope criterion) varies linearly from 55 fps at sea level to 62 fps at 7000 ft., to 55 fps at 27000 ft., to 17 fps at 80000 ft. For a conservative level to be used under the "combined" criterion in the absence of a mission analysis, these values increase to 101 fps at sea level, varying linearly to 110 fps at 7000 ft., to 117 fps at 27000 ft., to 37 fps at 80000 ft. Two techniques have been developed for integrating the statistical determination of loads with the detailed stress analysis. One is the matching condition technique, in which design conditions are generated to closely envelope the statistically defined loads, with phase relations of the various load or stress components properly accounted for. The other is the joint probability technique, in which the joint probability density of axial and shear stresses is determined at all potentially critical locations in the structure and related to the respective strength envelopes. The sensitivity of results to variations in input data is investigated.

This volume covers all parts of the study except the analysis of the Model 720B airplane and the development and illustration of the joint probability technique, which are covered in Report FAA-ADS-54, prepared by The Boeing Company under subcontract.

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#### INTRODUCTION

During the past fifteen years, great progress has been made in gust loads theory. The most fundamental advance has been the representation of atmospheric turbulence as a stationary random process, to which power-spectral methods of analysis can be applied. A second important advance has been the widespread development of automatic computer techniques for solving the equations of motion of the airplane in turbulence. It is now practical to represent the dynamics of the airplane in sufficient refinement to cover adequately not only the rigid-body motions but also the airplane elasticity and, if necessary, the effects of artificial stability augmentation devices.

The motivation for these advances, of course, has been to secure a safer and lighter structure from the standpoint of gust loads. Yet these advances in themselves do not result directly in achieving this objective. There are still two steps required. The first, and most important, is to modify or re-develop the suructural criteria by which a required strength level is established for any given airplane. The second is to fit the newer methods into the routine by which design loads are obtained, and stress analysis carried out, to assure a consistency in strength throughout all the individual elements of the structure.

The first of these, namely the criteria step, is particularly difficult. Gust severity, as affected by both magnitude and shape of the gust, is inherently a statistical phenomenon. Consequently, it is not possible to define a "worst possible" gust and simply design for this gust. Past gust criteria have consisted of a particular combination of gust intensity, gust shape, airplane flight condition (speed and weight), method of analysis, and factor of safety. This combination has resulted in a satisfactory level of safety. Other combinations, however, such as a higher gust intensity with a lower factor of safety, could equally well have been selected with no significant change in the strength level achieved. Similarly, with a change in the method of analysis, such as an improvement to include flexible-rirplane dynamics, or a change in the definition of the gust structure, the remaining factors must be re-evaluated to assure that an adequate yet not excessively high level of strength is defined.

To establish criteria directly, starting with agreement as to an acceptable loss rate, has generally been found not to be practical. Work along this line, however, has usually indicated that past criteria have not been overly severe. Consequently, in modifying existing criteria or devising new criteria, a practical objective is the achievement of a level of safety with respect to gust loads just equal to that of earlier satisfactory airplanes. If this is accomplished, the level of strength is certain to be adequate. It may be greater than actually necessary, but

probably by a rather small margin. More specifically, the new criteria must be of a severity such that when these criteria are applied to the older, satisfactory airplanes, these airplanes are found to be just adequate. A criterion of any greater severity would then indicate these airplanes to be inadequate, in contradiction to their satisfactory service records. A criterion of any lower severity would have permitted less strength; with the reduced strength the safety record might not have been satisfactory. As applied to new design, the new criteria, now incorporating the more realistic definition of the gust structure and the more refined methods of analysis, will more reliably predict the strength required than will the former criteria, established without the benefit of these recent advances.

Unfortunately, to re-write the gust criteria in a simple specific form that is sure to attain the above goal is a complicated task that had not been accomplished prior to the initiation of the present study. Some of the obstacles that had lelayed such an undertaking were the following:

- 1. It had been questionable whether the state of the art of gust loads analysis had advanced sufficiently to permit clear definition of the variables that must be included in the analysis, and in what degree of refinement, in order to achieve results of the required engineering accuracy. As a result, variations in the method of analysis had been found to have a rather sizable effect on the resulting loads.
- 2. To be realistic, gust criteria should reflect the actual operating usage of the vehicle, which may bear a quite different relation to the design envelope for various vehicles. Furthermore, the operating usage cannot be controlled entirely by placard without undue restriction on operating flexibility. Consideration of actual operating usage inherently complicates the criterion.
- 3. To confirm that any proposed criterion defines a reasonable level of strength, it should be applied to various existing airplanes. Each such study, if performed with the requisite thoroughness, would be quite costly; such cost was justifiable to individual manufacturers only in connection with the development of a new design, wherein only one or two earlier airplanes built by the same manufacturer were given the required detailed treatment.

Even though no simple, specific gust loads criterion utilizing the new developments was available, practical design techniques were developed that adequately achieved the desired objective in the design of recent aircraft.

The first step in the development of those techniques was taken toward the end of the era of piston engine transports. At that time it became apparent that the earlier airplanes had satisfactory service and safety records, even though no provision had been made in their design loads for dynamic effects that were known to be present. Thus it became evident that the design gust velocities had been set high enough so that for these airplanes no increase in design loads for dynamic effects was needed. On the other hand, it was apparent that, as airplanes become larger, faster, and more flexible, the relative dynamic effects might well increase; and, sooner or later, design to static loads alone could lead to a structure of inadequate strength.

Consequently, to prevent any deficiency in strength that might otherwise have resulted from this trend, the CAA at that time adopted a policy which was summarized as follows:

"During the AIA-CAA Gust'Loads Meeting in Washington, it was agreed that if a manufacturer showed that for his new model the percentage increase in load, due to transient effects, was no greater than that of his previous models, it would not be necessary to design for the increased load; however, if the increase was greater than for the previous models, this increase should be designed for."

This policy, reflecting what may be called the concept of "limited dynamic accountability", was applied, for example, in the design of the Lockheed Model 1649 Constellation and the Electra. As was the practice at that time, primary emphasis was placed on a comparison of dynamic magnification factors of wing bending moment. These were obtained utilizing both discrete-gust and power-spectral descriptions of the atmosphere. Even in these analyses, however, it was recognized that comparison of dynamic magnification factors alone would not assure that the new airplane would have as great gust load capability as the previous models. Consequently, consideration was also given to the effect of the following: (a) differences in the margin between design speed and normal operational speed; (b) differences in the static gust loads criteria to which these airplanes had been designed; and (c) positive margins of safety (indicative of strength greater than required) in the reference airplane.

More recently, important potential inadequacies were found in this simple treatment. As a result, more comprehensive and rational methods were developed. In one particular application, the approach was two-fold. First, a full dynamic analysis of the response of the flexible airplane to discrete gusts of various gradient distances was made, for both the new airplane and a reference airplane having a long and satisfactory service record. Complete wing loads were obtained for both

airplanes. A "dynamic accountability factor" was then employed to adjust the loads for the new airplane to the level of gust severity that would just take the reference airplane to limit strength. Second, to confirm the adequacy of the loads thus defined, a power-spectral analysis was performed on a "mission analysis" basis; in this analysis, it was required to show that the new airplane would fly at least as many miles before reaching limit strength as the reference airplane.

The major objection to a continuation of the type of approach described above is that data on the various satisfactory existing airplanes are available, in the necessary detail and scope, only to the manufacturers of those airplanes. Consequently, a manufacturer whose past airplanes may not have been gust-critical, or for other reasons may have had more than the required strength, must design his new aircraft to more severe criteria than the manufacturer whose past aircraft happen to have less margin. Further, no criteria short of "full dynamic accountability" are available to a manufacturer who has no previous aircraft in operation with a long, satisfactory service life.

For this reason, it has long been recognized that eventually it would be necessary to establish a gust criterion that could be employed without reference to any specific reference airplane. With the experience that has now been accumulated, it appears that the time is ripe for the development of such a criterion. The study described herein sets forth the form of such a criterion, provides evidence that the criterion will be practical to apply, and establishes tentative design levels.

As noted earlier, a second problem in the application of the newer advances in gust loads theory is to fit them into the routine by which design loads are obtained and stress analysis is conducted. Normal stress analysis practice utilizes design conditions each of which is defined over the whole of some major structural component at a given instant. Power-spectral methods, however, do not result in this sort of design condition. They lead, instead, to individual design-level values of load of equal probability at various points in the structure, or of various components of load such as wing shear, bending moment, and torsion, with the phasing undetermined. For example, it is not determined whether maximum up shear combines with maximum nose-up or maximum nose-down torsion or with some intermediate value. This difficulty can be circumvented to some extent by determining designlevel values of internal leads or stresses, such as front and rear beam shear flows. But this approach is likely to lead to the cumbersome procedure of determining separate power-spectra for loads in every minute element of the structure - literally thousands of elements in a typical modern airplane wing. In addition, there still remains a problem of handling combined stresses or stress redistribution after the material begins to yield or buckle.

Consequently, it is clear that for any criterion involving the power-spectral concept to be useable, there must be some assurance that practical means are available to integrate the gust loads determination into existing design procedures and organizational arrangements. Two rather different techniques that accomplish this purpose have been developed and are described herein.

Finally, it has been noted that variations in the methods of analysis have sometimes been found to have a rather sizable effect on the loads obtained. Consequently, for the envisioned criterion to be relied upon to provide adequate structure, it is necessary to obtain a specific indication of the variations in the resulting design loads that might be produced by variations in the input data used in the loads determination. Therefore, these effects have also been investigated.

In addition to the variations in method or input data that can be studied utilizing a given mathematical model, there are also subtle differences among various mathematical models, even though these models may all be of the same general level of complexity. Since the present study is conducted by two different manufacturers, an excellent opportunity has presented itself to compare the results obtained by two different models using identical input data. Consequently, such a comparison is made as part of the present study.

In summary, the objectives of the program reported herein can be listed as follows:

- 1. Provide a recommended form for a gust loads criterion based on power-spectral concepts.
- 2. Establish design levels based on strength of satisfactory existing airplanes, taking into account the significant rigid body and elastic modes.
- 3. Provide a practical technique for using statistically defined loads in stress analysis, and illustrate by application to an existing airplane.
- 4. Investigate sensitivity of results to data and methods.

It should perhaps be emphasized that, in carrying out these objectives, the intent has been to utilize the present state of the art of power-spectral gust loads analysis, rather than to advance the state of the art. Accordingly, only a very minor effort has been devoted to improving currently available models of the atmosphere, even though a need for a substantial effort in this direction has been generally recognized. Also, no attempt has been made to account for the effect of

spanwise variations of gust velocity. Various published papers have treated this subject, and eventually it may be necessary to consider the effects of a two-dimensional gust pattern. However, these effects are probably rather small for existing or proposed aircraft; and it is believed to be more important at this stage to proceed to develop criteria that exploit the simpler theory, which is the one that has been employed in most applications to date.

The general plan of this report is fairly evident from the Table of Contents.

Sections 2 and 3 discuss the selection of the three reference airplanes for analysis and the airplane components to be treated. Section 4 indicates the general forms that might be taken by a power-spectral gust loads criterion and that will be used in the present study. Section 5 then discusses the establishment of the particular atmosphere model to be used. A detailed comparison of this with the best-known previous model is given in Appendix A.

The dynamic analysis of two of the three reference airplanes, the Lockheed Model 188 and Model 749, is described in Sections 6 through 9, with detailed numerical results presented in Appendix B. The corresponding material for the Boeing Model 720B is contained in Reference 1.

The two design techniques developed as part of the present study are introduced in Section 10. The "matching condition" technique is developed in Section 11 and the "joint probability" technique in Reference 1. The two techniques are related and compared in Section 12.

Limit-strength and ultimate-strength levels for the three reference airplanes, in terms of the power spectral criteria described in Section 4, are then summarized in Section 13. These are determined from the results of the dynamic analysis, drawing upon the design techniques described in Sections 10 through 12 and performing such stress analysis of the structure as found necessary. Detailed accounts of this determination are included in Appendix E and in Reference 1.

The effect of parameter variations on gust loads is reported in Section 14 and in Reference 1.

Utilizing the limit strength levels presented in Section 13, with the information in Section 14 on the effect of parameter variations as further background, appropriate design levels for new airplanes are considered in Section 15. Suggested formal requirements are provided.

A summary of the over-all procedure for dynamic gust loads determination for new airplanes is then presented in Section 16. Comments on modifications that might be required for application to advanced configurations are included. Finally, in Section 17, consideration is given to the relation of the existing discrete-gust requirement to the power-spectral criteria proposed as a result of this study.

Some prior familiarity of the reader of this report with the concept of a stationary random process and the techniques of power-spectral analysis is assumed. Recommended introductory discussions are contained in References 2 and 3. References 4 through 6 provide additional material that may also be helpful.

## 1 NOMENCIATURE

Ā	Ratio of root-mean-square value of load to root-mean-square gust velocity
b <sub>1</sub> ,b <sub>2</sub>	Intensity parameters in the expression for probability density of $\sigma_{\mathrm{W}}$
ē	Mean wing chord
$^{\mathrm{c}_{\mathrm{L}}}{}_{a}$	Slope of curve of $C_{\mathbf{L}}$ vs $\boldsymbol{a}$ , per radian
f	Frequency, cycles per second
Î	Probability density
h	Altitude
Kg	Gust alleyation factor for one-minus-cosine discrete gust (Reference 31)
K <sub>o</sub>	Dimensionless gust response factor for continuous turbulence (Equation 5-5)
L	Scale of turbulence, a parameter in Equations 5-1 and 5-4
$M_x, M_y, M_z$	Bending or torsional moment about axis indicated
N <sub>o</sub>	Average number of zero crossings with positive slope, per unit time
N(y)	Number of exceedances of the indicated value of y per unit time (ordinarily per hour)
P	Probability that stress is in excess of limit load level, or that stress condition is outside the limit-strength envelope
P <sub>1</sub> ,P <sub>2</sub>	Fractions of total flight time in non-storm and storm turkulence respectively - parameters in the expression for probability density of $\sigma_{\rm W}$
q	Dynamic pressure. Shear flow
S	Reference wing area
	neretence with, area

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Airspeed Design rough-air speed  $v_{c}$ Design cruise speed

 $v_{D}$ Design dive speed

 $v_{\rm e}$  $\mathbf{v_{T}}$ True airspeed

Airplane gross weight

Any acceleration, load, or stress

Equivalent airspeed

Ratio of actual damping coefficient to critical, or deadbeat, damping coefficient

Ratio of design load to root-mean-square load  $\eta_d$ 

Airplane mass parameter as used in Reference 31, 2W/C<sub>La</sub> ρcgS

Same as  $\mu_{g}$  but with  ${\bf C_{L}}_{\alpha}$  taken as airplane instead of wing lift curve slope

Air density

Root-mean-square value of true gust velocity (vertical or lateral component)

Root-mean-square value of y

 $\phi(\Omega)$ Power-spectral density function

Reduced frequency, radians per foot

Other quantities, used only in particular sections of the report, are defined where used.

#### 2 SELECTION OF AIRPLANES FOR ANALYSIS

In the selection of a "reference" airplane to use for setting the level of severity of a new gust loads criterion, the most important consideration is a long and successful service life. This is necessary in order to provide a reasonable opportunity for any deficiency in strength to have become evident.

A second important consideration is that, to avoid excessive conservatism, the airplane should be as gust-critical as possible at normal operating speeds. For if the reference airplanes are not gust-critical, the strength put in for other than gust conditions, or perhaps for gust conditions at an unreasonably high design speed, will be interpreted as necessary to provide safety in turbulence. The new criteria would thus require an equivalent, unnecessarily high, strength in the new aircraft.

Another consideration of great practical importance is that complete and detailed data for the reference airplanes be available. These data must include not only the "over-all" aerodynamic, mass, and elastic data needed to solve the equations of motion, but also detailed data as to external and internal load distribution and local structural strength. Adequate data of this type can be obtained only as a result of extensive wind-tunnel tests, flight load measurements, stress analysis of a multitude of structural components, and panel tests to determine structural allowables.

An important additional consideration, although not a vital one, is that VGH data be available for the reference airplane to assist in defining the mission profiles to be used for analysis.

Similarity of the reference airplanes to the new airplanes to which the criterion will be applied, in such configuration characteristics as wing sweep, type of propulsion, number of engines, etc., is <u>not</u> a pertinent consideration in selecting the reference airplanes. The effect of dissimilarity in configuration should be fully accounted for in the dynamic analysis.

For the purpose of the present study, the Lockheed Model  $7^{1/3}$  Constellation, the Lockheed Electra (Model 188), and the Boeing Model 720B are selected as reference airplanes.

The Model 749 is regarded as particularly suitable as a reference airplane. As of January, 1965, individual ships of this fleet averaged about 43000 hours of service, with several as high as 55000 hours, all with no evidence of structural inadequacy to carry the gust loads that have been encountered.

The Model 749 is gust critical under the current FAR 25 criteria (Reference 7). Furthermore, in comparison with other airplanes of the piston-powered transport era, the 749 appears to be relatively gust critical at normal operational speeds. It has been found to be considerably more gust-critical than later Constellations, for example, primarily as a result of an increase in the wing loading of the later airplanes without any significant change in their typical operating speeds. In addition, VGH data have been published for Model 749 operation (Reference 8).

The particular version of the Model 749 for which the analyses are conducted is the Model 749A including modifications in accordance with Service Bulletin 545. This airplane was designed for a take-off gross weight of 107,000 lb. and a maximum zero-fuel weight of 86,464 lb. The majority of the 145 airplanes in the Model 749 fleet - totaling at least 104 airplanes and probably about 140 - were either delivered in this configuration or later converted to it.

The Electra provides a second suitable reference airplane. Individual airplanes in the Electra fleet as of January 1, 1965, had acquired as much as 18000 hours of service during their eight years of operation. The Electra is gust critical over much of the wing, fuselage, and empennage under FAR 25 criteria. And for it, too, extensive VGH data are available (References 9 through 11).

The particular Electra airplane for which the analyses are conducted has a design take-off weight of 116,000 lb. and maximum zero fuel weight of 86,000 lb. For the purpose of this study, airplane serial numbers 1035 - 1148 and 2001 - 2022, totaling 136 airplanes, can be considered to fall in this category. Actually, a considerable number of these airplanes are certificated for a take-off weight of only 113,000 lb., primarily because the increase in strength of the landing gear support structure required for the 116000 lb. gross weight was serialized somewhat later in the production program. However, the primary wing, fuselage and tail strength is the same for all 136 airplanes, and the flight loads given by the power-spectral analysis are essentially identical at both the 113,000 lb. and 116,000 lb. gross weights. (The last six Electra airplanes also had a small increase in fuselage shell strength to provide additional growth potential; this increase, however, would have no effect on the results of this study, and no further explicit consideration is given to it.)

The Boeing Model 720B provides an additional reference airplane representative of current subsonic jet transports. As of January 1, 1965, the fleet of 720 and 720B airplanes had accumulated a total of nearly 1,300,000 flight hours, with the high-time airplane in excess of 13000 hours. The 720B is selected in preference to other airplanes of the

707 and 720 series because it is the most nearly gust-critical, because its use in medium-range operations probably results in a somewhat more severe gust exposure, and because better and more complete data are available for use in the analysis. Although VGH data are not available for the 720B explicitly, extensive VGH data have been obtained from 707 operations and are available in Reference 9.

The selection of an airplane to use for illustrating the design techniques to be developed can be quite independent of the selection of the reference airplane. The Lockheed Electra and the Boeing 720B are used for this purpose. The basic principles involved can be adequately demonstrated utilizing these airplanes; possible modifications that might be required for other configurations such as arrow wing, variable geometry, or delta-canard are explored without specific numerical illustration.

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#### 3 AIRPLANE COMPONENTS TREATED

In developing criteria that will utilize the more recent advances in gust loads theory, major emphasis has usually been placed to determination of design wing loads. However, other airplane components, too, are often designed by gust loads. In fact, one of the more significant applications of power-spectral theory to gust loads has been in the investigation of vertical tail loads for the current subsonic jet transports where low damping in the Dutch roll mode has resulted in loads not adequately accounted for by the discrete-gust approach. In addition, vertical gusts produce loads on the fuselage (primarily due to inertîa) and on the horizontal tail, that have been critical for design.

Manifestly it would be desirable for a single design criterion to be applicable to all structural components and to both vertical and lateral components of turbulence. In order to assure, however, that the criterion developed in the present study does have the desired generality, each of these various areas is treated specifically. Primary emphasis is given to the wing. The fuselage and horizontal tail are treated by fairly simple extensions of the mathematical models developed originally to define wing loads. Side gust loads on the vertical tail require a separate treatment, and a significant part of the study is devoted to this aspect.

No explicit consideration has been given to loads on engine nacelles. In any new design, however, especially of a propeller-powered airplane, the determination of nacelle design loads would have to be included in the analysis.

### 4 TYPES OF POWER-SPECTRAL GUST LOADS CRITERIA CONSIDERED

In developing a gust loads criterion based on power-spectral analysis that can be used without reference to any specific comparison airplane, either of two general types of approach might be followed. The basic features of each of these approaches are discussed in considerable detail in the following paragraphs. A combined criterion, which includes use of both approaches, is then suggested. Finally two subsidiary considerations are discussed - namely, the treatment of stability augmentation systems and specification of structural failsafe conditions. Throughout the remainder of this report, data applicable to both of the basic types of criteria are developed.

#### 4.1 Mission Analysis Criterion

The first approach utilizes the mission analysis concept. A standard set of gust statistics is established, in the general form employed in NACA TN 4332 (Reference 12). This permits use of the equation

$$N(y) = N_0 \left[ P_1 \exp \left( -\frac{y}{b_1 \bar{A}} \right) + P_2 \exp \left( -\frac{y}{b_2 \bar{A}} \right) \right]$$
 (4-1)

to obtain curves of frequency of exceedance vs load, for each mission segment. In this equation, y can be any load quantity - for example, bending moment at a particular wing station. N(y) is the number of exceedances of y per unit time or distance flown. A is the ratio of the rms value of y to the rms gust velocity, and  $N_0$  is a characteristic frequency of y, obtained as the radius of gyration of the power-spectral density of y about zero frequency. Both A and  $N_0$  are evaluated by appropriate dynamic analysis, utilizing all pertinent degrees of freedom.  $P_1$ ,  $P_2$ ,  $p_1$ , and  $p_2$  are parameters defining the gust environment; plots of these are provided as functions of altitude, as described in the next section.

The exceedances determined for each mission segment by means of the above equation are then added to give the exceedances for overall operation of the airplane.

This type of criterion requires, for a new vehicle, establishment of typical mission profiles, which are then broken down into segments. Certain ground rules, or minimum requirements, may properly be specified for accomplishing this step, to assure that sufficient detail is provided to account for the more severe elements of the operational spectrum. The mission analysis results in a curve of frequency of exceedance vs load level for each pertinent load. The frequency of

exceedance corresponding to limit (or ultimate) load is specified; entering the frequency of exceedance curves for the various load quantities with this value then yields a design value of each load. The design frequency of exceedance must be carefully chosen on the basis of providing strength in new vehicles consistent with that found adequate in existing aircraft.

In the present study, the basic task in the development of the mission analysis type of criterion is the determination of the frequency of exceedance of limit (or ultimate)strength, at the most critical point in the structure for each of the three reference airplanes - the Lockheed Model 749 and Model 188 and the Boeing Model 720B. A single value is then to be selected to use in future design. On the basis that each of the three airplanes has demonstrated structural adequacy with respect to gust-induced loads, the rational selection would be the highest of the three frequencies of exceedance - that is, such as to define the lowest loads.

This frequency of exceedance can readily be expressed as a frequency either per flight hour or per flight mile. For application to new design, however, a different load level will result depending upon which way the frequency is stated. To illustrate, consider that a new airplane is being designed, which will fly much faster than the old reference airplane on which the design frequency of exceedance is based. Suppose that this new airplane is designed to reach limit strength, on the average, after the same number of flight miles as the old airplane - i.e., it is designed to the same frequency of exceedance per mile. The new airplane then, as a result of its higher speed, will reach limit load in fewer hours; and by the time it has flown the same number of hours, it will have reached - on the average - some higher load level. Consequently, its design loads would be higher if based on a given frequency of exceedance per hour rather than per mile. Accordingly, it is important to establish as logically as possible whether equivalent safety is properly achieved by design on a permile or a per-hour basis.

From the standpoint of a crew member, equivalent safety would appear to require design to reach limit (or ultimate) load after a given number of flight hours, since the crew member will expect to spend about the same number of hours in the air regardless of whether flying in a fast or slow airplane.

From the standpoint of a passenger, on the other hand, it might be argued that equivalent safety would involve design to reach limit (or ultimate) load after a given number of flight miles. A passenger, having decided to take a given trip, would want the same high probability of reaching his destination without mishap regardless of

whether traveling on a fast or a slow airplane. However, there is undoubtedly a tendency to travel more frequently and over greater distances as travel becomes faster and easier. Consequently, even from the passenger standpoint, it appears about as reasonable to design on a per-hour as on a per-mile basis.

It therefore appears that a mission analysis gust loads criterion for civil aircraft should specify a rate of exceedance of limit (or ultimate) load per hour. The results of the analyses conducted in the present program are therefore expressed on this basis.

While it would be a mistake to confuse economics with safety, it might also be noted that the desired fatigue life of a civil transport airplane tends to be roughly a constant number of hours, regardless of the flight speed. As a result, selection of a per-hour limit strength criterion has the added advantage of tending to lead to consistency of fatigue and limit strength and also to consistency in the calculation procedures for repeated loads spectra and design limit loads.

At this point it is pertinent to outline more specifically the steps in the actual computation of a frequency of exceedance curve for a given quantity.

First, it is noted that y in Equation 1 is actually the increment due to the gust - i.e., not including the one-g level flight value.

Letting y now denote the net load, including the one-g load, Equation (4-1) becomes

$$N(y) = N_0 \left[ P_1 \exp \left[ - \frac{y - y_{\text{one-g}}}{b_1 \overline{A}} \right] + P_2 \exp \left[ - \frac{y - y_{\text{one-g}}}{b_2 \overline{A}} \right]$$
 (4-2)

For any mission segment, N(y) is obtained as a function of y by selecting a series of values of y and calculating N(y) for each. The value of N(y) thus obtained will be the average number of exceedances per hour of flight (assuming  $N_0$  to have been converted to units of cycles per hour) in the given mission segment. To obtain the number of exceedances within the given segment per hour of over-all flight, N(y) is multiplied by the ratio of time in the given segment to total time. Curves of N(y) vs y are obtained in this way for each mission segment. At each of a series of values of y, the N(y) values for all the segments are then added, to give the over-all N(y) vs y relation.

#### 4.2 Design Envelope Criterion

The second approach disregards all considerations of the specific operational usage of various airplanes to which the criterion might be applied; instead, it leads to a criterion in which design is to a specified design envelope of speed, altitude, gross weight, fuel weight and c.g. position. In this respect, the criterion is similar to the past discrete gust criteria. The criterion resulting from this approach specifies a shape of gust power-spectral density function and a quantity  $\sigma_{\rm w} \eta_{\rm d}$  (following the notation of reference 13), in which  $\tau_{\rm w}$  is an rms gust intensity and  $\eta_{\rm d}$  is a factor representing the ratio i design load to rms load. The breakdown between the two factors is ordinarily not of consequence, except as an aid in visualizing the physical significance of the criterion; only the product is specified. (In the joint probability treatment of combined stress, however, values of  $\sigma_{\rm w}$  and  $\eta_{\rm d}$  must both be specified.) The quantity  $\sigma_{\rm w} \, \eta_{\rm d}$  is closely analogous to  $U_{de}$  in present criteria; it is specified as a function of altitude, for each of one or more speeds  $(V_B, V_C \text{ and } V_D)$ . The design load at any point is then given by multiplying  $\sigma_w \eta_d$  by  $\bar{A}$ , the ratio of the rms value of load at the given point in the structure to the rms gust velocity. The selection of the values to be specified for  $\sigma_{\rm w}\,\eta_{\rm d}$ must be based on providing strength in the new vehicles consistent with that found adequate in existing aircraft. (A refinement that might be made would be to include in the expression for design loads an appropriate multiplying factor, ordinarily close to unity, given as a function of the characteristic frequency of the load response quantity, No; the effect of such a refinement would be small, however, and the added complexity is therefore believed not to be justified.)

In the development of a design envelope type of criterion, a necessary preliminary step is to establish a variation with altitude of  $\sigma_w \eta_d$ . For this purpose, it is noted that

$$\begin{array}{rcl} y_{\mathrm{design}} &=& \eta_{\mathrm{d}} \, \sigma_{\mathrm{y}} \\ &=& \eta_{\mathrm{d}} \, \sigma_{\mathrm{w}} \, \bar{\mathrm{A}} \\ &=& (\bar{\mathrm{A}}) \, \left(\sigma_{\mathrm{w}} \, \eta_{\mathrm{d}}\right) \end{array}$$
 whence 
$$\begin{array}{rcl} \frac{y_{\mathrm{design}}}{\bar{\mathrm{A}}} &=& \sigma_{\mathrm{w}} \, \eta_{\mathrm{d}} \\ &&& \\ \sigma_{\mathrm{w}} \, \eta_{\mathrm{d}} &=& \left(\frac{y}{\bar{\mathrm{A}}}\right)_{\bar{\mathrm{design}}} \end{array}$$

It is reasonable to require that, as altitude varies, the design value of  $y/\bar{A}$ , or of  $\sigma_W$   $\eta_d$ , should also vary, in such a way that the average

frequency of exceedance of y is the same at all altitudes. Noting that b1, b2, P1, and P2 are functions of altitude only, it is seen that Equation 4-1 defines  $N(y)/N_0$  as a function y/X for constant altitude. Also, therefore, it defines y/X as a function of altitude for constant  $N(y)/N_0$ . Curves of the latter type are developed in the next section, "Model of the Atmosphere", and are shown in Figures 5-6 and 5-8. To the extent that  $N_0$  is independent of altitude, a given value of  $N(y)/N_0$  reflects a constant frequency of exceedance of load. Consequently, the variation of  $C_0 \eta_d$  with altitude will be defined by some constant value of  $N(y)/N_0$  in Figure 5-6 or 5-8.

The basic task in the development of the design envelope type of criterion is to establish the particular value of N(y)/No that will properly define  $\sigma_u \eta_d$  as a function of altitude. This is accomplished as follows. For each of the three "reference" airplanes, the limitstrength (or ultimate strength) y/A value (at the most critical point in the structure) is determined at as many altitudes as are likely to be critical. The limit strength value of y/A is simple the limitstrength value of the load quantity, y, less the one-g value, divided by A for this load quantity as obtained by the dynamic analysis. The flight conditions to be investigated at each altitude will consist of the critical combinations of gross weight, c.g. position, fuel load, payload, and airspeed within the structural design envelopes. For each of these limit strength (or ultimate strength) values,  $N(y)/N_0$  will be read from Fig. 5-8. The point corresponding to the largest value of  $N(y)/N_0$  - i.e., defining a curve farthest to the left in Fig. 5-8 will determine the ound variation appropriate to that airplane. Three such curves will thus be defined - one for each of the three reference airplanes. A single curve will then be selected for use in future design. On the basis that each of the three airplanes has demonstrated structural adequacy with respect to gust induced loads, the rational selection would be the curve representing the <u>highest</u> value of  $N(y)/N_0$  that is, such as to define the <u>lowest</u> loads.

In establishing design values of  $\sigma_w \, \eta_d$ , the investigation first is confined to definition of  $\sigma_w \, \eta_d$  for use at speed  $V_C$ . Consideration is then given to establishing values for use at  $V_B$  and  $V_D$ .

Retention of a VD gust requirement is undoubtedly appropriate. Although the percent of time at speeds substantially in excess of VD is probably very small, the highest speeds are likely to result from upsets in very severe turbulence; a reasonable capability to withstand turbulence at dips speed should therefore be assured.

A continued need for increased gust intensities at  $V_B$  is less obvious. Operating instructions increasingly emphasize the need for maintaining sufficient speed in reach air to maintain good control, and NASA analysis of their VGH data indicates that the tendency to slow down in

turbulence has been negligible. (Reference 15 does indicate that about 80% of storm turbulence is encountered at reduced speed; but the remaining 20% encountered at cruise speed still represents a substantial exposure.) Consequently, it might be concluded that whatever turbulence intensity is found to be adequate at speed VC should also be adequate at VB. However, all three airplanes are found to be good for turbulence intensities at VB considerably in excess of those at which they reach limit strength at VC. In the absence of compelling evidence that this capability is not necessary for safety, it is considered prudent to provide a comparable capability in future airplanes. Consequently, a design turbulence intensity at VB, higher than that at VC, is also established.

#### 4.3 Combined Criteria

While the type of criterion finally formulated might be simply one or the other of the two described above, it is believed that consideration should also be given to a criterion that would combine both of these approaches.

It appears that only by means of a realistic mission analysis can it be assured that the gust loads defined provide a strength level that is safe yet not overly conservative. Only the mission analysis approach, for example, will provide loads that are adequate for a new aircraft that operates most of its time close to its design envelope, without penalizing aircraft such as the current transports that operate generally rather far within their design envelopes. Yet the mission analysis approach does suffer certain disadvantages. Considerable judgment is required in setting up the design missions, and the design loads obtained are affected to greater or less extent by the decisions made at that stage. Also considerable care may be required to assure that a sufficient variety of off-typical flight conditions are included - e.g., extremes of c.g. position, payload, speed, etc.

Consequently, a combined criterion that would retain the advantages of the mission analysis criterion while minimizing its disadvantages would be attractive.

For example, a combined criterion might establish conservative design values of  $\sigma_W \eta_d$  that could be used in lieu of a mission analysis, together with a provision that these need not be met if an acceptable mission analysis is performed. Thus, for an airplane that is rather far from being gust critical, the mission analysis could be eliminated entirely. In addition, even when a mission analysis is performed, a  $\sigma_W \eta_d$  analysis might be required, but at some reduced  $\sigma_W \eta_d$  level. This would then provide a floor below which the mission analysis loads could not drop. It would thus provide a degree of insurance against omitting pertinent operational elements in setting up the mission profiles and breaking them into segments. Similarly, it would provide insurance against a possible rapid increase in gust response as the boundaries of the design envelope are approached.

## 4.4 Other Considerations

In any gust criterion, the treatment of automatic stability augmentation devices must be covered. Ordinarily, such devices would be considered operative. However, malfunction must also be provided for. In the mission analysis type of criterion, a certain percentage of flight time can be included with stability augmentation devices inoperative. This percentage can either be stated explicitly or left to the manufacturer to select and then justify by reliability considerations. In the "design envelope", or  $a_w \eta_d$ , type of criterion, a percentage reduction in  $a_w \eta_d$  can be established for use with stability devices inoperative. This percentage can be stated explicitly, or stated as a function of the percent of time that the devices are expected to be inoperative, this percent of time to be selected by the manufacturer and justified by reliability analyses.

Fail safe loads, also, must be covered. In the mission analysis type of criterion, fail safe conditions can be defined in terms of some different frequency of occurrence. In the design envelope type of criterion, fail safe loads can be defined by some different value of  $\sigma_{\rm W} \eta_{\rm d}$ .

#### 5 MODEL OF THE ATMOSPHERE

#### 5.1 Background

The model of the atmosphere adopted for use in the present program follows the general pattern set forth in NACA TN 4332. The atmosphere is first considered to be made up of discrete patches of continuous turbulence of different root-mean-square intensities,  $\sigma_{\rm W}$ , each of which is "stationary" and "Gaussian." This discrete patch model is then replaced by a model which has a continuously varying distribution of root-mean-square gust velocity,  $\sigma_{\rm W}$ . This variation is considered to be gradual enough in time, however, so that the various relations of output to input developed for a stationary Gaussian process still apply.

The shape of the power spectral density function of the gust velocity is assumed to be the same for all turbulence encountered, and in TN 4332 it is assumed to be given by the Liepmann equation,

$$\Phi (\Omega) = \sigma_{w}^{2} \frac{L}{\pi} \frac{1 + 3\Omega^{2}L^{2}}{(1 + \Omega^{2}L^{2})^{2}}$$
 (5-1)

with L = 1000 ft.

The probability density of  $\sigma_{\mathrm{W}}$  is defined in the mathematical form

$$\hat{f}(\sigma_{W}) = P_{1} \frac{1}{b_{1}} \sqrt{\frac{2}{\pi}} \exp\left(-\frac{\sigma_{W}^{2}}{2b_{1}^{2}}\right) + P_{2} \frac{1}{b_{2}} \sqrt{\frac{2}{\pi}} \exp\left(-\frac{\sigma_{W}^{2}}{2b_{2}^{2}}\right) (5-2)$$

In this expression, the two terms represent the contributions of "non-storm" and "storm" turbulence respectively.  $P_1$  and  $P_2$  are the proportions of total flight time in the two types of turbulence, and  $b_1$  and  $b_2$  are constants indicative of the probable intensities. More precisely,  $b_1$  is the root-mean-square value of  $\sigma_w$  considering only the time spent in non-storm turbulence, and  $b_2$  is the root-mean-square value of  $\sigma_w$  for the time spent in storm turbulence. A sharp distinction between storm and non-storm turbulence is not required, as Equation 5-2 can be regarded as an empirical equation covering all types of turbulence collectively without regard to the motivation leading to its expression as a sum of two terms. The quantities  $P_1$ ,  $P_2$ ,  $b_1$ , and  $b_2$  depend upon altitude, and values are provided in TN 4332 for various altitude bands.

A particular advantage of the mathematical form utilized in equation 5-2 is that it leads to a simple and convenient equation for load exceedances,

$$\frac{N(y)}{N_0} = P_1 \exp(-\frac{y/\bar{A}}{b_1}) + P_2 \exp(-\frac{y/\bar{A}}{b_2})$$
 (5-3)

In this equation, y is any load quantity, such as airplane center of gravity acceleration.  $\bar{A}$  and  $N_{0}$  are quantities obtained by solution of the airplane equations of motion;  $\bar{A}$  is the ratio  $\sigma_{y}/\sigma_{w}$ , and  $N_{0}$  is a characteristic frequency given by the radius of gyration of the power-spectral density curve for y with respect to zero frequency. Equation 5-3 is derived by use of Equation, 5-2 in conjunction with Rice's equation for exceedances at a given rms level (Equation 2 of Reference 5),

$$N(y) = N_0 \exp \left(-\frac{y^2}{2a_y^2}\right)$$

(As indicated in Reference 5, Rice's equation is an exact expression for the number of positive-slope crossings per second of given values of y; it is an approximate expression for the number of maximums - or peaks - per second above a given value of y. The approximation is extremely close for a time history characterized by a narrow-band power spectral density. For typical gust load time histories, which are relatively wide-band, the approximation is still very good, especially at y/o values greater than 2.)

For any given altitude,  $P_1$ ,  $P_2$ ,  $b_1$ , and  $b_2$  in Equation 5-3 are available as the parameters defining the probability distribution of  $\sigma_w$ . A plot of  $N(y)/N_0$  vs  $y/\bar{A}$ , as defined by Equation 5-3, then provides a generalized exceedance curve for that altitude. An actual exceedance curve for a particular load quantit on a given airplane then follows by multiplying ordinates by  $N_0$  and abscissas by  $\bar{A}$ .

It is seen that the same four parameters,  $P_1$ ,  $P_2$ ,  $b_1$ , and  $b_2$ , define both the  $\sigma_w$  distributions and the generalized exceedance curves. Thus the generalized exceedance curves provide an alternate to the probability density as a means of describing the statistical distribution of  $\sigma_w$ . This alternate form of presentation is now generally preferred, because of its close relation to the way in which the  $\sigma_w$  distributions are actually used in loads determination.

Inasmuch as TN 4332 represented a rather preliminary effort to define atmospheric turbulence in power-spectral form, it was considered desirable to up-date the information given therein, for use in the present study, to whatever extent this could be done without embarking on a major program.

Accordingly, a meeting was held at the NASA Langley Research Center in March, 1964, for the purpose of determining what improvements in the TN 4332 atmospheric model should be made. This meeting was attended by representatives of NASA, FAA, Lockheed and Boeing.

#### 5.2 Power-Spectral Density Function

As a result of information presented by NASA at this meeting and now available in references 13 and 14, it was the consensus that the gust power-spectral density function should be taken as described by the "isotropic turbulence" equation,

$$\Phi (\Omega) = \frac{\sigma^2 \tilde{L}}{\pi} \frac{1 + \frac{8}{3} (1.339 L\Omega)^2}{\left[1 + (1.339 L\Omega)^2\right]^{11/6}}$$
 (5-4)

with L = 2500 ft. This equation is plotted in Fig. 5-1. The quantity  $\Omega$  is a reduced frequency with units of radians per foot. The constant L is generally called the "scale of turbulence" and defines the frequency at which the bend in the curve occurs (approximately  $\Omega$  L = 1). It is seen that at the higher frequencies  $\Phi$  varies as  $\Omega$ -5/3.

Because of the generally isotropic nature of atmospheric turbulence, the above equation is considered to apply equally to the vertical and lateral components. It should be remarked, however, that the power spectrum of the component parallel to the flight path is inherently somewhat different; it can be derived from the above equation, if needed, by means of relations noted in Reference 14.

For altitudes less than about 2500 ft. above the ground, the scale of turbulence is probably somewhat smaller than the 2500 ft. value selected. For convenience in performing loads analyses, however, the 2500 ft. value will be retained for all altitudes. The effect on design loads as negligible for aircraft having gust response characteristics similar to those of current propeller driven aircraft. Somewhat conservative loads might result for a new vehicle spending large amounts of time in this altitude range if it were to fly very substantially faster than present airplanes or respond at a very much lower frequency.

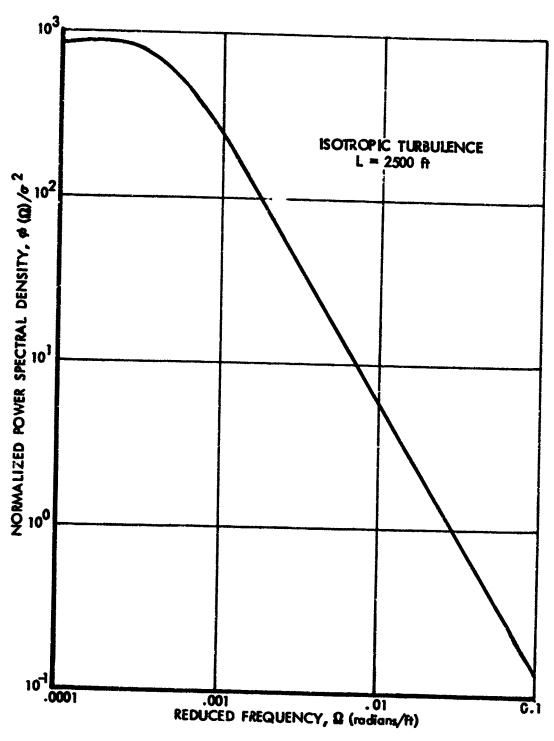


FIGURE 5-1. GUST POWER SPECTRAL DENSITY FUNCTION

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### 5.3 Probability Distributions of Gw

With respect to the  $\sigma_{\rm W}$  robability distributions, NASA indicated that they had done no specific work toward refining the b<sub>1</sub>, b<sub>2</sub>, P<sub>1</sub>, and P<sub>2</sub> values given in NASA TN 4332. They felt that such a study should involve a complete redetermination, and it was agreed that this could not be unitable and completed in time for use in the present program. NASA iid exphasize the preliminary nature of the numbers presented in the local and indicated that if certain simple modifications clearly applied ared to represent an improvement in the distributions they could see no objection to such modifications being made for the purpose of the present program.

It might be remarked that, in the present program, any overall conservatism or unconservatism in the  $\sigma_{\rm W}$  distributions will be automatically effset in the determinations of a design frequency of exceedance. However, it is obviously important that the relative variation of turbulence severity with altitude be accurately represented. Also, it is advantageous for the over-all level of severity to be as realistic as possible - first, in order to avoid giving a misleading impression of actual frequencies of exceedance of limit strength and, second, so that the  $\sigma_{\rm W}$  distributions can be used directly in fatigue calculations.

Accordingly, further consideration was given to simple means of improving the  $\sigma_{\rm W}$  distributions presented in TN 4332.

It was found that in ASD TR 61-235, "Optimum Fatigue Spectra" (Reference 15), an extensive re-analysis of available VGH data has already been accomplished. This included not only a substantial sample of the airline data, but also data from military operations at the higher altitudes. The analysis utilized the original  $\Delta n$  measurements from the VGH records; these were immediately converted to y/A form and plotted vs  $N(y)/N_O$ .

Since  $P_1$ ,  $P_2$ ,  $b_1$ , and  $b_2$  follow directly from the intercept and slope of such curves, the determination of  $U_{de}$ 's was bypassed; thus it was unnecessary to assume average airplane characteristics in converting the  $U_{de}$  exceedance data to  $\sigma_w$  form, as had been done in TN 4332.

The difference between the ASD TR 61-235 and the TN 4332  $\sigma_w$  distributions was found not to be great. However, the ASD TR 61-235 distributions do tend to be somewhat less severe. As indicated in Section 5.6, this is in the direction necessary to achieve the best agreement between analytically predicted and measured  $\Delta n$  exceedance for the three airplanes considered in this study.

In view of these advantages, a decision was reached to base the  $\sigma_{\rm W}$  distributions to be used in the present study on those presented in ASD TR 61-235.

Certain modifications, however, to the b and P values presented therein were considered necessary. As a minimum, the bl and b2 values quoted required modification to account for the difference in spectrum shape. In addition, it was considered desirable to make other simple changes, in order to place the determination on a slightly more rational basis and to eliminate at least a part of the conservation believed still to be present.

The computation of the modified b<sub>1</sub> and b<sub>2</sub> values from those given in ASD TR 61-235 is shown in Tables 5-1 and 5-2. The computations require certain assumptions as to airplane characteristics, and for this purpose the Table Ia and Table Ib airplanes of IN 4332 are assumed. These two airplanes have quite similar gust response characteristics; for consistency with IN 4332, however, the Table Ia airplane is used for determining modified b<sub>1</sub> values and the Table Ib airplane for the b<sub>2</sub> values.

The modification of the b1 and b2 values is based on a consideration of how these quantities are determined from the original  $\Delta n$  data. For a given altitude band, frequency of exceedance of  $\Delta n$  would be plotted, on a log scale, vs  $\Delta n$ . This plot would be made in the generalized form of N(y)/No vs y/A by dividing exceedances by N<sub>0</sub> and  $\Delta n$ 's by  $\overline{A}$ . On the semi-log coordinates, the non-storm and storm contributions will each plot as straight lines. P1 and P2 are given by the intercepts of these lines with the vertical axis; and b1 and b2 are proportional to the reciprocals of the slopes. Consequently, the numerical values obtained for b1 and b2 will be inversely proportional to the  $\overline{A}$  value used in obtaining the plot.

In both TN 4332 and ASD-TR-61-235,  $\overline{\Lambda}$  is obtained by means of the equation,

$$\overline{A} = \frac{\rho C_{L_{\alpha}} SV_{T}}{2W} K_{\sigma}$$
 (5-5)

The dimensionless coefficient  $K_{\sigma}$  is evaluated using simple theory, on the assumption that the airplane is rigid and free to plunge (move vertically) but not pitch. The resulting  $\overline{A}$  values may, however, be adjusted by estimated factors to account for the effects of elastic mode response and freedom in pitch.

Plots of  $K_{\sigma}$  as a function of a dimensionless mass parameter and of the ratio of scale of turbulence to mean wing chord are given in Figure 7

TABLE 5-1. RE-EVALUATION OF PARAMETER b) BASED ON ASD TR 61-235 DATA

<b>©</b>	Lq	8	3.903	3.64	3.42	3.59	3.27	3.15	2.93	3.28	3.82	2.93
@	<sup>K</sup> b <sub>L</sub> 1.15 Kg <sub>I</sub>	<u>©</u> 1.15 Φ	1.435	1.316	1.195	1.190	1.144	1.144	1.19	1.069	1.019	-992
Φ	K <sub>G</sub> Isotropic, L = 2500 FT	Function or (5) Fig. 5-2	<b>5</b> η€′	.350	• 360	.376	, 427	784.	442.	.63	. 708	. 767
0	K Topmann	or Or 1272, TR 1272, Fig. 7	.570	.530	495	.515	.562	.635	• 700	.775	.830	.875
0	<u>#</u>	⊕ 1.15	17.90	18.51	19.61	22.07	28.1	39.5	57.0	91.8	148.0	231.3
<b>②</b>	Pratt #	TN4332 Table Ia	20.6	21.3	22.6	25.4	32.3	45.4	65.5	105.0	170.0	266.0
0	ы		200	750	930	1000	1000	1000	1000	1000	1000	1000
@	b <sub>1</sub> ASD TR 61-235	ASD TR 61-235 Table I	2-72	2.77	5.86	3.6	2.86	2.75	2,62	3.07	3.75	2.95
Θ	n Ft.		0-1000	1000- 2500	2500- 5000	5000-10000	10000-20000	20000-30000	30000-1-0000	1,0000-50000	00009-00005	60000-70000

 $\overline{W}$  = 77000 Lb; S = 1463 Ft<sup>2</sup>;  $\overline{G}$  = 13.7 Ft;  $GL_{QG}$  = 4.95 per radian (wing alone) and (1.15) (4.95) = 5.70 per radian (airplane); isotropic turbulence spectrum, L = 2500 Ft. Date Assumed:

TABLE 5-2. RE-EVALUATION OF PARAMETER b2 BASED ON ASD TR 61-235 DATA

<b>©</b>	Z <sub>Q</sub>	<u>©</u>	7.76	1.56	8.17	9.52	10.52	11.88	₹.6	8.81	おこ	4.33
@	18 21.1	() () ()	1.427	1.248	1.1				1.121	1.08¢	70.1	.961
Θ	K Isotropic, Lassoo ft	Function or S	.350	.355	.370	.380	۰415	694.	.533	.614	₹69.	.762
9	K <sub>G</sub> Liepmann	or Of & Constraint Training Fig. 7	.575	.510	. 485	56 <b>†</b> °	945.	.620	.688	. 766	.830	, 843
9	ц	(4) 1.15	50.59	21.29	22.59	25.33	32.3	45.2	65.6	105.2	170.0	2,992
<b>④</b>	Pratt µ	TN4332 Table Ib	23.7	24.5	56.0	29.15	37.1	52.0	72·4	121.0	195.4	306.7.
<b>©</b>	1		500	750	930	1000	1000	1000	1000	1000	1000	1000
0	b <sub>2</sub> ASD TR 61-235	ASD TR 61-235 Table I	<b>ग्</b> ग*\$	90.9	7.17	8.16	9.20	10.35	8.78	8.13	6.77	4.51
0	r Fr		0- 1000	1000- 2500	2500- 5000	5000-10000	10000-20000	20000-30000	30000-1,0000	4000-50000	20000-60000	60000-70000

W=30000 Lb; S=662.4  ${\rm Pt}^2$ ;  $\overline{C}=10.5$   ${\rm Ft}_3{\rm Cr}_{\rm Q}=4.83$  per radian (wing alone) and (1.15) (4.83) = 5.55 per radian (airplane); isotropic turbulence spectrum, L = 2500 Ft. Data Assumed:

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of NACA Report 1272 (Reference 5), based on theory developed by Fung in Reference 16. Similar curves, utilizing more exact expressions for the unsteady lift growth functions, are given in Figure 70 of ASD TR 61-235 and were used therein. Both of these sets of curves assume the Liepmann shape of power-spectral density function. For use with the isotropic turbulence spectral shape, a new set of curves has been obtained. These are shown in Figure 5-2. The assumptions regarding lift growth are the same as for the curves in TR 1272.

The spectral shape affects  $\overline{A}$  only through the coefficient  $K_{\sigma}$ , and it is clear that  $b_1$  and  $b_2$  vary inversely as  $K_{\sigma}$ . In Tables 5-1 and 5-2, the  $K_{\sigma}$  curves in NACA TR 1272 and in Figure 5-2 herein are used to determine the  $K_{\sigma}$  ratio. It should be remarked, incidentally, that in TR 1272 the mass parameter is defined in terms of an assumed lift curve slope of  $2\pi$ ; in the computations in Tables 5-1 and 5-2, however, as well as in the original evaluation of  $b_1$  and  $b_2$  in ASD TR 61-235, the same value of lift curve slope selected for use explicitly in Equation 5-5 was also used in evaluating the mass parameter.

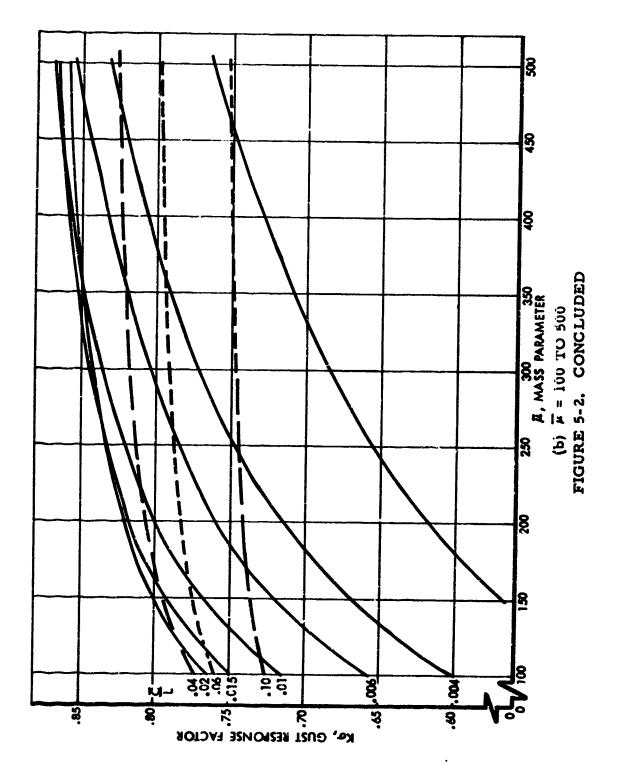
In the ASD TR 61-235 determination of b1 and b2 values (as well as in the TN 4332 determination), the lift curve slope,  $C_{L_{\alpha}}$ , was based upon an approximate formula that gives an excellent approximation to the wing lift curve slope but underestimates the airplane lift curve slope by some 15%. The airplane lift curve slope would appear to be the more rational one to use. Also, it leads to lower values of b1 and b2, which, as noted above, are desirable. Consequently, the  $\overline{A}$  ratio in Tables 5-1 and 5-2 includes also a 1.15 factor to account for the greater  $C_{L_{\alpha}}$  believed to be realistic. This increased  $C_{L_{\alpha}}$  is, of course, also used in evaluating the mass parameter.

No correction for pitch is included. Response calculations for the Model 749 with and without a pitch freedom indicate roughly a 7% reduction in A due to pitch. This percentage is quite small, and the exact value obtained will depend somewhat on the extent to which it is desired to include, at the same time, differences in the unsteady lift growth functions between those assumed in the simple "Fung" analysis and those applied on the various components in the more refined analyses. Furthermore, the pitch effect on the Model 749 undoubtedly differs somewhat from that of other airplanes from which WiH results were obtained for use in ASD TR 61-235. As a result of these considerations, it is believed desirable to ignore the effect of pitch.

(It might be remarked that the correction necessary to account for pitch effects can be minimized by appropriate selection of lift curve slope in the plunge-only analysis. If wing-alone lift curve slope had been used instead of airplane lift curve slope, the indicated correction for pitch would have been comparable in magnitude, although opposite in direction.

(a)  $\overline{\mu}$  = 0 TO 200 FIGURE 5-2. GUST RESPONSE FACTOR FOR ISCTROPIC TURBULENCE SPECTRUM

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Therefore, in this instance the criterion of a minimum correction for pitch was not helpful in selecting the basis for lift curve slope.)

No correction for elastic mode response is included in Tables 5-1 and 5-2, as this is considered to have been adequately accounted for in the original work. In the calculation of b1 and b2 values in ASD TR 61-235, calculated dynamic factors were used for the DC-6 and DC-7 airplanes. For all other airplanes it was reasonably assumed either that the dynamic factor was negligible or that the dynamic factor, static flexibility effect on lift curve slope, and pitch effect were mutually offsetting.

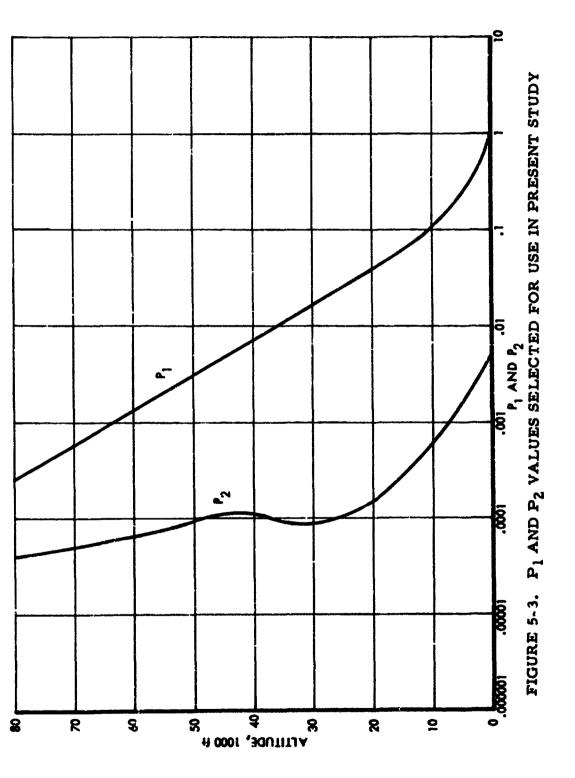
With the foregoing as background, the computations made in Tables 5-1 and 5-2 to obtain modified b values are self-explanatory.

P<sub>1</sub> and P<sub>2</sub> are also modified. The ASD TR 61-235 determination, like that in TN 4332, utilized estimated N<sub>0</sub> values of .7 for non-storm turbulence and .5 for storm turbulence. On the other hand, calculated values for typical airplanes (Lockheed Model 749 and Model 188 and also the Boeing 707/720 series) average about 1.1 cps. Consequently, the TN 4332 P<sub>1</sub> values are multiplied by .7/1.1 and the P<sub>2</sub> values by .5/1.1.

The resulting P<sub>1</sub>, P<sub>2</sub>, b<sub>1</sub>, and b<sub>2</sub> values are plotted as functions of altitude in Figures 5-3 and 5-4. These curves, in conjunction with the given shape of power-spectral density function, constitute the required model of the atmosphere.

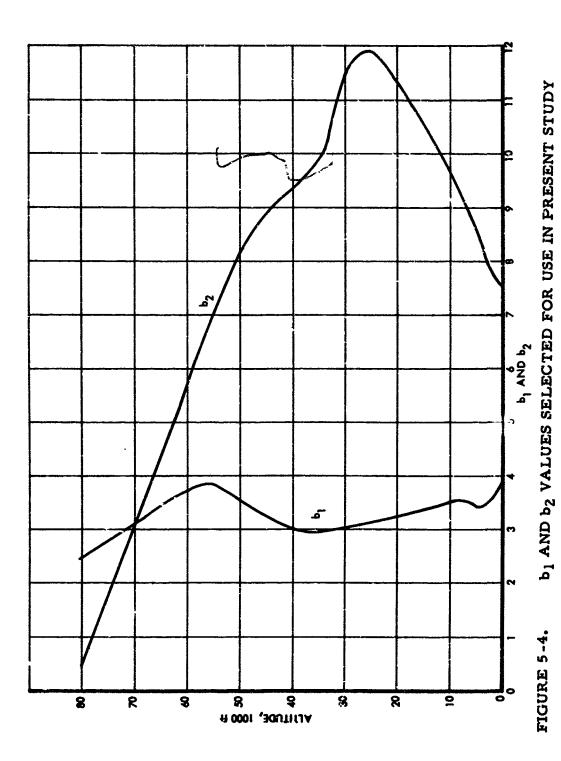
Generalized exceedance curves reflecting these P and b values are shown in Figure 5-5. It is suggested that these curves not be used for actual computations, because of the non-linearity of the interpolation between adjacent curves. Instead, P and b values should be read from Figures 5-3 and 5-4.

As a matter of interest, comparisons of the TN 4332 and ASD TR 61-235  $\sigma_W$  distributions are shown in Appendix A. These are in the form of plot vs altitude of the respective P and b values, and also as comparisons of the respective generalized exceedance curves at various altitudes. The comparisons are shown first for the probability distributions exactly as defined in these two documents. The comparisons are then repeated based on the distributions with appropriate modifications, comparable to those described above for the ASD TR 61-235 distributions. On either basis, it is found that the differences in the b and P values appear rather great, but that the resulting generalized exceedance curves show much closer agreement. At frequencies of exceedance in the vicinity of limit strength  $(N(y)/N_0 = 10^{-8} \text{ to } 10^{-6})$ , and over the altitude range of primary interest, the ASD TR 61-235 distributions are slightly less severe than the TN 4332 distributions, as desired.



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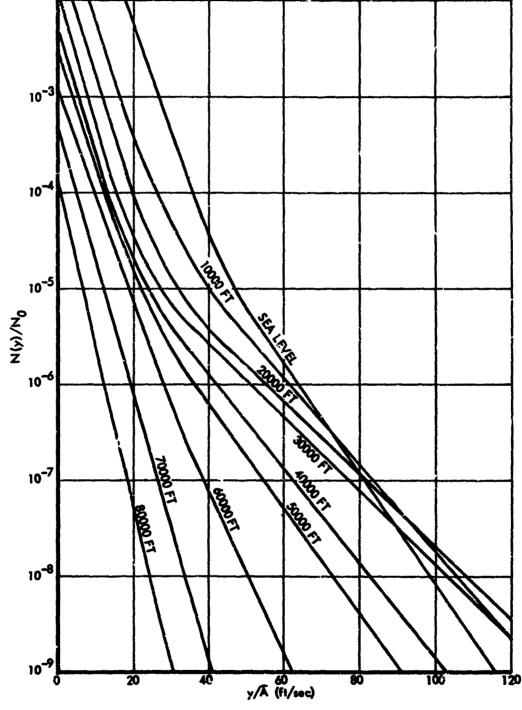


FIGURE 5-5. GENERALIZED EXCEEDANCE CURVES REFLECTING • W DISTRIBUTIONS USED IN PRESENT STUDY

# 5.4 Lateral-Gust ow Distributions

Evidence to date is that atmospheric turbulence tends strongly to be isotropic, except within a few hundred feet of the ground. (See, for example, Reference 14.) As a result,  $\sigma_{\rm W}$  distributions obtained from vertical gust measurements are considered to apply equally to the lateral component of turbulence.

For convenience, the symbol  $\sigma_{\rm W}$  is applied in this report to the lateral as well as the vertical component of turbulence, despite the origin of the subscript w as a velocity in the z direction.

# 5.5 Generalized Exceedance Curves for Use With Design Envelope Criterion

To assist in defining design values of  $\sigma_W \eta_d$  for use in the design envelope form of criterion, generalized exceedance curves are plotted in a different form in Figure 5-6. Instead of plotting N(y)/N<sub>O</sub> vs y/A for various altitudes, as in Figure 5-5, y/A is now plotted vs altitude for various values of N(y)/N<sub>O</sub>. The resulting curves are shown by the dash lines in Figure 5-6.

These curves are then simplified for design use as indicated by the solid lines. Because of the complete absence of data above 80000 ft., curves are conservatively defined for design use by constant y/A values above this altitude. As an aid in evaluating the fairing of the curves, the same curves are transformed from a true gust velocity basis to an equivalent gust velocity basis in Fig. 5-7 (i.e., if A is defined as oy/owtrue, in accordance with usual practice, use Fig. 5-6; if A is defined as  $\sigma_y/\sigma_{\text{weouiv}}$ , which would correspond more closely to the usual discrete pust treatment, use Fig. 5-7.) The waviness appearing in the dash lines in Figures 5-6 and 5-7 does not necessarily indicate improper fairing of the P1, P2, b1, and b2 data in Figures 5-3 and 5-4. It is interesting to note, for example, that the particular bend in the curves at 15000 ft. bears a similarity to the Ude data shown in Fig. 8 of NASA TN D-29 (Reference 17). In TN D-29 the Ude's in the 15000 - 20000 ft. band are markedly lower than the trend indicated by the other altitude bands. In the determination of b's and P's in TN 4332, however, the departure from the general trend in the 15000 - 20000 ft. band was faired out. Although the waviness shown by the dash lines is perhaps, therefore, a true reflection of the atmosphere, a rather gross fairing appears appropriate for use in a design ervelope criterion. The fact that the airplane must be designed for a range of altitudes tends to compensate for the fact that in some narrow altitude bands less strength might actually be required than indicated by the criterion,

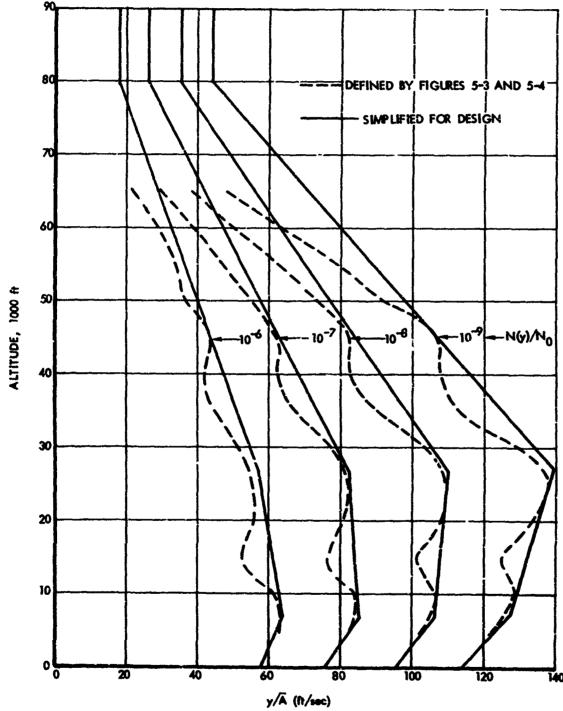


FIGURE 5-6. VARIATION OF  $y/\overline{A}$  WITH ALTITUDE FOR CONSTANT  $N(y)/N_0$ 

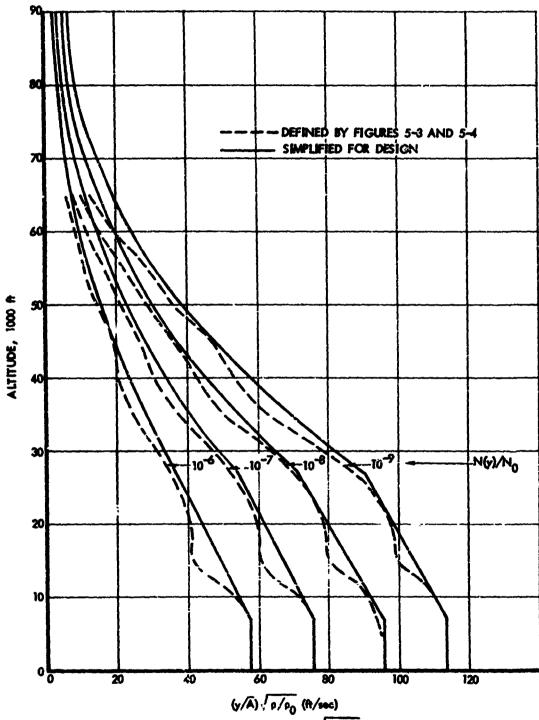


FIGURE 5-7. VARIATION OF  $(y/\overline{A})\sqrt{\rho/\rho_0}$  WITH ALTITUDE FOR CONSTANT  $N(y)/N_0$ 

The simplified curves in Figures 5-6 and 5-7 are used only in connection with the design envelope criterion; in the mission analysis approach, the data reflected by the dash lines in these figures are retained.

For use in later portions of this report, the solid lines of Figure 5-6 are repeated in Figure 5-8. Intermediate curves are added to facilitate interpolating, and the range is extended to higher load levels. (This extension is by linear extrapolation, which is valid because of the linearity of the  $N(y)/N_0$  vs  $y/\overline{A}$  curves in this region, as indicated in Figure 5-5). As these curves are intended to be used to establish design levels, the abscissas are relabeled  $\sigma_W \eta_d$ , the design load equivalent of  $y/\overline{A}$  (Section 4-2).

### 5.6 VGH and VG Comparisons

A qualitative check of the atmospheric model derived above can be obtained by comparing airplane c.g. exceedance curves calculated for the three reference airplanes, using the model, with curves obtained from VG and VGH measurements.

Such comparisons are shown in Figures 5-9, 5-10, and 5-11. The "mission analysis" curves are based upon the results given in Section 9 and Appendix B for the three reference airplanes. VG and VGH data were taken from the sources indicated (References 9, 17, and 18), but were changed to the form of cumulative exceedances of positive load factor per hour for this comparison.

Inasmuch as neither VG nor VGH data are available for the Model 720B, the VGH curve shown is for a Model 707-300. This curve is then adjusted to reflect differences in operating usage between the 707-300 and the 720B. The ratio by which the 707-300 exceedances were increased to compare with the 720B was obtained by recalculating the 720B exceedances using weighting factors for the five flight profiles representative of 707-300 operations. Dividing the exceedances calculated using the actual 720B weighting factors by the exceedances calculated using the 707-300 weighting factors gives a ratio of 1.37; this was then applied to the 707-300 exceedances obtained from the VCH data.

It might be remarked that, for the Model 749, the descent speeds used in the analysis were slightly lower than prevailed at the time the accelerations were measured (see Section 6.2); if consistent descent speeds had been used, the solid line in Figure 5-9 would have moved slightly to the right.

In Figures 5-9 through 5-11, it is seen that the agreement between predicted and measured data, although not perfect, is sufficiently close to indicate that the choice of atmospheric model is reasonable.

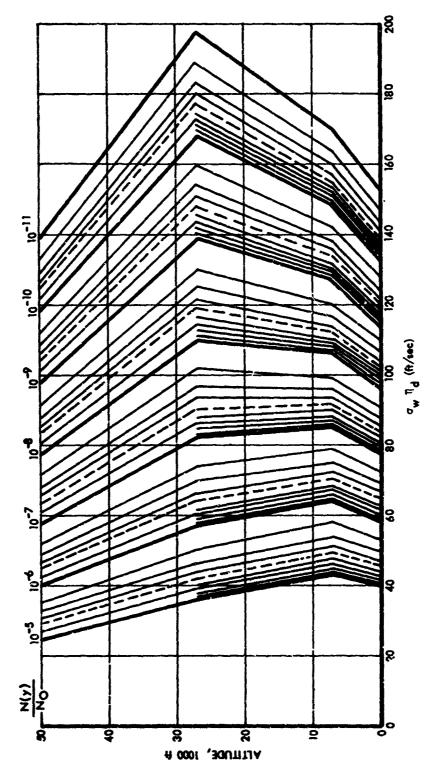


FIGURE 5-8. VARIATION OF ownd WITH ALTITUDE

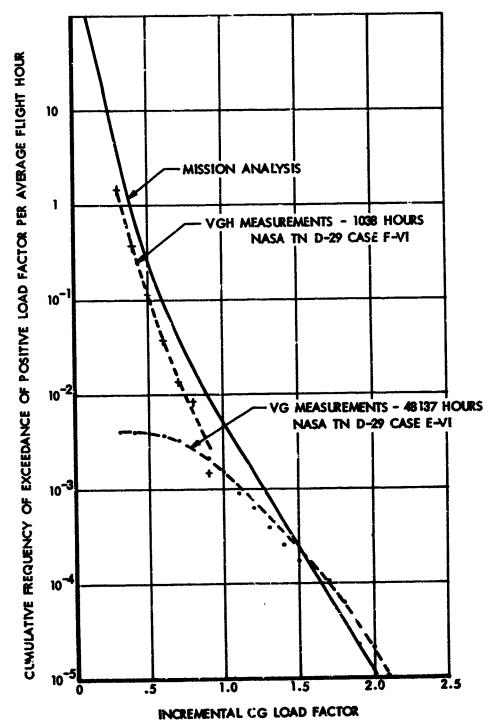


FIGURE 5-9. COMPARISON OF PREDICTED WITH MEASURED LOAD FACTOR EXCEEDANCES, MODEL 749

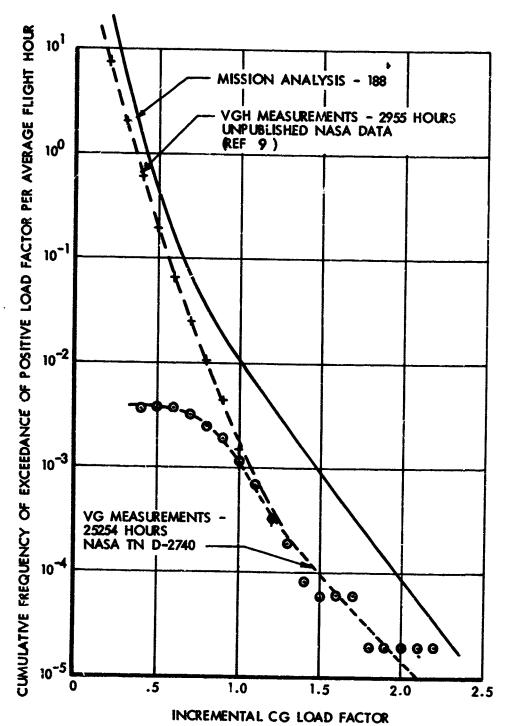


FIGURE 5-10. COMPARISON OF PREDICTED WITH MEASURED LOAD FACTOR EXCEEDANCES, MODEL 188

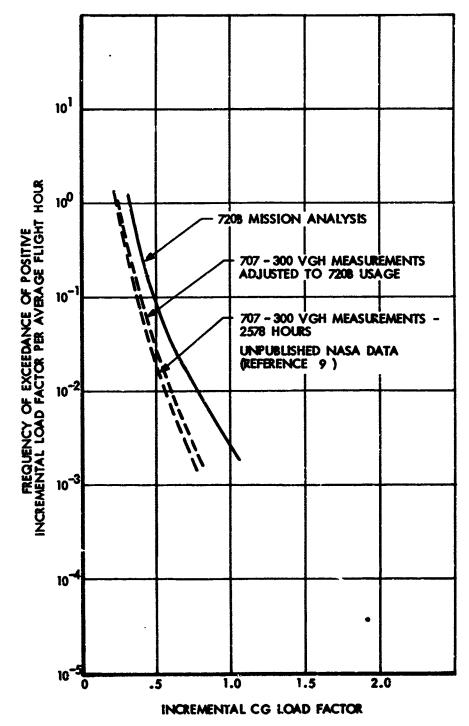


FIGURE 5-11. COMPARISON OF PREDICTED WITH MEASURED LOAD FACTOR EXCEEDANCES, MODEL 720B

Generally, the computed accelerations are somewhat greater than the measured, indicating a somewhat conservative model. The various steps taken to reduce the severity of the model, described earlier, thus appear to be well justified.

#### 5.7 Future Improvements

It is generally recognized that further work to improve the atmospheric models currently available would be highly desirable. The appropriate shape for the power-spectral density function and value of the scale of turbulence are still matters of conjecture; and much greater confidence in the  $\sigma_{\rm W}$  distributions would result if these were rederived from the vast store of available VG and VGH data utilizing directly  $\bar{\rm A}$  and  $N_{\rm O}$  values obtained from dynamic analyses of the respective airplanes.

However, it must be borne in mind that the design levels (N(y)) and  $\sigma_w\eta_d$  obtained as a result of the present study are based upon analysis of existing satisfactory airplanes, using the particular model of the atmosphere defined herein. Changes in the atmospheric model would ordinarily require changes in the design levels, and definition of the revised levels would be likely to require extensive reanalysis of the reference airplanes.

Any changes whatever in the shape of the power-spectral density function, including a change in the value of the scale of turbulence, would clearly require such reanalysis.

Changes in the b and P values in the altitude range where the reference airplanes operate would also require such reanalysis. However, the greatest uncertainty in the b and P values is at the higher altitudes, say above 40,000 ft. Improvements in the b and P values in this altitude range could be made freely, as the limit strength values of N(y) and  $\sigma_w \eta_d$  for the reference airplanes would not be affected. It is possible, too, that, even at somewhat lower altitudes, changes in the b and P values could be shown not to affect the design levels selected. Consideration would have to be given, in any particular case, to the magnitude of the proposed change, which of the reference airplanes was critical, and at what altitude it was critical.

# 6 MISSION PROFILES FOR REFERENCE AIRPLANES

#### 6.1 Model 188

The mission profiles for use in the Model 188 mission analysis are based upon the following sources of data:

- (1) NASA VGH statistical data given in References 9, 10, and 11;
- (2) Information gathered from contacts with the various airlines operating Electra airplanes;
- (3) Various published and unpublished Lockheed reports providing weight and operating data on Electra airplanes.

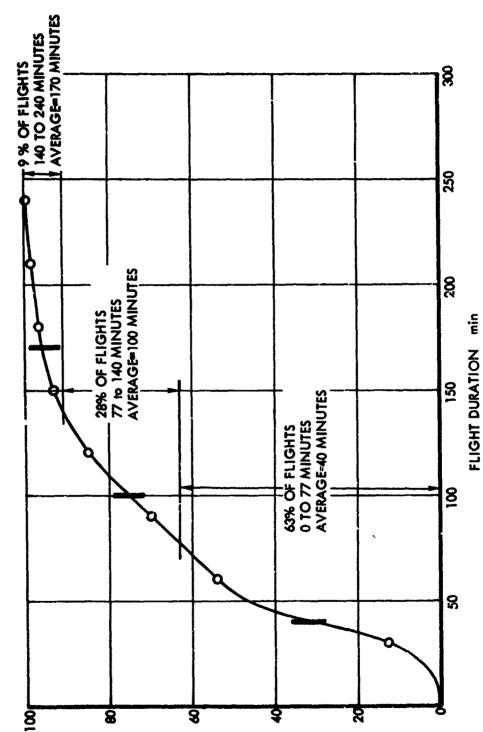
For the purpose of selecting appropriate flight durations, the distribution of flight durations given by Reference 9 is plotted in Figure 6-1. The following three mission durations were selected to represent this distribution:

Duration	% of Flights
40 min.	63
100 min.	28
170 min.	9

The tendercy of average cruise altitude to increase with flight duration is depicted in Figure 6-2, which is prepared from data presented in Reference 10. The cruise altitudes appropriate to the three mission durations are read from the faired curve as follows:

Duration	Cruise Altitude
40 min.	11,000 ft.
100 min.	11,000 ft. 16,000 ft.
170 min.	18,000 ft.

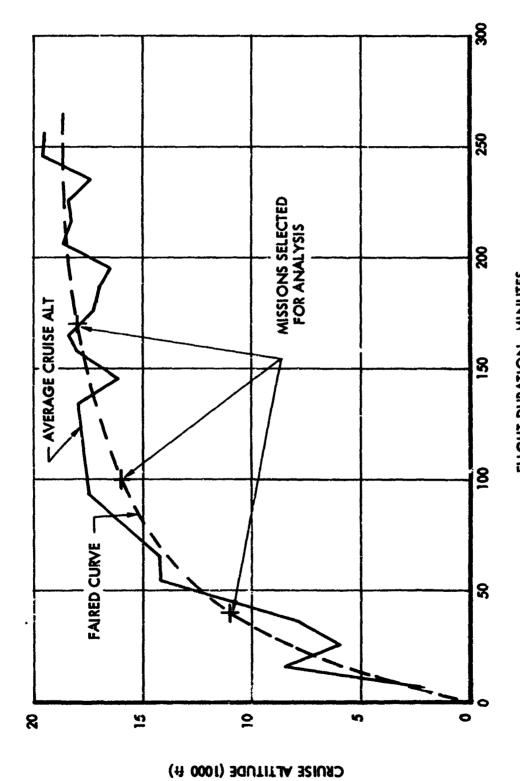
Representative speeds in climb, cruise and descent, based on data in Reference 9, are shown in Figures 6-3 - 6-5 as a function of altitude. (In Reference 9, all speeds quoted are indicated airspeeds; these are assumed equal to equivalent airspeeds.) For the purpose of establishing mission profiles, average speeds are indicated. The average climb speeds are simple averages taken directly from Reference 9. In the cases of cruise and descent, however, the ranges of speed are so great that use of a simple average would be unrealistic. For example, consider the effect on a frequency of exceedance curve for gust loads if a



% OF FLIGHTS LESS THAN JIVEN DURATION

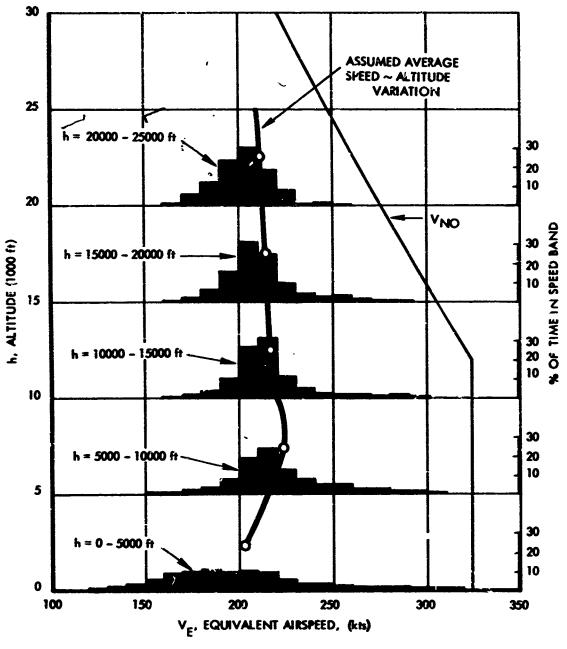
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FIGURE 6-1. FLIGHT DURATIONS, MODEL 188



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FIGURE 6-2. VARIATION OF AVERAGE CRUISE ALTITUDE WITH FLIGHT DURATION, MODEL 188 FLIGHT DURATION, MINUTES



Pending (Bankley New York)

FIGURE 6-3. DISTRIBUTIONS OF AIRSPEED IN CLIMB, MODEL 188

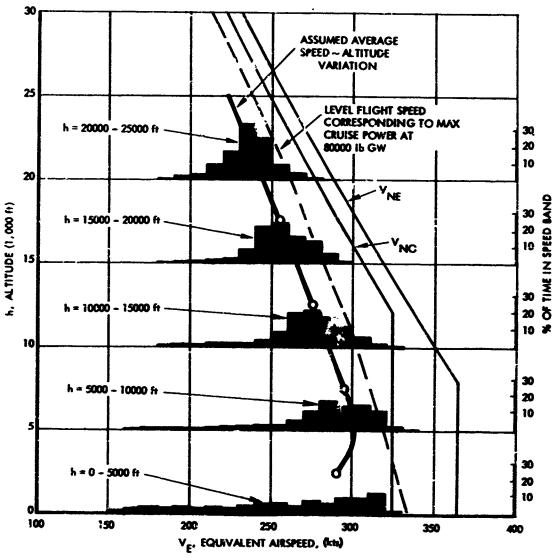


FIGURE 6-4. DISTRIBUTION OF AIRSPEED IN CRUISE, MODEL 188

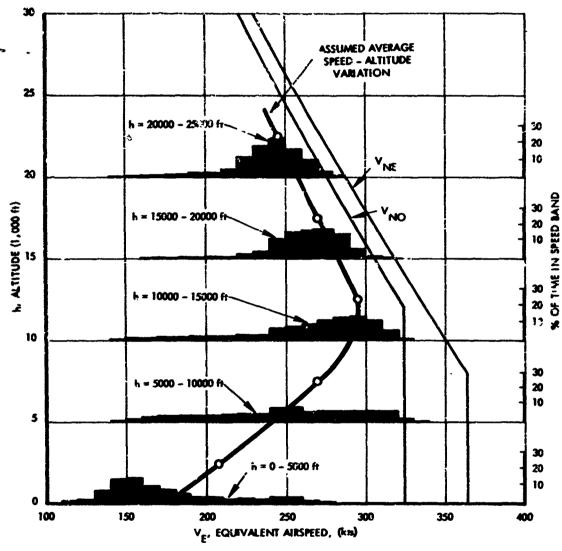


FIGURE 6-5. DISTRIBUTION OF AIRSPEED IN DESCENT, MODEL 188

given speed distribution were to be divided into a high speed and a low speed band, with the average speed in each band used for analysis. The low speed band would contribute negligibly to the exceedance curve. The high speed band would contribute only half as many load cycles as the total distribution, but its average speed would be appreciably higher. The increase in load due to the higher speed would have a far greater effect than the reduction in cycles. In order to approximate this effect, the "average" speeds shown for cruise and descent have been increased somewhat over the simple averages stated in Reference 9.

The mission flight profiles thus established are shown in Figures 6-6a thru 6-5e.

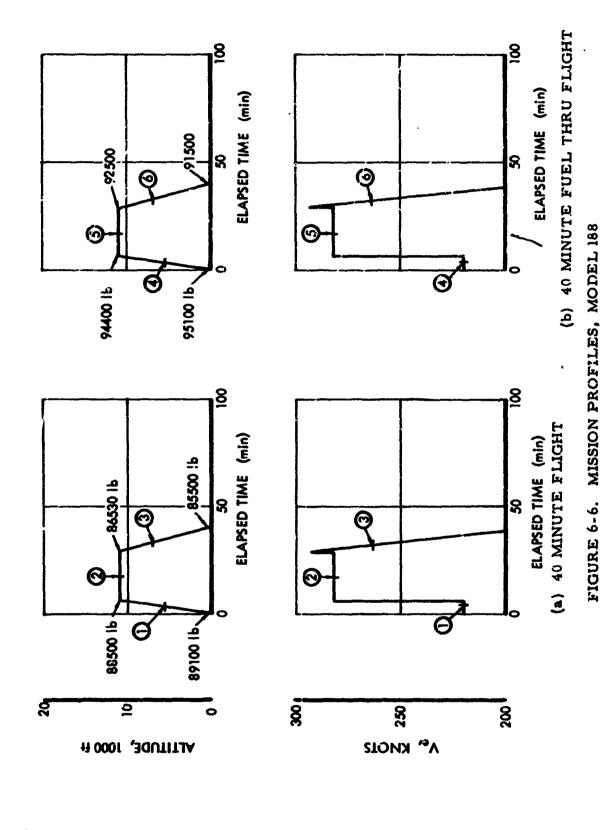
The airplane weights shown in Figure 6-6 were next determined.

Operating weight empty was determined by first examining the weight data available at the time of delivery of the airplanes to the various airlines. The average operating weight empty for the various airlines ranged generally from 59400 lb. to 61800 lb., with one airline as high as 64200 lb. (These weights include an adjustment to account for the increase in weight empty due to the "LEAP" modifications made to all airplanes after delivery.) These values were then increased to account for weight growth after delivery by use of recent Eastern Air Lines information indicating a weight growth of 1100 lb. for their airplanes. Based on the foregoing, a value of operating weight empty of 62,000 lb. was selected as representative of the fleet.

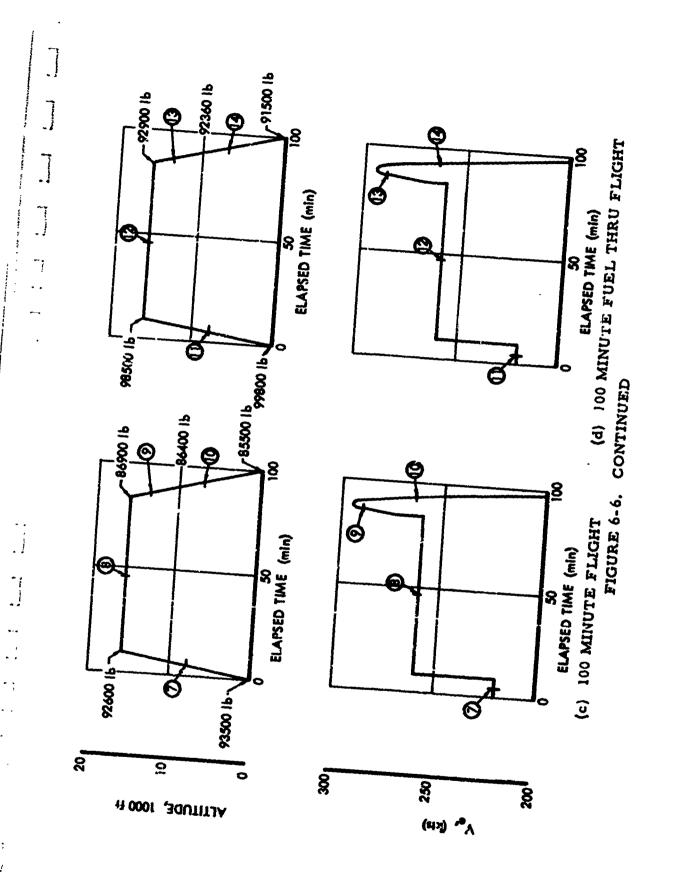
A representative payload was selected based on information obtained from several Electra operators. Average passenger load factors and other pertinent data are shown in the following table:

Airline	Passenger Load Factor	Fassenger Capacity	Assumed Weight Per Passenger (Incl. Baggage	Resulting Average Payload
AA	6 <b>3≸</b>	74	500	9300
EAL	∂ <b>0</b> ≸	73	200	8800
NAL	60-65%	<b>7</b> ₹	500	9800
PSA	80%(estim.)	96	170	13100
WAL	80%(estim.)	96	500	15400

A representative value of 12000 lb. was selected based upon the above figures. Although the Electra has provision for several thousand pounds of carge, express, and/or mail in addition to normal passenger baggage, this is seldom utilized; a nominal allowance at 500 lb. is included for this, giving a total average payload to use in analysis of 12500 lb.



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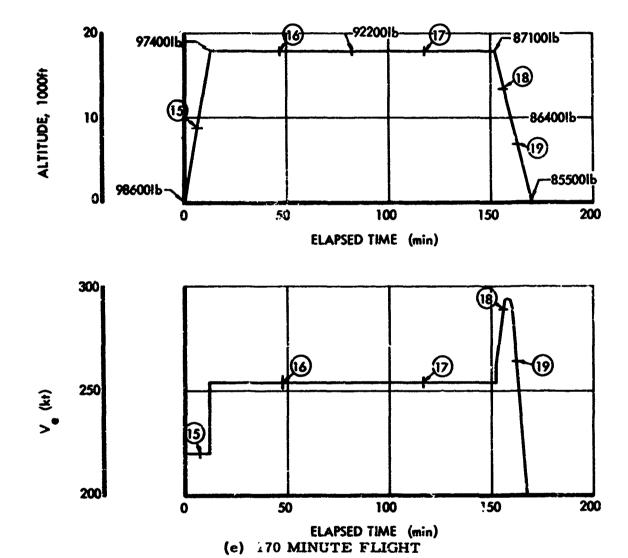


FIGURE 6-6. CONCLUDED

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The corresponding zero-fuel weight is 74,500 lb. This compares with a design maximum zero-fuel weight of 86,000 lb.

Reserve fuel at landing is the most difficult weight item to estimate reliably. Values used for analysis are based on the following considerations.

- 1. A nominal value, based primarily upon application of FAA operating regulations, would be about 8000 lb.
- 2. Based upon ~ known tendency to load fuel conservatively, average values would be expected to be somewhat greater than this perhaps on the order of 10,000 11,000 lb.
- 3. The Electra is often "fueled through" that is, fuel is not taken aboard between flights. Based on the design landing weight of 95,650 lb., an operating weight empty of 62,000 lb., and a first-leg payload of 12,500 lb., the maximum fuel at landing would be about 21,100 lb. This would permit taking off without refueling and making roughly a 170 minute flight while retaining an 8000 lb. reserve. It is clear that for short flights in series there is a likelihood of a wide variation in reserve fuel. It is estimated that roughly 30 to 35% of Electra individual flights are made without refueling before take-off.
- 4. Previous information provided to NASA and Lockheed by airlines for the purpose of computing gust velocities from airplane normal accelerations has indicated average Electra gross weights at the midpoint of the flight of 92,000 lb. to 101,000 lb. For these weights especially the latter, which is currently used by NASA to be consistent with the operating weights empty, phyloais, and flight durations indicated herein, considerably more than 8000 lb. reserve fuel is indicated.

As a result of these considerations, it is assumed that 20% of all flights will carry reserve fuel of 17,000 lb., reflecting the more extreme fuel-through situations, and the remaining 80% of flights will carry reserve fuel of 11,000 lb., reflecting non-fuel-through operations together with the remainder of the fuel-through flights. The high-reserve-fuel flights are assumed to be confined to the 40 minute and 100 minute flights, divided 75% to the 40 minute flights and 25% to the 100 minute flights.

The landing weights corresponding to the above assumptions are as follows:

Operating Wt. Empty	62000 lbs.	62000 lbs.
Payload	12500	12500
Reserve Fuel	11000	17000
Landing Wt.	85500 lbs.	91500 lbs.

The airplane weights for various points in the representative missions are found by working backwards from the landing weights using fuel consumption and performance data of reference 19.

The mission profiles thus established and shown in Fig. 6-6 are broken down into segments, or blocks, for analysis as indicated by the circled numbers in Figures 6-6a to 6-6e. These segments are tabulated in detail in Table 6-1.

The mission segments shown in Table 6-1 are then combined for analysis in Table 6-2. Only very nearly identical segments are combined, except in the case of the climb segments, which previous analyses had indicated contribute negligibly to the gust load exposure. Airplane center of gravity positions shown in Table 6-2 are based on a center of gravity midway between forward and aft limits without fuel, in accordance with the best available estimates.

## 6.2 Model 749

The mission profiles for use in the Model 749 mission analysis are based upon the same general sources of data as the Model 188 mission profiles.

The distribution of flight durations given in Reference 9 is plotted in Figure 6-7. The following three mission durations were selected as representative:

Duration	f of Flights
60 min.	63
120 min.	28
300 min.	9

The flight duration for the intermediate range mission - 120 minutes - was taken slightly lower than the actual average of 140 minutes in order to partially reflect the trend toward shorter stage lengths experienced by the Model 749 since the time the vGA data were obtained (1951 - 1953, in eastern seaboard operations).

TABLE 6-1. MISSION PROFILE DATA, MODEL 188

Percent	Of Total		26.25 28.28	· · · · · · · · · · · · · · · · · · ·	5553 0.000 0.000 0.000	4.7.	1.99.13 81.98 33.68
	W Average	eg EB	88800 87500 87500	94700 93400 92000	93100 89800 86700 86000	99000 95700 92600 92000	98,600 9,4800 9,600 9,00 9,
	h Average	Altitude FT	5500 11000 7000	5500 11000 7000	8000 16000 13500 7000	8000 16000 13500 7000	9000 18000 18000 13500 7000
	Average	Specd Knots	082 882 882 882	5 0 0 d 0 0 0 d 0 0 0 d	0000 0000 0000 0000	000 000 000 000 000 000 000	03 4. 4. 0. 49 88 88 88 88
	Time In	Per Flight Minutes	ه څاړ	1 984	<i>ం</i> గ్రాం రే	<i>૰દ</i> ૰ઇ	2500 J
	C11mb.	Enroute Or Descent	ප <b>ශ</b> අ	о м о	០ឣ឴ឩឩ	OMAA	c គេ គប ប
		Segment No.	ମରାଜ	ማጣቱ ና	F8 60	ជនជុះ	
	Percent	Total F11ghts	84	15	ଝ	ĸ	Oι
		Mission Description	ho Min	40 Min Fuel through	100 Min	100 Min Fuel through	170 Min

TABLE 6-2. SUMMARY OF LUMPED FLIGHT SEGMENTS FOR MISSION ANALYSIS, MODEL 188

	ž	ote: Zero in	uel weight =	Note: Zero fuel weight = $74500$ pounds for all cases.	for all can		
Segment Case Number	Segment Murber in Table 6-1	Climb, Furoute or Descent	Ve Average Speed Knots	h Average Altitude Feet	W Average GW Pound	C. G.	Percent of Total Airplane Time In Segment
201	2,4,7,1,1)	υ	220	7000	92300	25.2	9.80
202	ભ	ы	282	11000	87500	24.3	16.32
203	8,17	M	258	16500	89750	24.7	34.67
707	ĸ	N	282	11000	00,136	25.4	5.10
502	12,16	ĸ	256	17000	55100	25.6	14.85
506	3,10,19	A	192	7000	86500	24.1	12.,3
207	9,18	A	590	13500	86500	24.1	3.10
208	6,14	6	792	2002	92300	25.2	3.18
8	13	£	99	13500	002300	25.0	717

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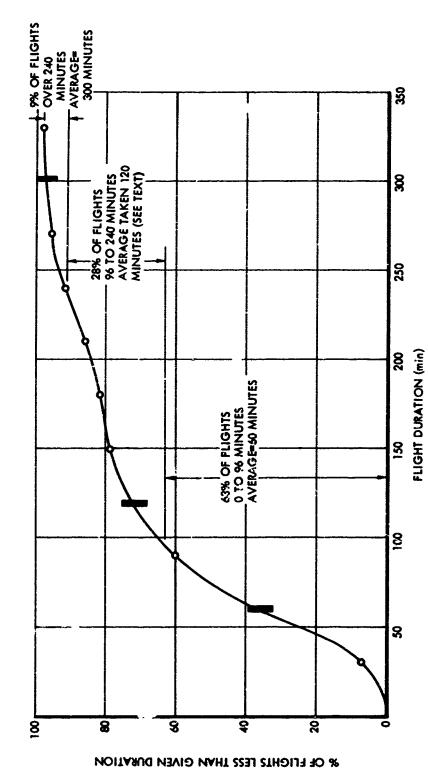


FIGURE 6-7. FLIGHT DURATIONS, MODEL 749

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The trend of average cruise altitude with flight duration is estimated in Figure 6-8. Since actual statistical information was not available, this trend was established by plotting the single over-all average cruise altitude and flight duration obtained from Reference 9 and fairing a curve through this point guided by the 188 trend. The cruise altitudes appropriate to the three mission durations are read from the resulting curve as follows:

Duration	Cruise Altitude
60 min.	8,000 ft.
120 min.	13,000 ft.
300 min.	18,000 ft.

Reasonable confirmation of this selection is indicated by Fig. 6-9, which shows the number of cruise hours spent in each altitude band as indicated by the data in Reference 9.

The distributions of speeds for climb, cruise and descent as given in Reference 9 are shown in Figure 6-10. The breakdown of these distributions by altitude band is not available.

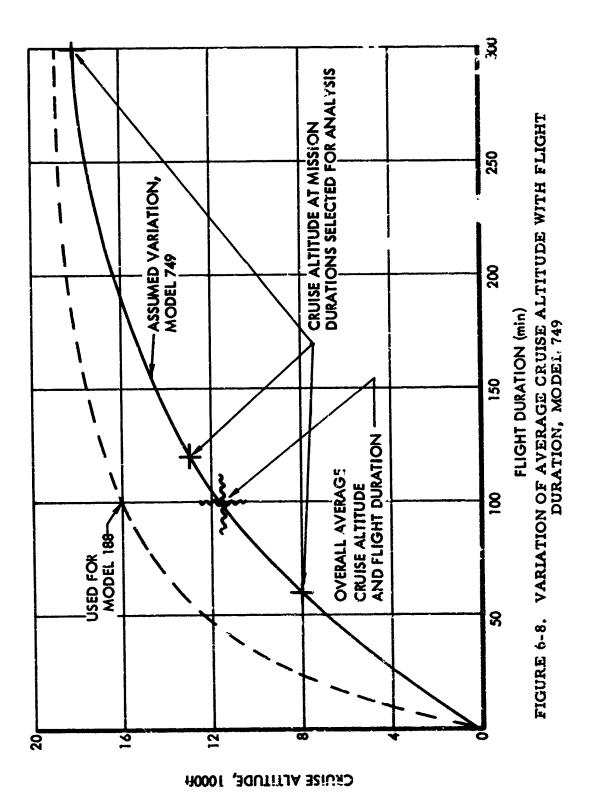
The representative climb speed is taken as a constant 157 knots equivalent airspeed for all three missions.

Average cruise speeds as a function of altitude are estimated by means of Figure 6-11. The average cruise speed obtained from Fig. 6-10 and the average cruise altitude shown in Fig. 6-8 are plotted as a single point in Fig. 6-11. The average cruise speeds at the three altitudes required in the mission analysis are then estimated using the curve of speed at meximum cruise power as a guide. The resulting average cruise speeds for the three mission profiles are:

Cruise Altitude	Cruise Speed
8,000 ft.	210 knots EAS
13,000 ft.	205 knots EAS
18,000 ft.	190 knots EAS

The descent speed is taken as a constant 220 knots for each of the three missions, based upon maintaining a reasonable spread - approximately 15 knots - between the actual speed and  $V_{NO}$ . The distribution shown in Figure 6-10 indicates typical descent speeds to be somewhat higher. However, this distribution is based on data obtained at a time when normal practice was to descend, in smooth air, at close to  $V_{NE}$ . As a result largely of the same data shown in Figure 6-10 (obtained in the period 1951 - 1953), the descent-speed policy was altered to prohibit descent in excess of  $V_{NO}$  shortly after the data were obtained.

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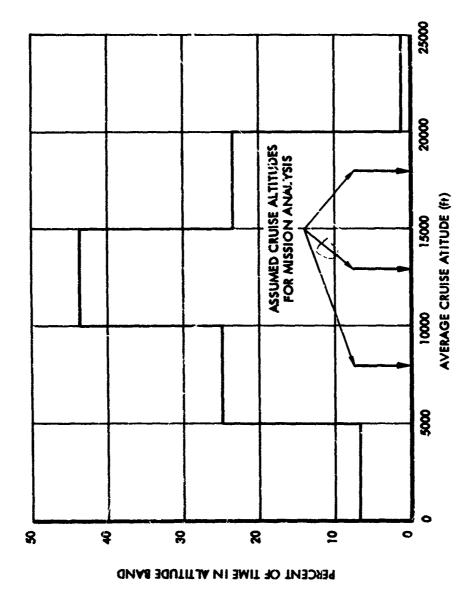


FIGURE 6-9. PERCENT OF CRUISE TIME SPENT IN VARIOUS ALTITUDE BANDS, MODEL 749

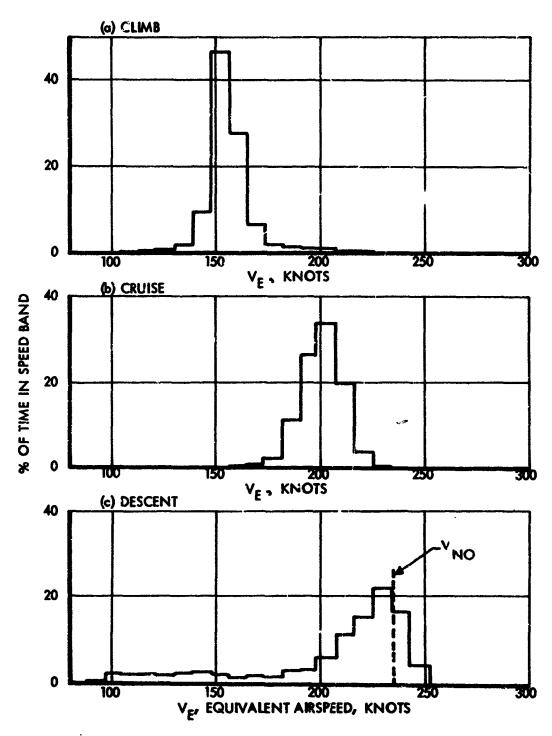
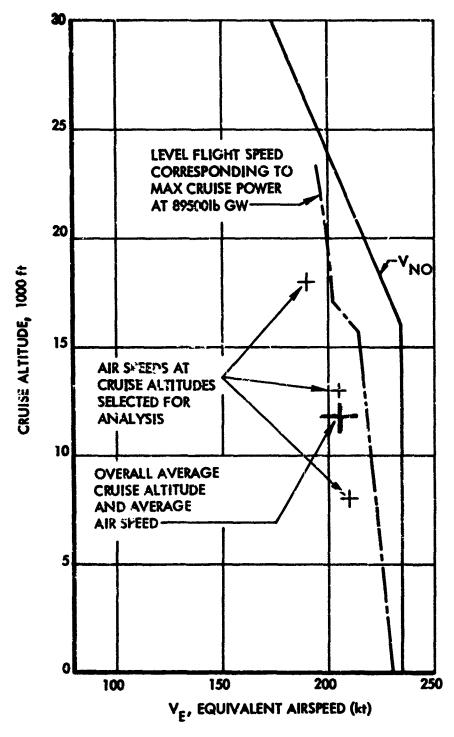


FIGURE 6-10. DISTRIBUTIONS OF AIRSPEED, MODEL 749



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FIGURE 6-11. VARIATIONS OF AVERAGE CRUISE SPEED WITH ALTITUDE, MODEL 749

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The three representative mission profiles are shown in Figure 6-12a through 6-12d.

The airplane weights shown in Figure 6-12 were next determined.

Operating weight empty for the 749 is taken as 68640 lbs. Calculations based upon as-delivered weights indicated an average value of approximately 63,000 lbs. with a variation of several thousand pounds in this weight due to different interior configurations. However, weight growth due to configuration changes, conversions and structural modifications has taken place on the 749 fleet and a detailed weight summary is not readily available. A fleet of 749's presently operating report an average operating weight empty of 68640 lbs. contrasted to an estimated as-delivered operating weight of 63200 lb. This is taken as a representative increase, and, because the original weight of this fleet was close to the overall average, the operating weight of 68640 lbs. is used as representative.

An average 749 payload of 9500 lbs. is selected based upon information obtained from the same major 749 operator. This estimate corresponds to a load factor of 70% applying to a numinal maximum payload of 13590 lbs. It corresponds to a passenger load factor of 77%, based upon a passenger capacity of 62 and a weight per passenger of 200 lb. including baggage, with no cargo carried. It corresponds to 53% of maximum payload as controlled by the placard zero fuel weight of 86464 lt. in combination with the operating weight empty of 68640 lb. The zero-fuel weight corresponding to the 9500 lb. payload is 78140 lb.

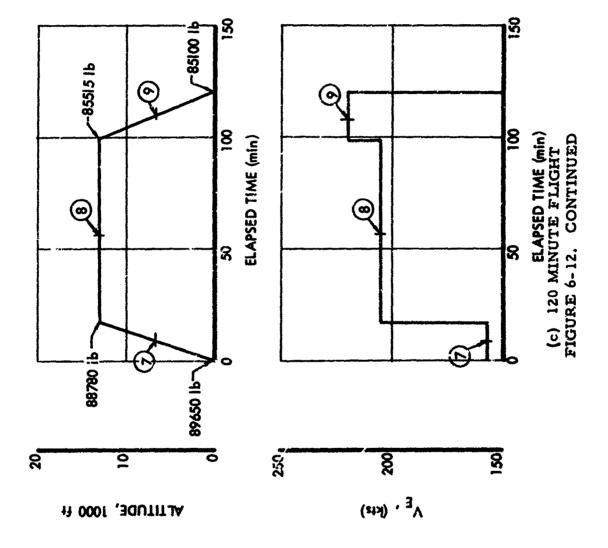
Representative reserve fuel quantities for the assumed operating weight empty and payload range from the FAA required minimum of 4200 lbs. to a maximum of 11360 lbs. The latter figure is the maximum that can be carried at the assumed operating weight empty and payload without exceeding the design landing weight of 89,500 lb. It is estimated that the 749 is operated such that approximately 25% of the missions are fueled through and thus require high landing fuels. As a result, it is assumed that 15% of all flights will carry 11,000 lb. of reserve fuel, reflecting the more extreme fuel-through situations, while the remaining 85% of flights will carry 7000 lb. of reserve fuel, reflecting non-fuel-through operations together with the remainder of the fuel-through flights. The fuel-through operation is limited to the 60 minute flights.

The landing weights corresponding to the above assumptions are as follows:

Operating Wt. Empty	68600	68600
Average Payload	9500	9500
Reserve Fuel	7000	11000
Landing Wt.	85100	89100

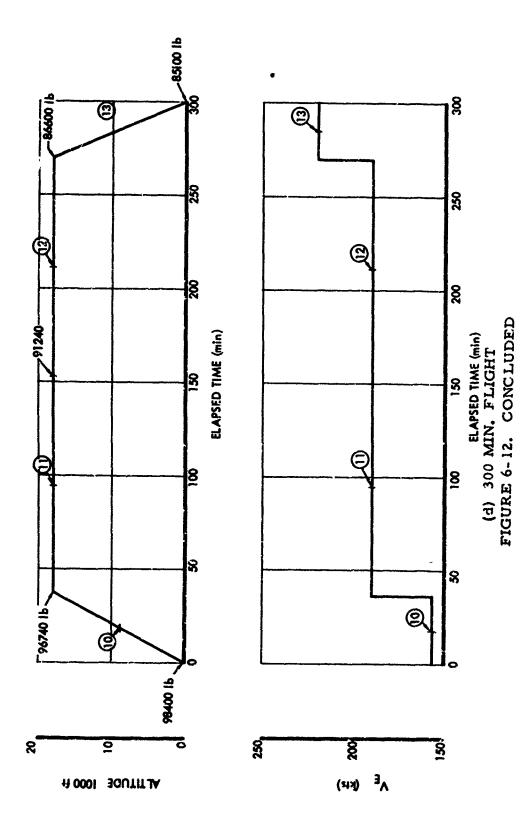
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The airplane weights for various points in the representative missions are found by working backwards from the landing weights using fuel consumption and performance data available in unpublished form.

The mission profiles thus established and shown in Figure 6-12 are broken down into segments for analysis as indicated by circled numbers in Figures 6-12a to 6-12d. These segments are tabulated in detail in Table 6-3.

The mission segments shown in Table 6-3 are then combined for analysis in Table 6-4. Only very nearly identical segments are combined, except in the case of the climb segments, which previous analyses had indicated contribute negligibly to the gust load exposure. Airplane center of gravity positions shown in Table 6-4 are based on a center of gravity midway between forward and aft limits without fuel, in accordance with the best available estimate.

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TABLE 6-3. MISSION PROFILE DATA, MODEL 749

Mission Description	Percent of Total Flights	Segment No.	Climb, Enroute Or Descent	Time In Segment Per Filght Minutes	Ve Average Speed Knots	h Average Altitude Ft	Average OW Lb	Percent Or Total Airplane Time In Segment
60 Min	38	ศิลต	ព្ធជ	10 37 13	157 210 220	000 <del>1</del> 000 <del>1</del> 000 <del>1</del>	86870 85994 85225	1,83 18,05 6,34
60 Min Fuel through	25	3 WO	υĦΑ	33. 13.	157 210 220	0004 00004 7	90850 89975 89225	1.83 5.33 1.98
120 Min	28	F-80 60	CMA	17.5 80.8 21.7	157 205 220	6500 13000 6500	89215 87150 85308	22.98 6.18
300 Min	6	ខ្លះជូន	ОММО	37.0 116.5 116.4 30.1	157 190 190 220	9000 18000 18000 9000	97570 93990 88470 85402	3.88 10.66 10.65 2.75

TABLE 6-4. SUMMARY OF LUMPED FLIGHT SEGMENTS FOR MISSION ANALYSIS, MODEL 749

	Fercent Of Total Airplane Time In Segment	15.07	18.05	6.34	5.33	1.98	22.99	6.18	10,66	10.65	2,75
	C.G.	25.4	54.5	24.8	25.4	25.3	25.0	24.8	25.7	25.2	24 <b>.</b> 8
	W Average GW Lb	90528	₩ ₩ ₩	85290	89975	89225	871.50	85290	93990	88470	85290
	h Average Altitude Ft	0009	8000	0001	8000	0001	13000	6500	18000	1,8000	0006
cases.	Ve Average Speed Knots	157	210	220	210	220	205	220	190	190	820
8100 lb for all	Climb, Enroute Or Descent	ຍ	ы	ធ	ÞQ.	A	E	A	Ħ	æ	Ω
Note: Zero fuel weight = 78100 lb for all cases	Segment No. In Table 6-3	1, 4, 7, 10	Q	က	ľ	v	ω	δ	7	ដ	13
Note: Zero	Segment Case No.	101	102	103	101	105	106	101	108	109	011

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# 7 SELECTION OF DESIGN ENVELOPE POINTS FOR ANALYSIS OF REFERENCE AIRPLANES

## 7.1 Model 188

The design speed-altitude chart for the Model 188 is shown in Figure 7-1, and the weight-c.g. envelope in Figure 7-2.

In Figure 7-1, the V<sub>C</sub> and V<sub>D</sub> lines reflect the values used for structural design. The V<sub>NE</sub> speed, while not used directly in structural design, is shown for information. The V<sub>B</sub> speed of 180 knots is to a certain extent arbitrary. In existing criteria, V<sub>B</sub> is defined as the speed at which a 65 fps gust line on the V-n diagram intersects the stall line. The actual speed depends upon gross weight, and is also subject to some variation depending upon the source of data used in determining the stall speeds. For application in a power spectral criterion, the definition would, of course, have to be recast into power-spectral form, and some difficulty might be encountered in arriving at a simple yet rational definition. The 180 knots V<sub>B</sub> speed used in the present analysis is the value indicated by existing criteria at a gross weight of about 95000 lb.

The c.g. limits shown in Figure 7-2 are based upon operating placards and are slightly more restrictive than the limits actually used in the structural design of the airplane.

In addition to the envelopes shown, there are, of course, further restrictions as to location of fuel and payload, which are taken into account in the analyses conducted herein. In particular, it is noted that the minimum fuel for structural design is 3145 lb.

The design envelope cases for which vertical gust dynamic analysis was conducted for the Model 188 are listed in Table 7-1.

In selecting these cases, an effort was made to reduce to a minimum the number of cases for which a full dynamic analysis was required. Manifestly, it was necessary to include enough cases to assure that the critical combinations of airplane speed, altitude, weight, and weight distribution were covered. Moreover, the selection of critical conditions was complicated by the variation of  $\sigma_{\rm W}$   $\eta_{\rm d}$ , or design y/A, with altitude, as shown in Figure 5-8. The number of potentially critical cases is, therefore, very large. In order to reduce the number requiring detailed dynamic analysis, the effect of altitude was

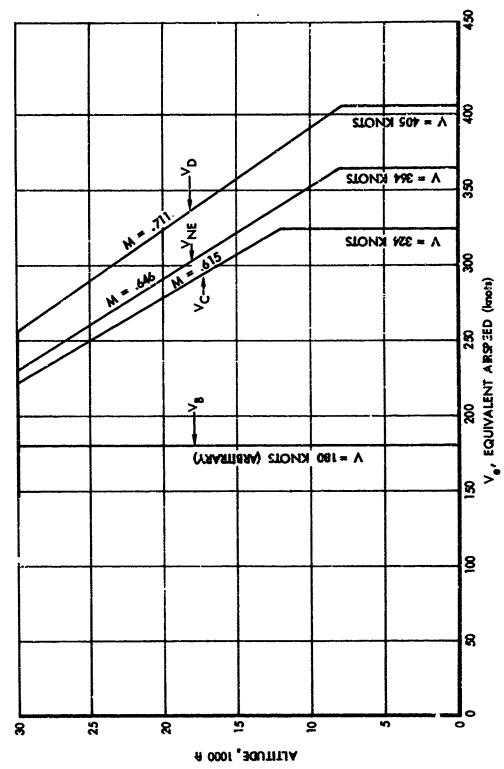


FIGURE 7-1. DESIGN SPEED ALTITUDE CHART, MODEL 188

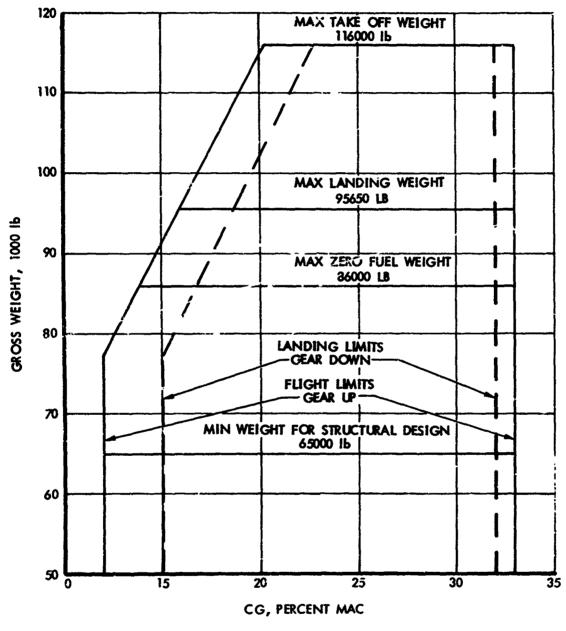


FIGURE 7-2. DESIGN WEIGHT - CG ENVELOPE, MODEL 188

TABLE 7-1. DESIGN ENVELOPE CASES FOR VERTICAL GUST ANALYSIS, MODEL 188

Case	Gross Weight Lb	Zero Fuel Weight Lb	Fuel Weight Lb	c. g. \$ M/C	Altitude Ft	V <sub>B</sub> , V <sub>C</sub> Or V <sub>D</sub>	V e Knots
401	65000	61855	3145	12.0	12000	ν <sub>c</sub>	324
402	6 <b>5</b> 000	61855	3145	33.0	12000	٧	324
403	97345	61855	<b>35</b> 490	16.2	12000	νc	324
404	97345	61855	35490	33.0	12000	V <sub>C</sub>	324
405	116000	80 <b>5</b> 10	<b>35</b> 490	20.2	12000	ν <sub>c</sub>	324
i406	116000	80510	<b>35</b> 490	33.0	12000	v <sub>C</sub>	324
407	89145	86000	3145	14.5	12000	٧ <sub>C</sub>	324
408	89145	86000	3145	33.0	12000	vc	324
409	95620	86000	9620	15.8	12000	ν <sub>C</sub>	324
410	95620	86000	9620	33.0	12000	v <sub>c</sub>	324
411	101860	86000	15860	17.2	15000	$^{\nu}_{\rm c}$	324
412	101860	86ი <b>ი</b> ი	15360	33.0	12000	ν <sub>c</sub>	324
413	107000	86000	21000	18.3	12000	ν <sub>c</sub>	324
414	107000	86 <b>0</b> 00	21000	33.0	12000	v <sub>c</sub>	324
415	113000	86000	27000	19.6	12000	v <sub>c</sub>	<b>3</b> 24
416	113000	86000	27000	33.0	12000	Ϋ́c	324
417	116000	86000	30000	20.2	12000	ν <sub>C</sub>	324
418	116000	86000	30000	33.0	12000	v <sub>C</sub>	324
419	39145	86000	3145	145	20000	v <sub>c</sub>	275
420	89145	86000	3145	1 <sup>1</sup> 5	16000	v <sub>c</sub>	299
75J	89145	86000	3145	14.5	7000	v <sub>c</sub>	324
422	89145	86600	3145	14.5	0	ν <sub>c</sub>	324
423	65000	61855	3145	12.0	7000	V <sub>D</sub>	405
1424	65000	61855	3145	33.0	7000	v <sub>D</sub>	405
425*	89145	86000	3145	14.5	7000	v <sub>D</sub>	405
126	89145	86000	3145	33.0	7000	v <sub>D</sub>	405
427	89145	86100	3145	14.5	7:000	v <sub>B</sub>	180
428	89145	86 <b>00</b> 0	3145	14.5	12000	v <sub>B</sub>	180
9*	116000	86000	30000	20,2	12 <b>00</b> 0	v <sub>B</sub>	180
430	116000	86 <b>000</b>	30000	20.2	12000		550
431	116000	86000	30000	20.2	2 <b>7000</b>		220

<sup>\*</sup> Cases found to be critical

investigated first by examining center of gravity accelerations obtained on a much simpler basis. For this purpose, the curves of Figure 5-2 were used, which are based on the assumption of a rigid airplane free to plunge only. The c.g. accelerations thus obtained should indicate, to a good first-order approximation, the effect of altitude on wing loads as these would be obtained by the more complex dynamic analysis.

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A values thus obtained are shown as a function of altitude, for three gross weights, in Figure 7-3. These A values are then multiplied by values of y/A from the various curves of Figure 5-8, to yield Figures 7-4 and 7-5. These curves represent equal probability values of c.g. load factor, based on the simplified analysis. For any particular gross weight and weight distribution the curves can also be interpreted, to a reasonable approximation, as equal-probability curves for structural loads. Actually, there is a tendency for the load per g to increase with altitude due to reduced aerodynamic damping in the elastic modes; as a result, the true equal-probability curves for most structural loads would tend to shift slightly to the right with increasing altitude.

Inasmuch as the limit design value of N(y)/N<sub>O</sub> was expected to fall in the range  $10^{-6}$  to  $10^{-8}$ , it appeared quite certain that the critical altitude would be either 7000 ft. or 12000 ft., with 12,000 ft. perhaps the more likely. The 12,000 ft. altitude, it may be noted, corresponds to the knuckle in the design speed-altitude V<sub>C</sub> line, and the 7000 ft. altitude to the knuckle in the curve of y/A vs altitude.

Accordingly, the first 18 cases in Table 7-1 were taken at an altitude of 12,000 ft. A wide range of gross weights, payloads (as defined by zero-fuel weight), and fuel weights was covered; and for each of these weight combinations, a case was included at both forward and aft c.g. limits

Using results obtained for the 2 18 cases, preliminary limit-strength values of y/A were then determined, based upon four load quantities only - namely shear and bending moment at WS 83 and WS 275. Phasings, including the probable effect of torsion, were estimated from the results of earlier analyses (Reference 20) and limit strengths were based upon available design load envelopes. The critical case was indicated to be No. 407. As a result, cases 419 to 422 were then added, to assure that the critical altitude had been selected. (More thorough analysis, discussed in Appendix E, indicated later that Case 417 was actually more critical than 407; however, the pattern of cases actually selected was found to be sufficient to draw the necessary conclusions.)

Four cases were next selected for analysis at design dive speed. These include two weight cases - minimum fuel weight with maximum zero-fuel weight, and minimum flying weight. The former had been found most critical for V<sub>C</sub> conditions, but the latter was included to provide for

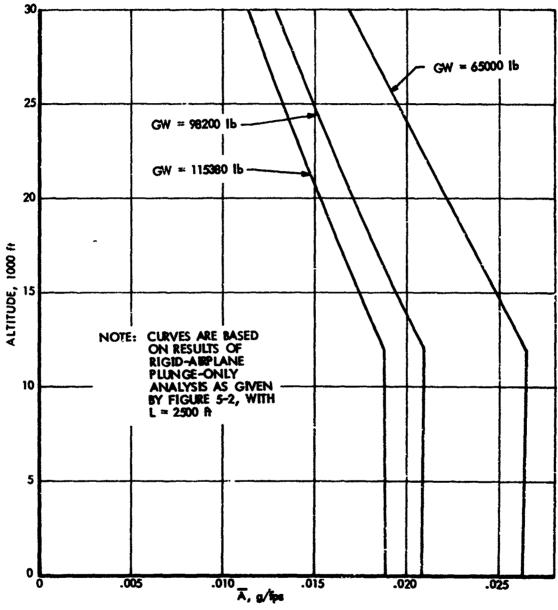


FIGURE 7-3. EFFECT OF ALTITUDE ON THE FOR CG ACCELERATION, MODEL 188

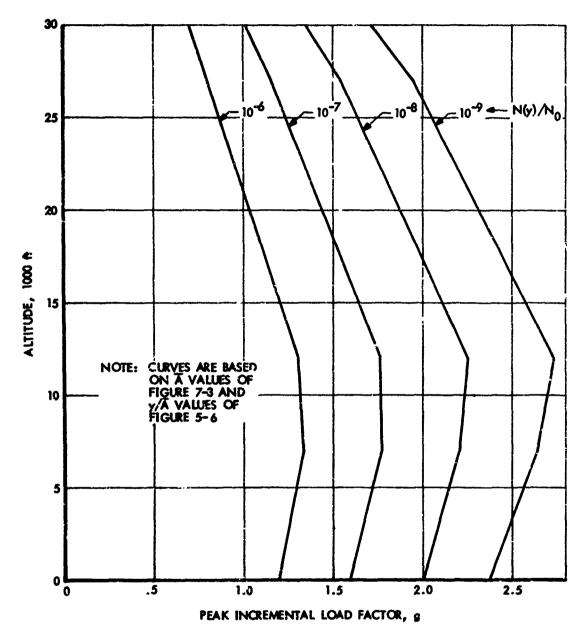


FIGURE 7-4. EFFECT OF ALTITUDE ON DESIGN LEVEL OF C.G. ACCELERATION, MODEL 188 - VARIOUS  $N(y)/N_O$  LEVELS, GROSS WEIGHT = 98200 LB

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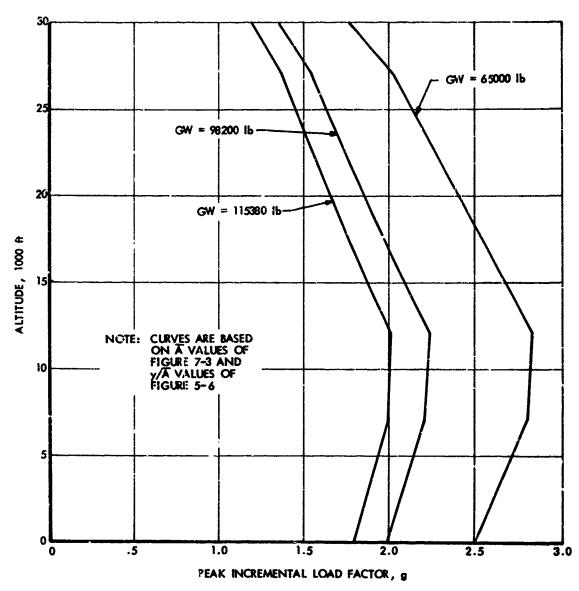


FIGURE 7-5. EFFECT OF ALTITUDE ON DESIGN LEVEL OF C.G. ACCELERATION, MODEL 188 - VARIOUS GROSS WEIGHTS,  $N(y)/N_0 = 10^{-8}$ 

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the possibility that a negative gust in combination with level flight loads modified by high speed aeroelastic effects could be more critical in down bending on the wing. The selection was based primarily on results of the earlier design analysis contained in Reference 20. The choice of a critical altitude was not a problem. The knuckle in the speed-altitude envelope shifts down to 8000 ft. at dive speed; this is so close to the 7000 ft. altitude at which the knuckle in the  $\sigma$   $\eta$  vs altitude curve occurs that the loads are sensibly the same at both altitudes.

Inasmuch as reduction of speed from VC to VB was expected to have little effect on the critical weight condition, the VB case was taken for the same weight configuration and c.g. location expected to be critical at VC. The altitude was reduced from 12000 ft. to 7000 ft., however, as a result of preliminary evaluation of the results obtained in cases 419-422. Following detailed study of loads resulting from cases 401-427 (described in Appendix E), it became evident that the critical VB condition would occur at a gross weight of 116,000 lbs. rather than 89,145 lbs., and that the critical altitude, too, might be higher than selected. Also, because of the somewhat arbitrary selection of a VB speed, it appeared desirable to determine the effect of a range of potential VB speeds. Accordingly, cases 428-431 were added.

The design envelope points for which lateral gust dynamic analysis was made are shown in Table 7-2. The conditions listed cover a range of weights from minimum flying weight to maximum take-off gross weight. The center of gravity travel investigated included both forward and aft design limits, and both VC and VD variations with altitude are represented. No VB cases are included. Preliminary runs, in which fewer load outputs were available, indicated the critical VB loads to be appreciably lower than 50/66 of the VC loads and consequently not critical.

The cases in Tables 7-1 and 7-2 later found to be critical (Appendix E) are indicated by asterisks.

### 7.2 Model 749

The design speed-altitude chart for the Model 749 is shown in Figure 7-6, and the weight-c.g. envelope in Figure 7-7.

In Figure 7-6, the  $V_C$  and  $V_D$  constant equivalent airspeed lines at low altitude are the values used for structural design. The knuckle at 16,000 ft. in the  $V_C$  line is in accordance with the flight placard. A constant Mach line above this point is assumed for the purpose of the present study, although the actual flight placard is a straight line approximation to this. The knuckle in the  $V_D$  line is considered to occur at the same altitude as the knuckle in the  $V_{NE}$  line, which is shown at 13,000 ft. in accordance with the flight placard.  $V_D$  is assumed to follow a constant Mach line above 13,000 ft. Although a constant Mach line is also shown for  $V_{NE}$ , the actual flight placard is a straight line approximation to this line.

TABLE 7-2. DESIGN ENVELOPE CASES FOR LATERAL GUST ANALYSIS, MODEL 188

Case	Gross Weight Ib	Zero Fuel Weight Ib	Fuel Weight Lb	C.G. MAC	Altitude Ft	V <sub>B</sub> , V <sub>C</sub> or V <sub>D</sub>	V e Knots
501	116000	86000	30000	35.0	6000	v <sub>c</sub>	324
602*	11.6000	86000	30000	35.0	7000	v <sub>c</sub>	324
6 <b>c</b> 3	116000	86000	30000	35.0	12000	v <sub>c</sub>	324
604	116000	86000	30000	35.0	20000	v <sub>c</sub>	276
605	116000	86 <b>000</b>	30000	35.0	30000	v <sub>c</sub>	221
6 <b>0</b> 6	116000	85 <b>000</b>	30000	35.0	4000	v <sub>D</sub>	405
607	116000	86000	30000	35.0	7000	v <sub>D</sub>	405
é28*	116000	66 <b>000</b>	30000	35.0	8000	v <sub>D</sub>	405
609	116000	86000	30000	35.0	20000	ν <sub>D</sub>	<b>3</b> 28
610	116000	36000	30000	35.0	30000	η <sup>D</sup>	256
612	86590	86000	500	35•0	7000	άC	324
612	86500	56 <b>00</b> 0	500	35.0	7000	v <sub>D</sub>	405
613	6500C	61855	3145	35.0	7000	v <sub>c</sub>	321;
614	65000	61855	3145	35.0	7000	v <sub>D</sub>	405
615	86500	86000	500	35.0	12000	v <sub>c</sub>	324
615	116000	86000	30000	20.1	20000	AC	276
617*	116000	86000	30000	20.1	6000	٧c	324
618	116000	86000	30000	20.1	30000	νc	551
619	116000	86000	30000	20.1	20000	v <sub>C</sub>	328
620	11.6000	860 <b>0</b> 0	30000	20.1	30000	v <sub>D</sub>	256
621*	116000	86000	30000	20.1	8000	Λ <sup>D</sup>	405

<sup>\*</sup> Cases found to be critical

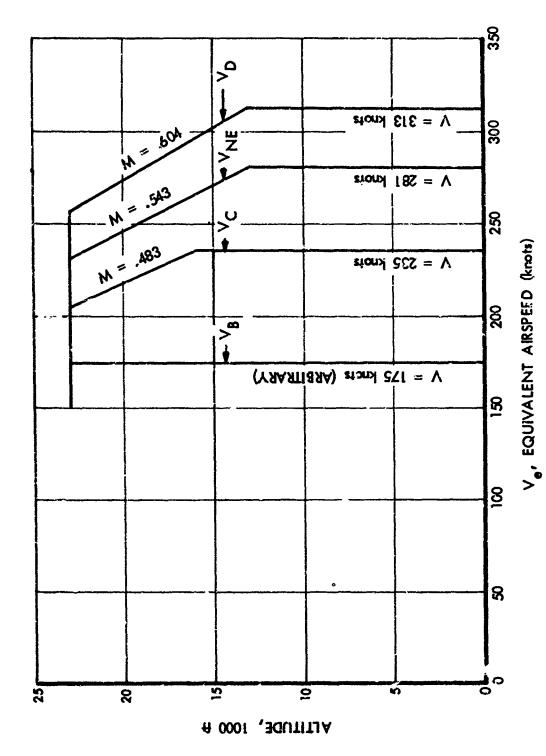


FIGURE 7-6. DESIGN SPEED ALTITUDE CHART, MODEL 749

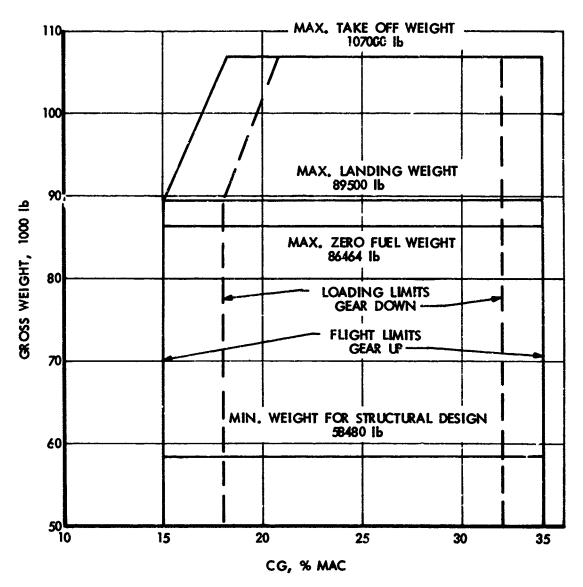


FIGURE 7-7. DESIGN WEIGHT'- CG ENVELOPE, MODEL 749

The maximum altitude shown, while not used in the original structural design of the sirplane, is a reasonable value based upon performance limitations.

As in the case of the Model 188, the  $\rm V_B$  speed is somewhat arbitrary. The 175 knot value used herein is in agreement with present criteria at a gross weight of about 99,000 lb.

The c.g. limits shown in Figure 7-7 are based upon operating placards. Throughout this study, the aft c.g. limit in flight was inadvertently taken equal to the loading limit, at 32% MAC; inasmuch as the results of this study have generally shown the c.g. position to have a very small effect on loads - generally less than 5%, and for the vertical gust loads only 1 or 2%, for the full range between forward and aft limits - no attempt has been made to adjust the results for this discrepancy.

The minimum weight for structural resign, shown so 58480 lb., is an early design number and is obviously low for the sirplanes as currently operated, with an average operating weight empty of 68640 lb. Cases at minimum weight, however, are found not to be critical.

The design envelope cases for which vertical gust dynamic analysis was conducted for the Model 749 are listed in Table 7-3.

The approximate effect of altitude on loads was determined by means of a simplified analysis, as for the Electra, with the results shown in Figures 7-8, 7-9, and 7-10. It is clear that critical loads will occur at either 7000 ft. or 16000 ft. altitude, with the 16,000 ft. altitude slightly more likely.

Consequently, the first 14 cases in Table 7-3 represent a variety of weight conditions at an altitude of 16,000 ft.

Based on preliminary analysis of the results for these cases, it appeared that Case 308 was critical. Accordingly, a range of altitudes was next investigated for this weight condition; this investigation comprises Cases 315-318.

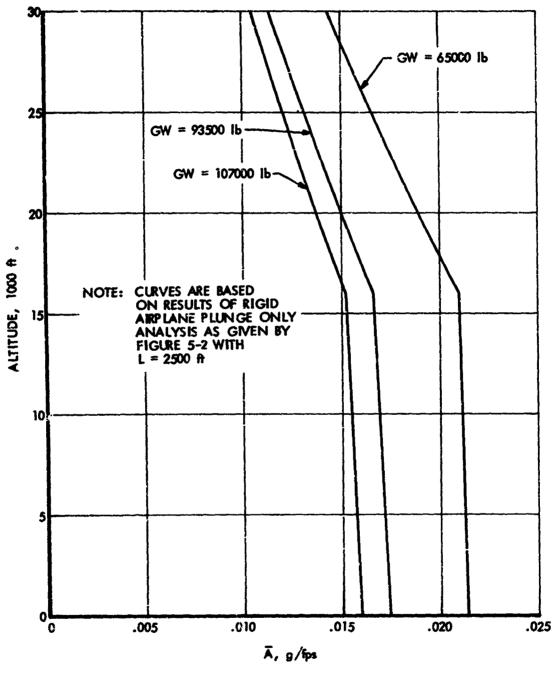
Selection of four  $\mathbf{V}_{D}$  cases and a  $\mathbf{V}_{B}$  case was made in the same way as for the Electra.

The design envelope points for which lateral gust dynamic analysis was made for the Model 749 are listed in Table 7-4. Results of the Model 188 analysis were used to eliminate conditions that would clearly not be critical. Critical forebody loads were found to occur in the weight condition having maximum forebody weight combined with minimum fuel and minimum aftbody weight. This result is reasonable; forebody loads are primarily inertial, and maximum values should occur with high forebody weights in combination with the greater accelerations associated with the highest natural frequencies. On the other hand, the aftbody is

TABLE 7-3. DESIGN ENVELOPE CASES FOR VERTICAL GUST ANALYSIS, MODEL 749

Case	Gross Weight Lb	Zero Fuel Weight Lb	Fuel Weight Lb	C. G. % MAC	Altitude Ft	v <sub>B</sub> ,v <sub>C</sub> Or v <sub>D</sub>	V e Knots
301	58480	55980	2500	15.0	16000	v <sub>c</sub>	235
302	58480	55980	2500	32.0	16000	ν <sub>c</sub>	235
303	90900	5598c	34920	15.2	16000	νc	235
304	90900	55980	34920	32.0	16000	ν <sub>c</sub>	235
305	107000	72080	34920	18.5	16000	v <sub>C</sub>	235
306	107000	72080	34920	32.0	16000	v <sub>C</sub>	235
307	88964	86464	2500	, 15 <b>.</b> 0	16000	v <sub>C</sub>	235
308	88964	86464	2500	32.0	16000	$v_{c}$	235
309	95000	86464	8536	16.0	16000	v <sub>c</sub>	235
310	95000	86464	8536	32.0	16000	v <sub>c</sub>	235
311	101000	86464	14536	17.1	16000	v <sub>C</sub>	235
312	101000	86464	14536	32.0	16000	v <sub>c</sub>	235
313	107000	86464	20536	18.5	16000	v <sub>c</sub>	235
314	107000	86464	20536	32.0	16000	v <sub>c</sub>	235
315	88964	86464	2500	32.0	20000	v <sub>C</sub>	218
316	88964	86464	2500	32.0	12000	v <sub>c</sub>	235
317*	88964	86464	2500	32.0	7000	v <sub>C</sub>	235
318	88964	86464	2500	32.0	16000	v <sub>c</sub> .	235
319	58480	55980	2500	15.0	7000	$v_{_{ m D}}$	313
320	58480	55980	2500	32.0	7000	$v_{\scriptscriptstyle D}$	313
321	88964	86464	2500	15.0	7000	v <sub>D</sub>	313
322*	88964	86464	2500	<b>3</b> 2.0	7000	$v_{\scriptscriptstyle D}$	313
323*	88964	86464	2500	32.0	7000	v <sub>B</sub>	175

<sup>\*</sup> Cases found to be critical



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FIGURE 7-8. EFFECT OF ALTITUDE ON \$\overline{A}\$ FOR C.G. ACCELERATION, MODEL 749

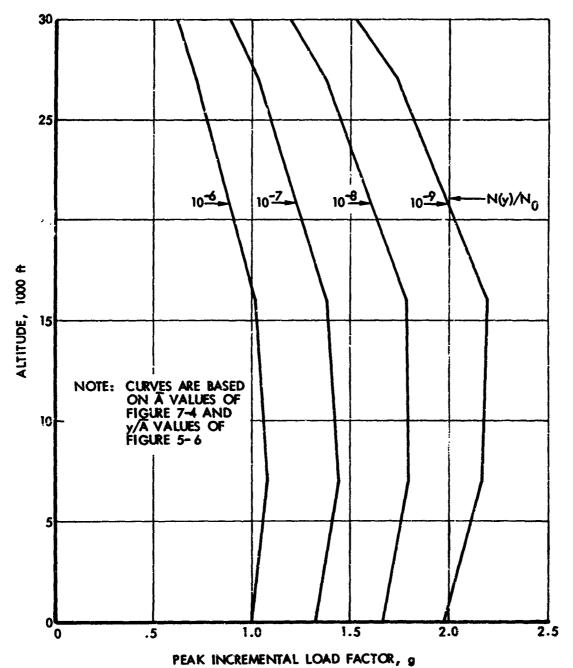
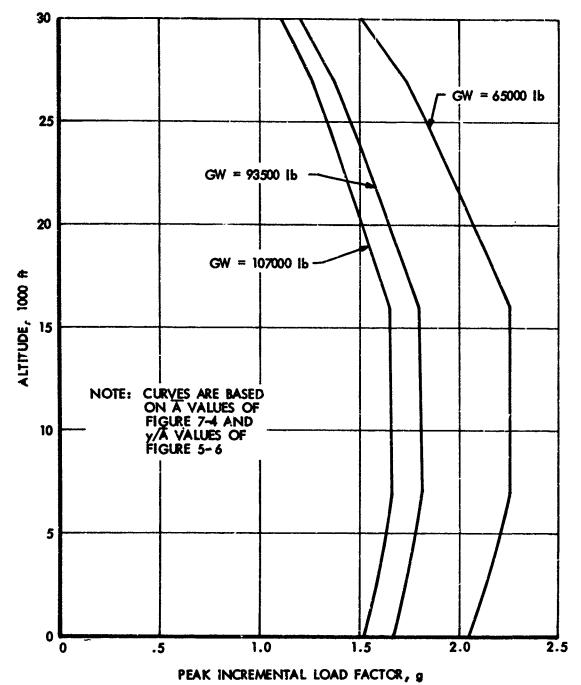


FIGURE 7-9. EFFECT OF ALTITUDE ON DESIGN LEVEL OF CG ACCELERATION, MODEL 749 - VARIOUS N(y)/N<sub>o</sub> LEVELS, GROSS WEIGHT = 93500 LB



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FIGURE 7-10. EFFECT OF ALTITUDE ON DESIGN LEVEL OF CG ACCELERATION, MODEL 749 - VARIOUS GROSS WEIGHTS,  $N(y)/N_o = 10^{-8}$ 

TABLE 7-4. DESIGN ENVELOPE CASES FOR LATERAL GUST ANALYSIS, MODEL 749

Case	Gross Weight Ib	Zero Fuel Weight Lb	Fuel Weight Lb	C.G. MAC	Altitude Ft	v <sub>B</sub> , v <sub>C</sub> or v <sub>D</sub>	V <sub>e</sub> Knots
501*	107000	86464	20536	32.0	<sub>7</sub> +000	v <sub>C</sub>	235
502*	107000	86464	20536	32.0	J1000	v <sub>D</sub>	313
503*	701000	86464	2 <b>053</b> 6	32.0	10000	v <sub>c</sub>	235
504*	107000	86464	2 <b>053</b> 6	32.0	10000	v <sub>D</sub>	313
505	107000	86464	20536	32.0	13000	v <sub>D</sub>	313
506	197000	86464	20536	32.0	16000	v <sub>c</sub>	<sup>2</sup> 35
507	107000	86464	2 <b>053</b> 6	32.0	16000	v <sub>D</sub>	59,4
<b>50</b> 8	107000	86464	20536	32.0	20000	v <sub>c</sub>	217
509	107000	861161	20536	32.0	20000	v <sub>D</sub>	271
510	107000	85464	20536	32.0	25000	v <sub>c</sub>	195
511	107000	86464	20536	32.0	30000	v <sub>C</sub>	174
512	107000	86464	20536	32.0	30000	v <sub>D</sub>	217

<sup>\*</sup> Cases found to be critical

loaded primarily by the air load on the vertical tail and is, therefore, critical for the high gross weight cases. However, the maximum tail and aftbody loads are much more critical than the maximum forebody loads. Accordingly, in the Model 749 analysis, only the high gross weight, aft c.g. cases were included. Also, inasmuch as  $V_{\rm B}$  conditions were clearly not critical for the Model 188, these also were excluded from the Model 749 analysis.

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The combinations of speed and altitude chosen represent both  $\rm V_C$  and  $\rm V_D$  speeds over a range of altitudes. It should be noted that, for the purposes of this study, several points outside the design operating envelops were obtained - namely, the 25,000 ft. and 30,000 ft. altitude points. These cases are listed in Table 7-4, but are not considered in establishing limit and ultimate strength values of N(y) and of  $\sigma_{\rm w}$   $\eta_{\rm d}$ .

The cases in Tables 7-3 and 7-4 later found to be critical (Appendix E) are indicated by asterisks.

The second secon

#### 8 MATHEMATICAL MODELS OF REFERENCE AIRPLANES

### 8.1 Vertical Gust, Models 188 and 749

8.1.1 Equations of Motion. In the mathematical model employed to determine dynamic response of the Model 188 and Model 749 airplanes to the vertical component of turbulence, the airplane is represented by means of a rigid fuselage and horizontal tail, a wing represented elastically by an elastic axis straight and normal to the plane of symmetry, and two nacelles per side having flexibility relative to the wing.

Airplane motions are defined in terms of ten generalized coordinates - fuselage plunge and pitch, two wing bending modes, two wing torsion modes, and plunge and pitch of each nacelle mass relative to the wing. The first wing bending and torsion modes are uncoupled cantilever modes obtained by assuming a reasonable deflection shape and iterating once. The second bending and torsion modes are obtained similarly; however, with only the one iteration, these depart considerably more from the true natural-mode shapes. Provision is also made for specifying both mode shape and frequency for any or all of the four modes, with no fur her iteration to be made.

Wing masses and aerodynamic forces are lumped at ten spanwise wing stations. Spanwise flow effects are not accounted for, although any desired spanwise variation of  $C_{\mathbf{L}\alpha}$  can be used; in the present study, panel  $C_{\mathbf{L}\alpha}$  values were chosen to match static spanwise distributions produced by a constant increment in angle of attack. Definition of the mass of each panel includes the chordwise location of the center of gravity and the pitching moment of inertia.

Each nacelle (in addition to that portion considered rigidly attached to the wing) is represented as a dumbbell mass with translational and rotational inertia. Aerodynamic forces as felt by the propeller as well as the nacelle proper are applied.

The fuselage is assumed to develop aerodynamic lift and moment; lift developed on the forward portion of the forebody is separated out in order to account for the time lag between nose and wing penetration of the gust.

Tail aerodynamic forces include the effect of wing downwash, and the time lags of the gust and downwash proceeding from the wing to the tail are accounted for. Provision is included for aerodynamic force increments on the tail due to elevator float or elevator motions introduced by a stability augmentation system. The elevator float motion is

introduced actually as an eleventh generalized coordinate, with elevator mass (including moment of inertia about the hinge line) as well as aero-dynamic forces included. A simple static treatment could have been used, and would have given essentially the same results; this would have eliminated the need to include appropriate external damping in the mode.

Unsteady lift growth functions for gust encounter (Kussner function) and for airplane motions (Wagner function) are represented separately for wing, tail, fuselage, nose, nacelles, and propellers. The customary exponential approximations appropriate to low Mach number and infinite aspect ratio are used for the various wing panels and for the horizontal tail. For the fuselage, nacelles, and propellers, the same exponential expressions are used, but effective values of chord are estimated such as to provide reasonable approximations to the lift growth on these components.

Loads at various points in the airplane are obtained by superimposing the loads produced by the direct effect of the gust and those resulting from the motions in the ten generalized coordinates. Provision is included for computation of the following load quantities as desired: wing shears, bending moments, and torsions at ten spanwise locations; up to 20 wing shear flows (or other internal loads that can be expressed as linear combinations of the shears, bending moments, and torsions); nacelle c.g. shears and pitching moments (two nacelles); and up to ten fuselage loads (shears or bending moments) including load on the horizontal tail. For the wing, the load read-out locations are defined by the initial lumping of mass and aerodynamic data. Loads are determined for the individual panels and summed as appropriate to yield shears, bending moments, and torsions at the panel boundaries. Since the fuselage is considered rigid, its mass and aerodynamic properties need not be broken into numerous panels for solution of the equations of motion. For the purpose of fuselage load determination, however, the serodynamic forces are distributed to a number of panels. Fuselage shear or bending moment at any given station s then obtained by summing terms consisting of appropriate coefficients multiplying the pitch and plunge accelerations and the airloads on the various panels.

The ten simultaneous differential equations of motion are solved for a forcing function consisting of a steady sinusoidal variation of gust velocity. Frequency-response, or transfer, functions relating both the generalized coordinates and the various airplane load quantities to the input gust velocity are thus evaluated, at up to 100 frequencies. The modulus of each transfer function is then squared and multiplied by the input gust spectrum to obtain an outp t power spectrum. These in turn are integrated with respect to frequency o give  $\overline{A}$  and  $\overline{N}_0$  values. The upper limit of integration was taken as 10.2 cps.

Provision is also included in the equations of motion for elevator motion instead of gust velocity as an input, in order to obtain transfer functions of meneuver loads for establishing the adequacy of the aero-dynamic input data.

All of the calculations indicated above were carried out in a continuous operation on an IBM 7094 automatic digital computer.

A complete presentation of the equations of motion, including their derivation, is contained in Reference 21.

8.1.2 One-g Level Flight Loads. The one-g level flight loads to which the incremental loads due to the turbulence must be added were obtained by appropriate static loads methods.

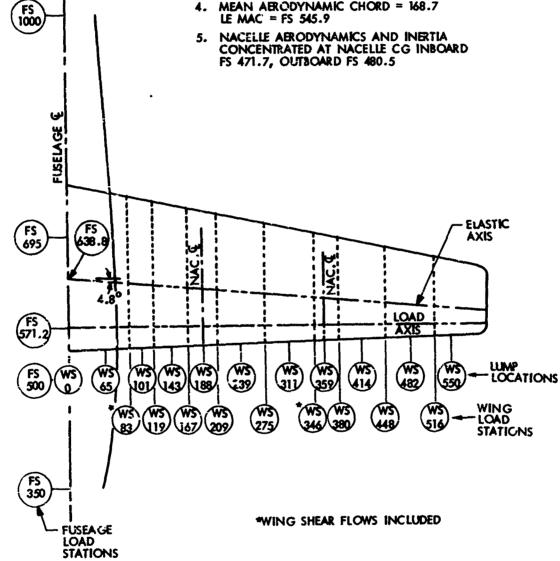
For the Model 186, the distribution of air loads between the wing, fuselage, and horizontal tail was based upon wind tunnel force data. Wing spanwise lift distributions, for the rigid wing, were obtained by means of theory. Wing and nacelle aerodynamic pitching moments were based on integrated use of published NACA documents, wind tunnel pitch data for the Model 188 wing with and without nacelles, calculated propeller normal forces, and flight-measured wing torsions over a wide range of speed and load factor. Air load increments due to the wing twist resulting from the rigid airplane aerodynamic and inertia forces were calculated and included. Arbitrary adjustments to the theoretical airload distributions were made where necessary to bring the calculated loads into close agreement with flight-measured loads.

For the Model 749, as for the Model 188, the distribution of air loads between wing, fuselage, and horizontal tail was based upon wind tunnel force data. Wing airload distributions, too, were determined in a generally similar manner, although flight-measured torsions were not available. Excellent agreement was found between wing bending moments calculated using these distributions and bending moments obtained by flight measurements on a Model 1049B, which had a wing aerodynamically identical to that of the Model 749.

8.1.3 Input Data for Dynamic Analysis. The scheme for lumping of input data and the locations of load read-out points are shown in Figures 8-1 and 8-2 for the Model 188 and Model 749 respectively.

For the wing, load read-out stations are determined by the panel boundaries defined for lumping of input data. Consequently, a fairly detailed coverage of load outputs was inherently provided. Shear, bending moment, and torsion were obtained at each of the wing load

- 1. INERTIA AND PITCHING MOMENT OF INERTIA ARE LUMPED AT CHORDWISE CENTER OF GRAVITY OF EACH PANEL.
- LOCAL AERODYNAMIC CENTER IS ASSUMED TO BE AT LOCAL 24% CHORD.
- LOCAL CHORD = C; = 227 .229y:
- MEAN AERODYNAMIC CHORD = 168.7 LE MAC = FS 545.9



NOSE LIFT AT FS 102.2

TAIL APRODYNAMIC CENTER AT FS 1207.8

FIGURE 8-1. MODEL 188 GEOMETRY AND LOAD STATIONS

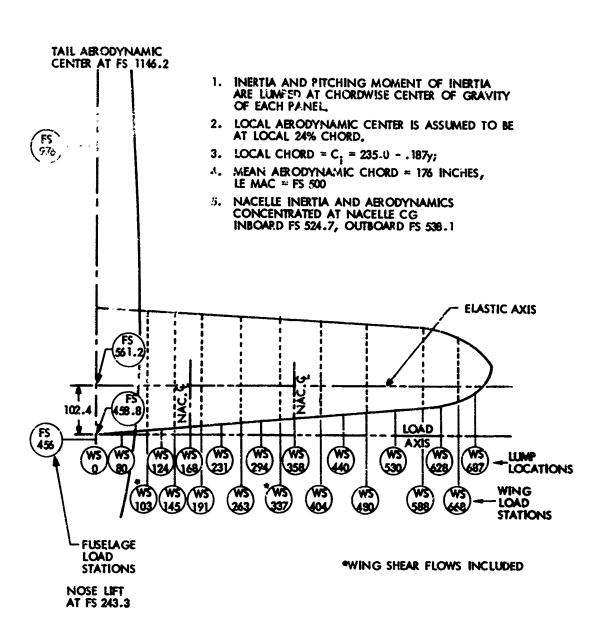


FIGURE 8-2. MODEL 749 GEOMETRY AND LOAD STATIONS

stations indicated in the figures, and front and rear beam shear flows were also obtained at the two wing stations noted.

For the Model 188 fuselage, the selection of load output points was influenced by an examination of margins of safety for the design gust conditions, with the critical locations selected. The Mcdel 749 fuselage was designed to extremely severe criteria and is much less critical than the wing; consequently, only a limited number of load cutputs were obtained. In obtaining fuselage load outputs, overlapping assumptions with respect to the distribution of payload were made, in the design envelope cases, in order to simplify the preparation of input data. For a given total paylcad, the distribution of payload between the forebody and aftbody depends upon whether the sirplane c.g. is to be at the forward or the ait limit. However, in determining the increments of fuselage shear and bending moment due to turbulence, the panel weights by which the local accelerations were multiplied in the dynamic analysis were always taken as the higher of the forward limit and aft limit values, regardless of the actual c.g. position for the case being analyzed. Horizontal tail loads were included as outputs for the particular cases found to be potentially critical as a result of examining the fuselage loed results.

Mass and aerodynamic data used in the dynamic analysis of the two airplanes are generally consistent with the data used for stat. : loads determination, as described in the previous section.

Wing EI and GJ (flexural and torsional stiffnesses) were obtained by calculation; guidance as to appropriate assumptions regarding extent of effective material was obtained from the results of static load-deflection measurements and ground vibration tests. Nacelle stiffnesses were obtained similarly, with particular reliance on load-deflection data for the individual engine mounts and on nacelle mode natural frequencies obtained in ground vibration tests.

Wing structural damping was assumed to be zero, inasmuch as the substantial aerodynamic damping present overshadows the structural damping.

Inclusion of structural damping in the nacelle modes, however, was considered desirable. Comparison of Model 182 calculated with flight measured power-spectral densities indicated that nacelle response above about h cps could not be adequately represented by the ten-degree-of-freedom analysis. Not only is the mechanical representation of the nacelle vertical freedoms too crude, but also: 1) coupling with the yaw motions is not included, 2)there is no way to account for the effect of side gusts and their coupling with vertical motions, and 3) spanwise variations of gust velocity, not considered in the theory, invalidate the couplings assumed between nacelle and wing motions. As a result, power spectral densities of nacelle loads calculated without the inclusion

of structural damping indicated considerably more power above about 4 cps than was actually present. In earlier studies, to assure realistic nacelle load inputs to the wing, the integration of the power-spectral densities had beer limited to a maximum frequency of about 4-1/2 cps, thereby eliminating the increased response. This had little effect on wing loads since most of their response is in the short period and first tending-torsion modes. In the present study, as a more rational means of preventing possible over estimation of nacelle response at the higher frequencies, structural damping was introduced into the spring connection of the nacelles to the wing. A structural damping coefficient of .20 was assumed; this is the value of g in the expression (1 + ig) k and corresponds, at the resonant frequency, to a relative viscous damping of .10. This damping value appears reasonable, and it sufficiently reduces the high frequency response to give substantially improved agreement with flight measured power spectral densities.

In order to account adequately for the effect of static aeroelastic deflection on the spanwise load distribution and on the gust load factor of the Model 188, it was found necessary to replace the second dynamic wing torsion mode by a static aeroelastic deflection shape. This was because a significant part of the static aeroelastic deformation occurs outboard of the outboard nacelle, whereas neither of the first two dynamic torsion modes contains significant deformation in this region. While some loss of detail in the dynamic representation results, it appears that, over-all, the static aeroelastic mode is more important than the second dynamic torsion mode. It is therefore included in the present Model 188 analysis.

Considerable effort was put forth to assure that, on a static basis, the ten-degree-of-freedom analysis duplicated losas obtained by the accepted static loads methods. For this purpose, ten-degree-of-freedom loads were obtained for both the Model 188 and Model 749 for a maneuver condition obtained by introducing a low-frequency elevator oscillation. The resulting loads are not sensitive to the exact frequency chosen, as long as it is well below that of the airplane short-period mode. The effect of frequency is shown in Table 8-1. Based on the results shown therein, a frequency of .05 cps was selected for the loads comparison. The comparison of ten-degree-of-freedom loads with static analysis loads, per g of c.g. acceleration, is shown in Tables 8-2 and 8-3. Torsional moments are compared on a difference rather than a ratio basis, since torsional moments can easily be close to zero, depending on the location of the arbitrary moment axis, and ratios have little meaning. For comparison, the approximate limit design torsions are noted in the tables. It is seen that the ten-degree-of-freedom analysis reproduces the loads obtained by the static loads analysis very well. The small differences that do exist are not considered significant, especially since in some respects the ten-degree-of-freedom analysis may be more rational than the static analysis.

TABLE 8-1. EFFECT OF FREQUENCY OF ELEVATOR MOTION ON MAGNITUDE OF ROOT BENDING MOMENT

		Model 749		Model 198				
Frequency Of Klevator Motion	10	6 <sub>M_x</sub> /n <sub>z</sub> ew.s.	103	10 <sup>-6</sup> m <sub>x</sub> /n <sub>2</sub> ew.s. 83				
CPS	V <sub>e</sub> =205 Kt	V <sub>e</sub> =235 Kt	V <sub>e</sub> =290 Kt	v <sub>e</sub> =264 Kt	V <sub>e</sub> =314 Kt	V <sub>e</sub> =364 Kt		
.0125	5.720	5.909	6.363	3.646	3.791	4,085		
.025	5.718	5.908	6.387	3.644	3.790	4.085		
.050	5.713	5.904	6.384	3.637	3.785	4.082		
.100	5.691	5,88?	6.373	3.609	3.767	4.070		
.200	5.606	5.822	6.330	3.504	3,700	4.027		
.400	5, 291	5.578	6 <b>. 16</b> 5	3.165	3.476	3.884		
1,00	3.870	4.406	5-335	1.872	2,640	3.446		

TABLE 8-2. COMPARISON OF LOADS COMPUTED BY THE DYNAMIC ANALYSIS PROGRAM AND BY STATIC ANALYSIS METHODS, MODEL 188

	Static Analysis				Dynamic Analysis			Comparison			
Wing Station			10 <sup>-6</sup> My		10 <sup>-6</sup> M <sub>x</sub>	10 <sup>-6</sup> My	Sz <sub>Dyn.</sub>	M <sub>XDyn.</sub>	1.0 <sup>-6</sup> (My <sub>Dyn.</sub> -My Stat.)	10 <sup>-6</sup> My Limit Design	
	V = 264 knots, h = 13500 ft										
83	11259	3.689	127	10948	3.637	022	.975	.987	.105	-7.9	
119	10497	3.292	190	10275	3.264	090	.986	-995	.100	-7.8	
167	8197	2.813	203	8177	2.833	109	-995	1.003	.034	-7.7	
209	11635	2.378	079	11828	2.391	~.045	1.018	1.003	.034	-4.0	
275	9512	1.682	122	9692	1.700	088	1.018	1.007	.034	-3.3	
346	6429	1.121	123	6599	1.131	086	1.023	1,006	.037	-2.6	
380	9151	.831	091	9384	.842	114	1.021	1.011	023	-1.25	
448	5488	.332	053	5593	.340	067	1.020	1.021	014	75	
516	2189	.087	018	2308	.076	025	1.050	.874	007	35	
	V <sub>e</sub> = 314 knots, h = 13500 ft										
83	11391	3,811	+.056	11225	3.785	.023	.966	.994	033	-7.9	
119	10702	3.4.7	009	10617	3.401	046	.99h	1.000	037	-7.8	
167	8487	2.917	024	8595	2.951	066	1.010	1.010	042	-7.7	
209	11977	2.468	+.017	12256	2.494	028	1.018	1.010	045	-4.0	
275	9889	1.749	027	10139	1.774	071	1.020	1.010	044	-3.3	
34:6	6774	1.161	027	7003	1.175	068	1.033	1.010	041	-2.6	
380	9455	.861	096	9726	.875	119	1.028	1.018	023	~1.25	
448	5687	.345	057	5824	.354	070	1.023	1.023	013	75	
516	2275	.092	019	2412	.079	027	1.060	.859	008	35	
				v <sub>e</sub>	- 364 km	cts, h =	13500 kts				
83	11481	4.016	.247	11860	4.082	.089	1.032	1.016	158	-7.9	
119	10951	,	.179	11354	3.671	.018	1.038	1.017	161	-7.8	
167	8923	1 -	.159	9452	3.183	004	1.055	1.023	163	-7.7	
209	12535	1 .	.117	13133	2.691	003	1.043	1.021	120	-4.0	
275	10549		.071	11020	1.913	046	1.043	1.021	117	-3.3	
346	7410	· .	.071	7773	1.256	041	1.043	1.017	112	-2.6	
380	10027	1 -	110	10361	. 937	-,129	1.036	1.020	019	-1.25	
448	6059	1	065	6237	.380	076	1.030	1.022	011	75	
516	2434	l -	023	2594	.085	029	1.064	.868	006	35	

MOTE: Torsion Moments, My are about load axis ATFS 571.2

TABLE 8-3. COMPARISON OF LOADS COMPUTED BY THE DYNAMIC ANALYSIS PROGRAM AND BY STATIC ANALYSIS METHODS, MODEL 188

	-764	tic Anal;	ysis	Dynamic Analysis			Comparison			
Wing Station	S <sub>z</sub>	10 <sup>-6</sup> M <sub>x</sub>	10 <sup>-6</sup> M An <sub>z</sub>	S <sub>z</sub>	10 <sup>-6</sup> M <sub>x</sub>	10 <sup>-6</sup> My	S Dyn S Static	M <sub>x</sub> Dyn M <sub>x</sub> Static	10 <sup>-6</sup> (MyDyn - MyStat)	10 <sup>-6</sup> My Limit Design
V = 205 knots, h = 13000 ft										
103	15627	5.838	-1.775	15499	5.713	-1.658	-990	.98ა	.117	8.12
145	12499	5.219	-1.648	12469	5.132	-1.532	-995	-983	.116	.7.94
191	18154	4.497	-1.798	16197	4.427	-1.741	1.002	.084	.057	-~ .28
263	13730	3.371	-1.528	13813	3.257	-1.470	1.006	•966	.058	-6.53
337	9285	2.496	-1.217	9412	2.424	-1.162	1.014	-971	.055	-5.66
hoh	12507	1.674	-1.250	12522	1.650	-1.264	1.001	.986	.014	-4.40
480	8453	.883	887	8\69	.861	890	1.002	-975	003	-3.26
588	3739	.226	417	3762	.219	420	1.000	.969	003	-1.57
668	1149	.031	127	1167	.022	135	1.016	.710	008	-
V <sub>e</sub> = 235 knots, h = 13000 ft										
103	16949	5-993	-1.844	16715	5.904	-1.748	.986	. 985	.006	-8.12
145	13015	5.328	-1.664	13017	5.280	-1.577	1.000	.991	.087	-7.94
191	19251	4.569	-1.870	19288	4.537	-1.830	1.002	-993	.040	-7.28
263	14017	3.395	-1.539	14229	3.31C	-1.508	1.015	-975	.031	-6.53
337	8950	2.522	-1.176	9280	2.470	-1.155	1.037	-977	.021	-5.66
404	12793	1.687	-1.277	12898	1.681	-1.301	1.008	.996	024	-4.46
480	8512	.885	893	8610	-373	905	1.012	.986	014	-3.26
588	3741	.225	43.7	3803	.222	424	1.017	.987	007	-1.57
668	1146	.031	127	1176	.022	136	1.026	.710	009	
				ν <sub>e</sub>	= 290 kg	ors, h =	13000 ft			
103	18099	6.011	-1.924	19397	6.384	-1.671	1.072	1.082	.253	-8.12
145	13154	5.310	-1.677	14375	5.675	-1.410	1.093	1.069	.267	-7.94
191	20080	4.528	-1.930	21628	4.842	-1.887	1.687	1.069	.043	-7.28
263	13966	3.332	-1.526	15860	3.478	-1.456	1.108	1.044	.070	-6.53
337	8117	2.496	-1.106	9211	2,606	-1.004	1.135	1.044	.102	-5.66
404	12865	1.670	~1.282	13906	1.773	-1.401	1.031	1.062	119	-4.46
¥80	8412	.871	882	9040	.910	951	1.075	1.045	069	-3.26
588	3672	.220	409	3946	.229	440	1.075	1.036	031	-1.57
668	1122	.013	124	1213	.023	140	1.081	.742	016	-

NOTE: Torsion moments, Ny, are about load axis at FS458.8

Inasmuch as results of an analysis including the pitch freedom can be somewhat sensitive to the static stability in pitch, precautions were taken to assure that the pitch stability is correctly reflected in the analysis. Since the pitch stability results from the sum (or difference) of many different contributors - including each wing element, the nacelles, the propellers, the fuselage, the tail, the control system, all of the masses - the many separate contributions do not always add up to the best value for the airplane as a whole, and adjustments were made as needed.

An option with respect to pilot technique is available in that flight can be assumed to be either "stick-fixed" or "stick-free." In order to account realistically for the strongly stabilizing effect of the Model 188 control column bob-weight, it was considered appropriate to assume a stick-free technique. Moreover, recommended techniques for flight through turbulence have generally called for a very light touch on the control column, which would appear to be more closely approximated by a stick-free than a stick-fixed condition. Accordingly, both Model 188 and Model 749 vertical gust analyses were conducted stick-free. A comparison of stick-fixed with stick-free results, however, indicated that the loads produced were not sensitive to the choice between the two assumptions.

## 8.2 Lateral Gust, Models 188 and 749

8.2.1 Equations of Motion. The equations of motion employed to determine Model 138 and Model 749 loads due to the lateral component of turbulence were derived following closely the derivation presented in NACA TN 3603 (Reference 22).

The equations of motion are written with respect to an Eulerian moving axis system and utilize as generalized coordinates the three rigid-body motions of sideslip, yaw, and roll. Provision is included for inertia coupling between the generalized coordinates through the product of inertia,  $I_{XZ}$ ; however, for the Model 188 and Model 749 this term is so small as to have negligible effect and is assumed to be zero.

Elastic mode response is not included. For both the Model 188 and the Model 749, the lowest fuselage-tail side bending natural mode is far higher in frequency than the Dutch roll mode - roughly 6 to 8 cps vs .2 to .3 cps. Consequently, for these airplanes, the elastic modes were expected to contribute negligibly to the loads produced by turbulence.

Provision is made to include the effects of rudder and aileron float, if desired, or of artificial stability augmentation systems.

For the purpose of accounting for the penetration of the various aerodynamic elements into the gust, aerodynamic forces are evaluated separately for the wing, fuselage, and vertical tail. Wing and fuselage aerodynamic forces are lumped at the airplane c.g., and tail forces at the vertical tail aerodynamic center.

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Provision is made in the equations of motion for the effect on each aero-dynamic element of the sidewash produced by the other elements; but the best indications are that on the Model 188 and Model 749 the side-wash is negligible, and it is assumed zero in the analysis.

Unsteady lift growth functions for gust encounter (Kussner function) and for airplane motions (Wagner function) are represented separately for the vertical tail, the fuselage body, and the wing. Suitable exponential approximations are used; the effective chord for use in these expressions is taken equal to the mean chord for the vertical tail and wing and zero for the fuselage.

Fuselage loads at any desired fuselage station are obtained by superposition of inertia loads due to lateral, rolling, and yawing accelerations (including the lateral component of gravity) and aerodynamic loads due to the net sideslip angle at the airplane c.g.

The three simultaneous differential equations of motion are solved for a forcing function consisting of a steady sinusoidal variation of lateral gust velocity. Frequency-response, or transfer, functions relating both the generalized coordinates and the various airplane load quantities to the input gust velocity are thus evaluated, at up to 40 frequencies. The modulus of each transfer function is squared and multiplied by the input gust spectrum to obtain an output power spectrum. These in turn are integrated with respect to frequency to give  $\overline{A}$  and  $N_{\rm O}$  values. The upper limit of integration was taken as 9 cps. The lower limit of integration was taken as .04 cps instead of 0, in order to exclude a sizeable response associated with an unstable spiral mode which, in practice, would be adequately controlled by the pilot.

All of the calculations indicated above were carried out in a continuous operation on an IBM 7094 automatic digital computer.

A complete presentation of the equations of motion, including their derivation, is contained in Reference 23.

8.2.2 Input Data for Dynamic Analysis. Airplane mass data for use in the Model 188 and Model 749 lateral gust analyses were drawn from calculations made in the course of design loads determination.

The various stability derivatives were obtained from a careful evaluation and integration of such sources as wind tunnel force measurements,

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flight-measured stability and control characteristics, theoretical calculations, and published NASA information.

The following quantities were selected for load determination:

Quantity	Location Model 188	Location Model 749
Fin side load	Total for fin	Total for three fins
Fin bending moment	Fin root	(Not obtained)
C.G. lateral acceleration	Actual c.g.	Actual c.g.
Pilot station lateral acceleration	FS 132	FS 200
Vertical tail lateral acceleration	FS 1161	FS 1194
Aftbody side shear	FS 694	FS 1057
Aftbody side bending	<b>FS</b> 694	FS 1057
Aftbody torsion	FS 694	FS 1057
Forebody side shear	FS 571	<b>FS</b> 456
Forebody side bending	FS 571	<b>FS</b> 456

The fin side loads were obtained ignoring the effect of relieving inertia. Results for a representative case - Model 188 mission analysis case 201 - indicated that inclusion of the relieving inertia reduced the load by only about 3%.

In selecting specific values for the Kussner and Wagner unsteady lift growth functions for use in the lateral gust analysis, it appeared at first that any reasonable approximation would be satisfactory. Loads due to lateral gust occur predominantly at frequencies in the vicinity of the Dutch roll natural frequency. As a result of the low frequency of this mode, in combination with a vertical tail chord length considerably less than that of the wing, the unsteady lift growth functions are very close to unity, and it appeared that it would be hard to be very far in error in their determination. Accordingly, for the fin, exponential approximations appropriate to an infinite aspect ratio surface at low Mach number were assumed initially.

Closer examination of the unsteady lift growth functions, however, indicated this assumption to be inadequate. The absolute value and the real part, or in-phase component, of both Kussner and Wagner lift growth functions were indeed close to unity, with values of about .97. The imaginary part, or 90-degree out-of-phase component, of the Kussner function is of no concern, except for the extent to which it might be different for two parts of the same airplane. The imaginary part of the Wagner function, however, is quite significant. Based on the high aspect-ratio, low Mach number assumption, its value is about .07. This, acting upon the aerodynamic spring force - which is several times as great as the damping force - produces a sizeable force in phase with, and in the same direction as, the yaw velocity. Thus a negative damping force increment is introduced. This was found to reduce the damping coefficient,  $\zeta$  , for the Dutch roll mode to about 2/3 of the value it would have with instantaneous lift growth. Inasmuch as the various A values vary approximately inversely , the corresponding increase in A values due to the unsteady lift growth is about 22%.

Because of this sizeable effect, it became important to use the best available information for the Wagner lift growth function. Accordingly, the assumed exponential approximation was replaced by one which accounts approximately for the actual aspect ratio and Mach number.

The expression used was of the form

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where s is the distance traveled in chord lengths. The values selected for the constants were a = .40 and b = .376. The original form of the Kussner function was considered satisfactory and was retained.

The effect of the revised lift growth function was evaluated by comparing  $\overline{A}$  and  $N_O$  values computed using the two different versions of the Wagner function for both the Model 188 and the Model 749. Generally the  $\overline{A}$  values decreased by about 10% and the  $N_O$  values increased by about 8%. Therefore, the improved lift growth representation shown above was used throughout the lateral analysis.

As in the vertical gust analysis, options were available as to assumed pilot technique. The effect of pilot technique on gust loads may be substantial. It is undoubtedly complex, and a completely rational treatment is well beyond the present state of the art. Several idealized techniques, however, are readily amenable to analytical representation.

These include various combinations of the following: (a) Rudder held fixed, or rudder free to float, or rudder controlled so as to eliminate

all yaw motion of the airplane; (b) ailerons held fixed, or ailerons free to float, or ailerons controlled so as to eliminate all roll motion.

In order to determine how much the results of the analysis might be affected by the choice of pilot technique, responses were obtained, for Model 188 mission analysis case 202, for four of the nine available techniques.

- (1) "Rudder fixed" rudder and ailerons fixed.
- (2) "Rudder free" rudder free, ailerons fixed.
- (3) "No roll" rudder fixed, ailerons controlled so as to prevent all roll motion.
- (4) "No roll, no yaw" rudder and ailerons controlled so as to prevent roll and yaw motion.

Major attention was directed to the first three of these techniques. Although a still more restrictive control action could be assumed, as represented by technique (4), it was considered unlikely that a pilot would attempt much tighter control than represented by techniques (1) through (3).

Consideration was also given to inclusion of autopilot operation. Discussions with persons familiar with operating practices indicated that autopilots are sometimes used in fairly light turbulence, up to peak vertical gust load factors of about .25 to .30. At this point the autopilot is almost certain to be disengaged. Consequently, autopilot action was not further considered in the present study.

The  $\overline{A}$  values (ratios of rms response to rms gust velocity) for the four pilot techniques investigated are as follows:

Pilot Technique	C.G. Lateral Load Factor	Pilot Station Lateral Load Factor	Sideload On Vertical Tail
(1) Rudder fixed	.00564	.00233	270
(2) Rudder free	.00715	.00286	304
(3) No roll	.00568	.00236	275
(4) No roll, no yaw	(.00504)	(.00504)	(249)

The corresponding power spectral densities are shown in Figures 8-3 through 8-5.

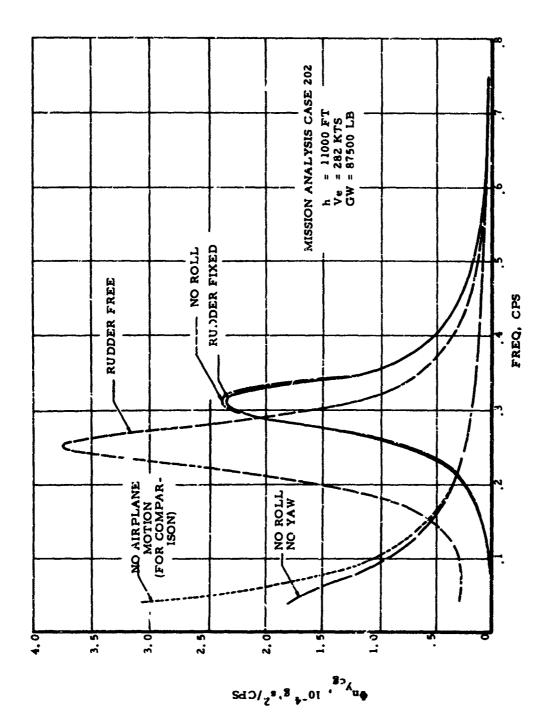


FIGURE 8-3. POWER SPECTRAL DENSITY OF MODEL 188 CG LATERAL LOAD FACTOR FOR VARIOUS PILOT TECHNIQUES

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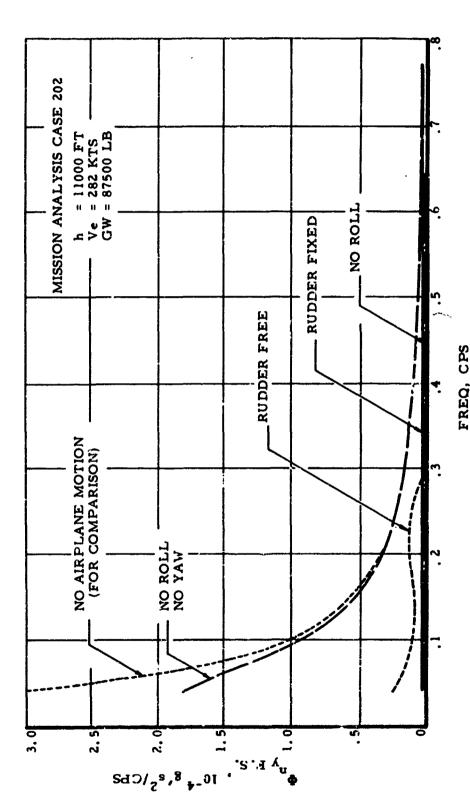


FIGURE 8-4. POWER SPECTRAL DENSITY OF MODEL 188 PILOT STATION LATERAL LOAD FACTOR FOR VARIOUS PILOT TECHNIQUES

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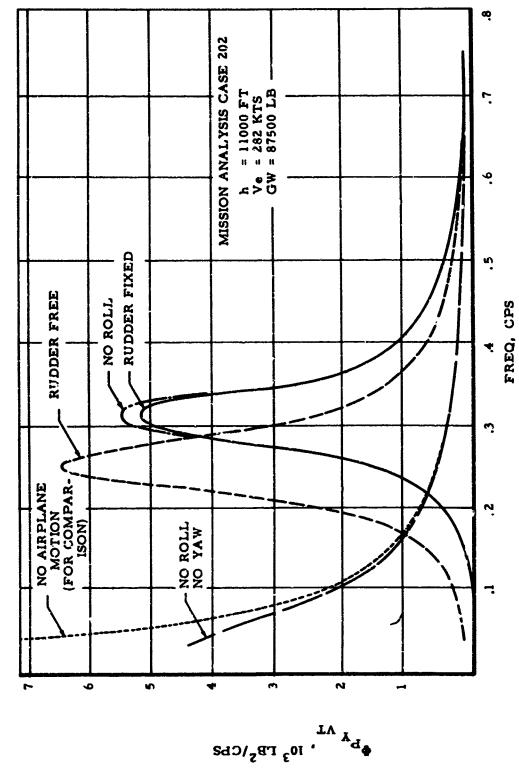


FIGURE 8-5. POWER SPECTRAL DENSITY OF MODEL 188 FIN SIDE LOAD FOR VARIOUS PILOT TECHNIQUES

The values shown in the above table for the no roll, no yaw case are of limited meaning. As noted earlier, the range of integration had already been set to start at .04 cps in order to exclude the spiral mode at the very low frequencies. For the no roll, no yaw case, nowever, as can be seen from the power-spectral density plots in Figures 8-3 through 8-5, the frequencies below .04 cps contribute substantially to  $\sigma^2$ . Including this contribution would increase the A values by some 15%. Furthermore, at the very low frequencies where the greatest contribution occurs, it is highly uncertain what the pilot would actually be coing. To eliminate all yaw motion of these frequencies, it would appear necessary for the pilot to devote continuous attention to a heading indicator, or for an autopilot to be used.

For the remaining three cases, which are considered more realistic, the effect of pilot technique on the tail load is seen to be gratifyingly small. The spread from the lowest to the highest A value is only about 10%; and Case (4) would even fall within the same range if increased by 15% as would appear appropriate from the discussion above. The lateral accelerations differ somewhat more, but critical stresses due to lateral gust depend far more on tail load than on accelerations.

The power-spectral densities are also quite similar for the three more reasonable techniques. The chief difference is a decrease in the frequency of the peak response for the rudder-free case relative to the rudder-fixed cases, as a result of the decreased static stability. It is interesting to note that locking out the roll motion has a negligible effect on the frequency for peak response as well as on the magnitude of the response. For this airplane, at least, the major characteristics of the "Dutch roll" mode, from the gust load standpoint, seem to be preserved even when roll motion is excluded. The reason may be that for a high aspect ratio airplane the damping in roll is so great as to effectively eliminate the roll motion, without further action by the pilot. For Case (4), the power-spectral density function shapes differ markedly from those shown for Cases (1) - (3), and the close agreement in A values must be considered largely coincidental.

The lateral accelerations at the pilot station (second column in the above tabulation, and Figure 8-4) are, for all three cases, somewhat lower than at the c.g., due to the relieving effect of the yaw acceleration. The sharp resonant peak at about .3 cps happens to be almost completely eliminated. The power spectral density remains fairly constant, however, over the entire range from about .05 to 3.0 cps, so that the percentage effect on  $\overline{A}$  is not as great as would be inferred from the power spectral density values at the Dutch roll frequency.

In summary, the critical stresses in the airframe due to lateral gusts are essentially unaffected by the pilot technique assumed, withi; the

range of assumptions investigated herein and considered realistic. Consequently, any of the first three pilot techniques could be selected, without significant effect on the frequency of exceedance of  $\sigma_{\rm W}$   $\eta_{\rm d}$  values corresponding to limit strength. The rudder-fixed assumption is perhaps as realistic as any. It is probably the one that has been used most generally in the past, and it avoids the need for incorporating rudder float aerodynamic data in the analysis. The rudder-fixed, aileron-fixed pilot technique was therefore assumed in the remainder of the lateral gust investigation.

The characteristics of the Models 188 and 749 are such that lateral gust response had not, in the past, been the subject of extensive analysis. Consequently, it appeared important to gain a better feel for the reasonableness and significance of the results obtained by comparing the results for a particular case, at least qualitatively, with loads and accelerations measured in flight.

Such measurements were available as a result of instrumented flights through turbulence of the Model 188. Although the principal purpose of these flights was to measure the response to vertical gusts, time histories of c.g. lateral acceleration and fin root shear were also included. Rms values, power-spectral densities, and peak counts were available for the c.g. lateral acceleration, but no reduction of the fin shear data had been performed. Although cases corresponding exactly to the flight test conditions were not included in the analysis, mission analysis Case no. 202 did not differ greatly. And by making the comparison on the basis of ratios of side to vertical acceleration, the effects of differences in flight conditions were minimized. The results of the side load factor comparison are shown in the following table.

			$v_e$		RMS Val	ues
Test	G.W.	Altitude	(Knots)	$\Delta n_y$	$\Delta n_z$	$\Delta n_y / \Delta n_z$
532	§1,600	8,000	260	.0558	.135	.44
544	108,400	1,500	268	.0465	.128	.36
552	85,600	4,700	°268	.082	.217	.38
Average	:					•39
Analysi (Rudder	s 92,300 Fixed)	11,000	282	.00564	.02192	.26

It is seen that the average measured value of the ratio  $\Delta n_y/\Delta n_z$  is greater than the analytical value in the ratio .39/.26 = 1.50.

In searching for the reason for this discrepancy, the flight-measured power-spectral density curve was examin-This curve is shown in Figure 8-6. Its most striking feature is a large contribution in the 4.5 - 3.5 cps range, due evidently to elastic mode response. Roughly 60% of the area under the curve occurs beyond 3 cps, indicating a dynamic factor due to elastic mode response of about  $\sqrt{1.00/.40} = 1.58$ . The analytical model, on the other hand, makes no provision for elastic mode effects. As indicated above, the lowest fuselage-tail side-bending elastic mode, for both airplanes, is far higher in frequency than the Dutch roll mode; consequently, it was expected that the elastic modes would not contribute significantly to the loads produced by turbulence and could be omitted from the mathematical model. If the flight-measured value of  $\Delta n_y/\Delta n_z$ , .39, is divided by the indicated dynamic factor of 1.58, the result is .25; this is in good agreement with the analytical value of .26.

Although the analytical and flight-measured lateral accelerations were thus reconciled, the presence of a significant elastic mode contribution in the flight-measured load factor did raise the question of the adequacy of the analytical model for the purposes of the present study. In order to obtain a more direct indication of the effect of the elastic mode response on critical structural loads, the flight-measured fin root shear time history from one test only was processed to obtain its power spectral density. The resulting curve is shown in Figure 8-7. Although the frequency resolution is not adequate to define the curve in detail in the vicinity of the Dutch roll frequency, it is clear that the elastic mode effects are relatively small. Also, it is noted that the dynamic response occurs not in the 4.5 - 8.5 cps range, as in Figure 8-6, but in the vicinity of 12 cps.

Consequently, the existing mathematical model should yield quite realistic vertical tail loads. Furthermore, the fuselage is critical for lateral gust loads only in the aftbody. It would appear that airloads from the vertical tail will contribute a good deal more to the critical aftbody loads than will fuselage inertias. In this connection, inspection of Model 188 shake test results indicates a fuselage lateral bending-torsion mode at about 8 cps, which was probably the major contributor to the elastic mode peak in Figure 8-6. This mode has a node line running approximately longitudinally at the fin root. Consequently, there will be some tendency for the inertia forces acting on the fin to offset those acting on the fuselage. In all, it appears that the existing mathematical model should yield fairly realistic values of frequency of exceedance of limit and ultimate strength, and of limit and ultimate strength values of  $\sigma_{\rm w}$   $\eta_{\rm d}$ .

MODEL 188A SERIAL NO. 1001 TEST 532

GW = 81730 LB

CG = 21. 1% MAC

Ve = 266 KTS

h = 8400 FT

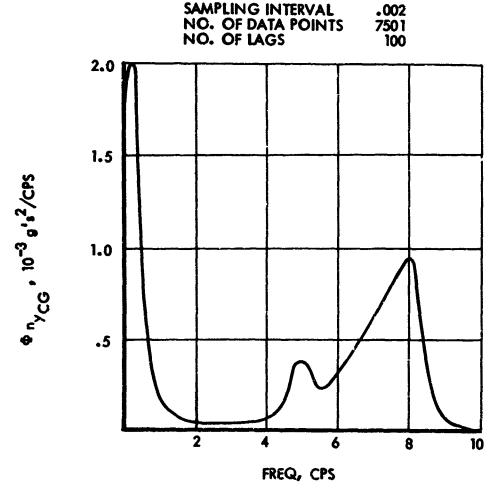
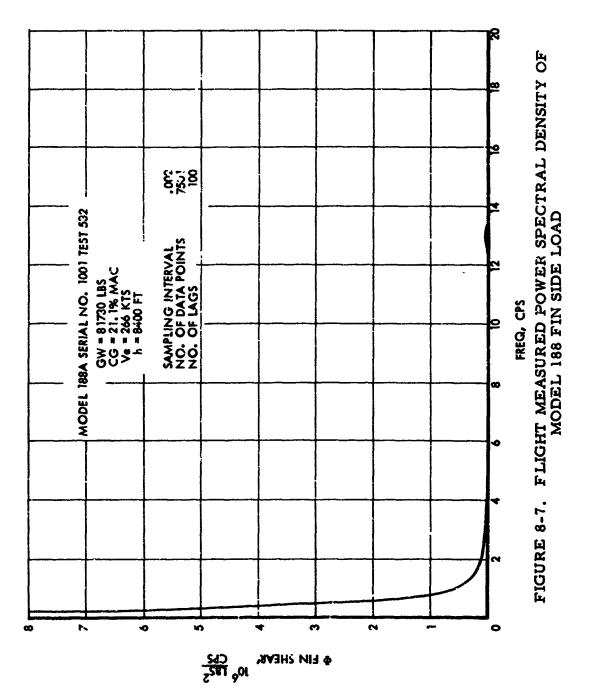


FIGURE 8-6. FLIGHT MEASURED POWER SPECTRAL DENSITY OF MODEL 188 CG LATERAL LOAD FACTOR



## 9 RESULTS OF ANALYSIS

A and No values obtained from the vertical gust and lateral gust dynamic analyses of the Model 188 and Model 749, together with the associated one-g level flight loads, are presented for reference in Appendix B.

Sample power-spectral densities of c.g. load factor are shown for the two airplanes in Figures 9-1 and 9-2. These are for a representative mission analysis segment in each case

Sample power-spectral densities of a number of wing and fuselage load quantities, for the same mission segments, are shown in Figures 9-3 and 9-4 for the Model 188 and in Figure 9-5 for the Model 749.

Sample power-spectral densities for fin root shear and c.g. lateral acceleration, obtained from the lateral gust analyses, are shown in Figures 9-6 and 9-7 for the Model 188 and Model 749 respectively.

For use later in determining N(y) values corresponding to limit and ultimate strength, exceedance curves were prepared for all load quantities. For the various wing load quartities, separate curves were obtained for both positive and negative gust increments. The preparation of these curves followed the procedure outlined at the end of Section 4.1, using b and P values from Figures 5-3 and 5-4 and  $\overline{A}$  and  $N_O$  values from Tables B-1, B-3, B-5, and B-7.

Frequency of exceedance curves for Model 188 loads due to vertical gusts, at representative wing and fuselage locations, are shown in Figures 9-8(a) through (d). The curves are plotted in these figures on a compressed scale in order to show the full range from close to zero load increment to loads in the region of ultimate strength. The same quantities are also plotted to expanded scales in Figures 9-9(a) through (d), in order to show in more detail the region of limit strength, including the contributions of the individual mission segments. It is in this latter form that the complete set of exceedance curves referred to above was obtained.

Similar curves are also shown for wing loads in the root region of the Model 749. The compressed-scale curves are shown in Figure 9-10, and the expanded scale curves, showing the contributions of the various mission segments in the region of limit strength, in Figure 9-11.

Frequency of exceedance curves for airplane c.g. load factor, obtained similarly, are shown in Figures 5-9 and 5-10, together with the experimentally determined curves based on airline VGH and VG data for comparison. This comparison was discussed in Section 5.6.

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Frequency of exceedance curves for fin root shear are shown in Figures 9-12 through 9-15. Both compressed-scale and expanded-scale plots are shown, as in the corresponding vertical gust presentations.

A values of fin root shear for some of the Model 188 design envelope cases are plotted vs altitude in Figure 9-16. To provide a preliminary indication of the critical altitude,  $\overline{A}$  values from Fig. 9-16 are then multiplied by  $y/\overline{A}$  values given in Figure 5-6, for an  $N(y)/N_0$  value of 10-6, and plotted in Figure 9-17. (The 10-6 level was selected arbitrarily, but corresponds roughly to the limit strength level.) Similar curves for the Model 749 are shown in Figures 9-18 and 9-19.

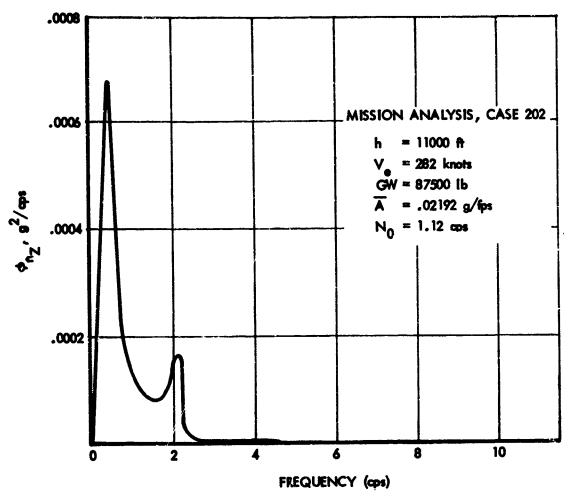


FIGURE 9-1. POWER SPECTRAL DENSITY OF CG LOAD FACTOR DUE TO VERTICAL GUST, MODEL 188

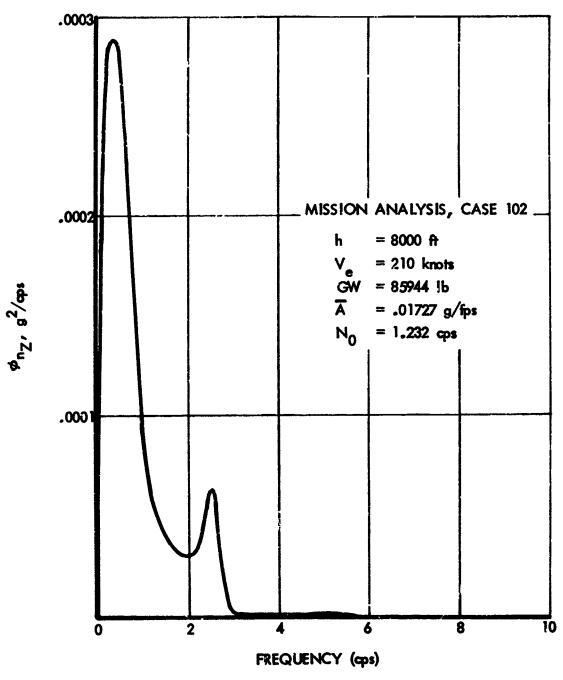
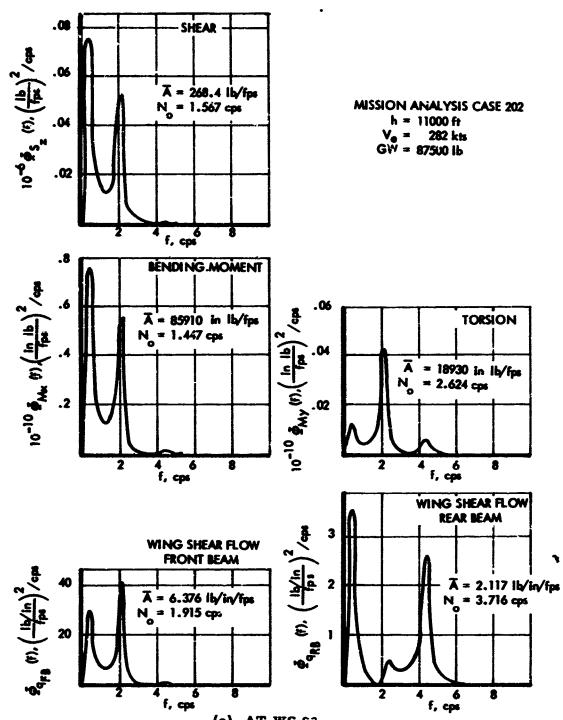
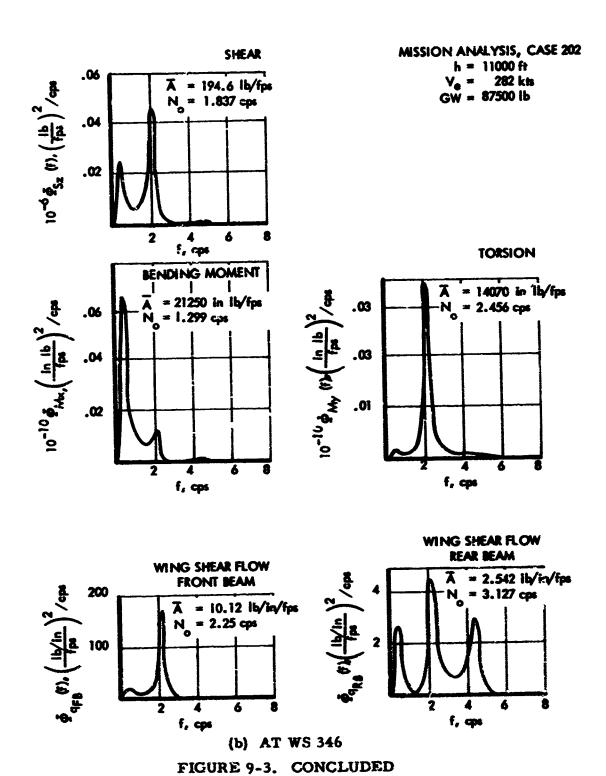
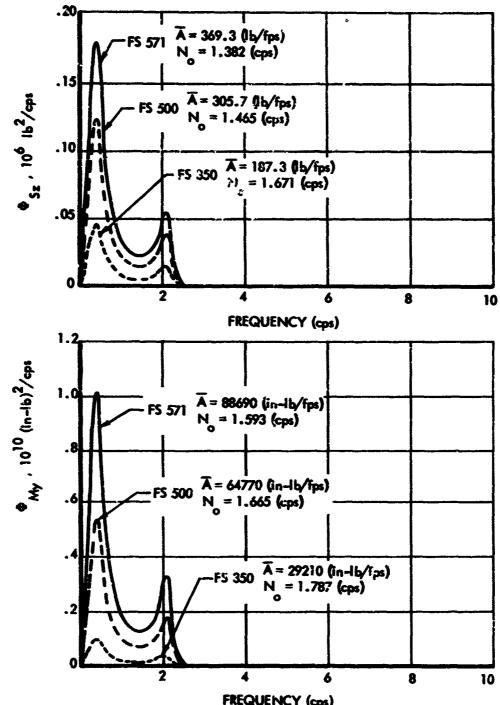


FIGURE 9-2. POWER SPECTRAL DENSITY OF CG LOAD FACTOR DUE TO VERTICAL GUST, MODEL 749



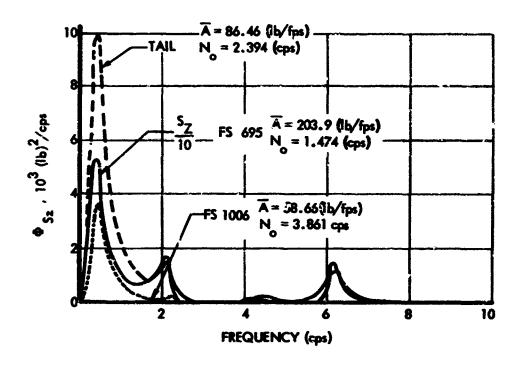
(a) AT WS 83
FIGURE 9-3. POWER SPECTRAL DENSITY OF VARIOUS WING LOADS,
MODEL 188

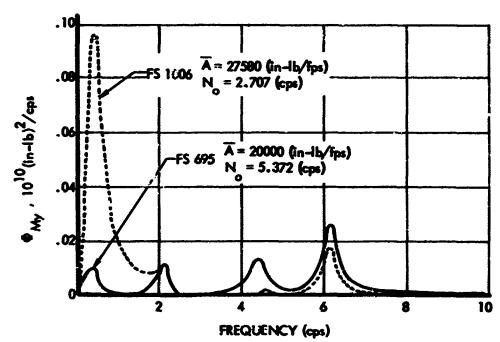




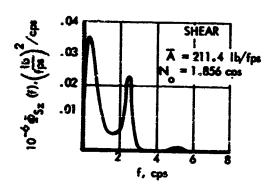
HEAT WAS A STREET OF THE STREE

FREQUENCY (cps)
(a) FOREBODY
FIGURE 9-4. POWER SPECTRA OF MODEL 188
FUSELAGE LOADS-CASE 202



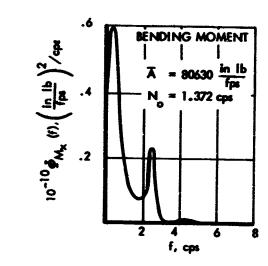


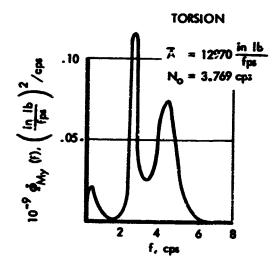
(b) AFTBODY FIGURE 9-4. CONCLUDED

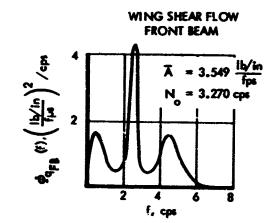


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MISSION ANALYSIS, CASE 102 h = 8000 ft V<sub>a</sub> = 210 kts GW = 85944 lb







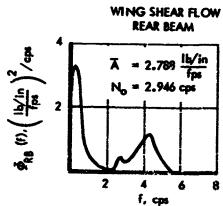
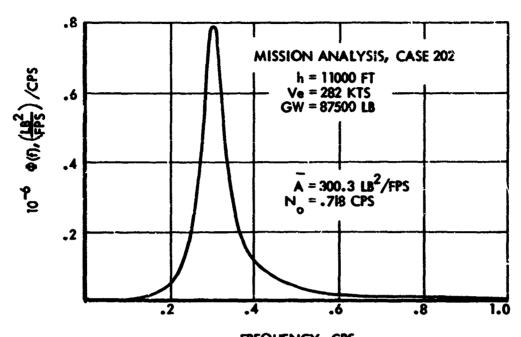
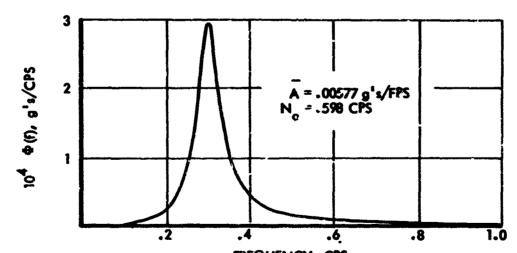


FIGURE 9-5. POWER SPECTRAL DENSITY OF VARIOUS WING LOADS AT WS 145, MODEL 749





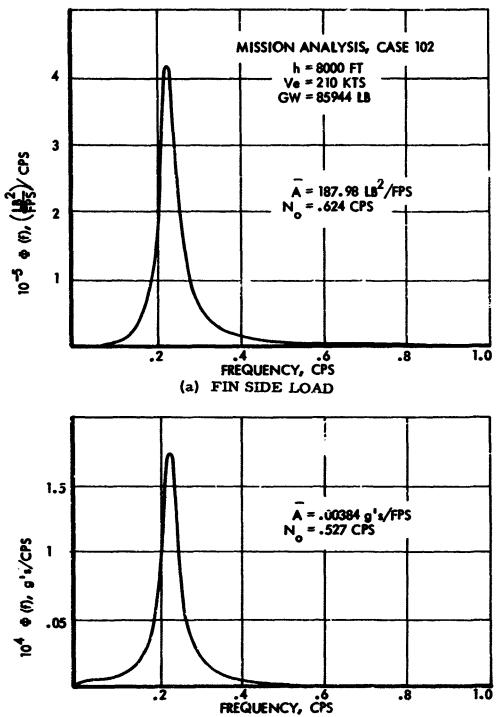


FREQUENCY, CPS

(b) CG LATERAL ACCELERATION

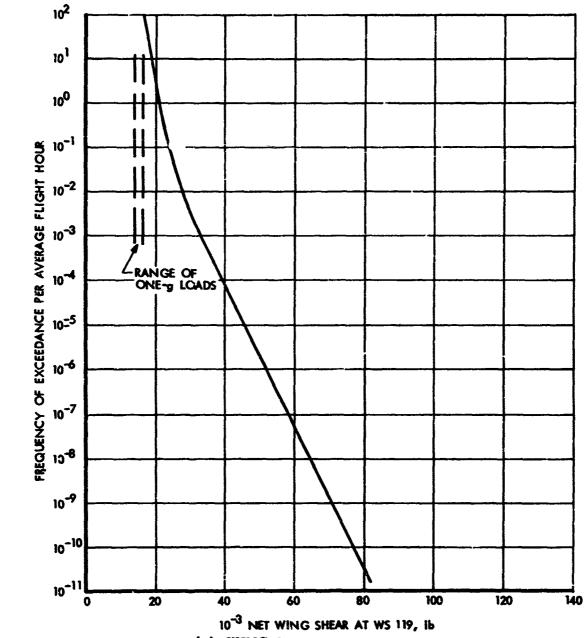
FIGURE 9-6. POWER SPECTRAL DENSITY OF FIN SIDE LOAD AND

CG LATERAL ACCELERATION, MODEL 188

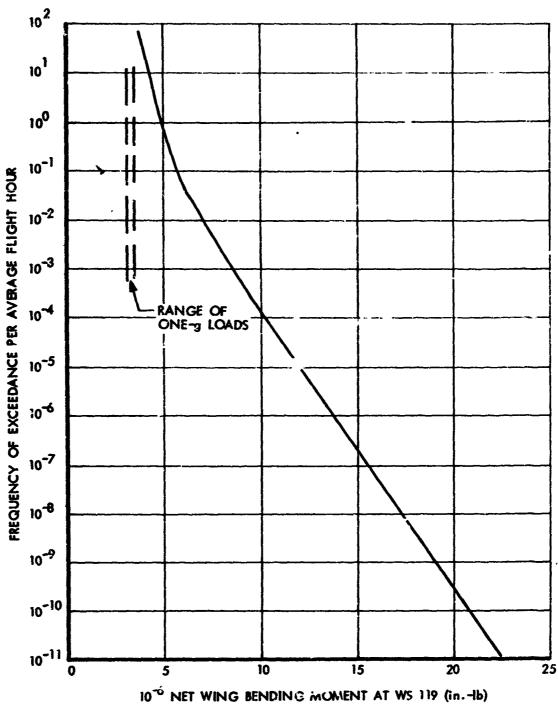


(b) CG LATERAL ACCELERATION
FIGURE 9-7. POWER SPECTRAL DENSITY OF FIN SIDE LOAD AND
CG LATERAL ACCELERATION, MODEL 749

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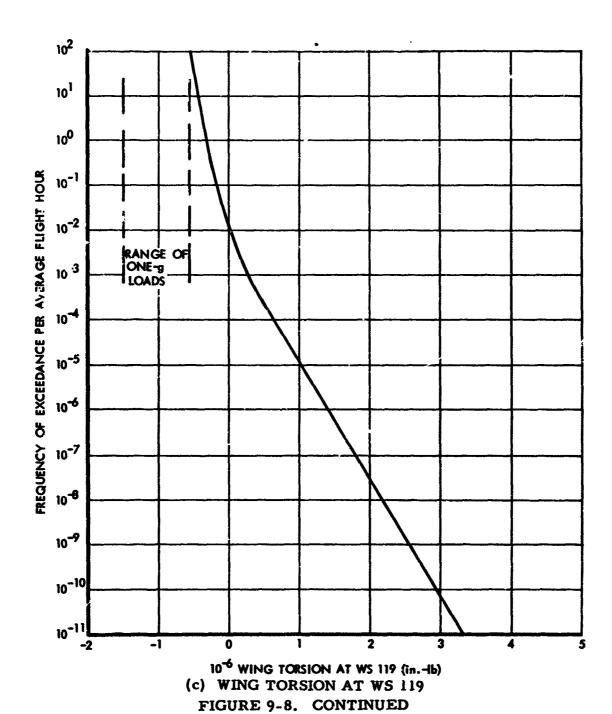


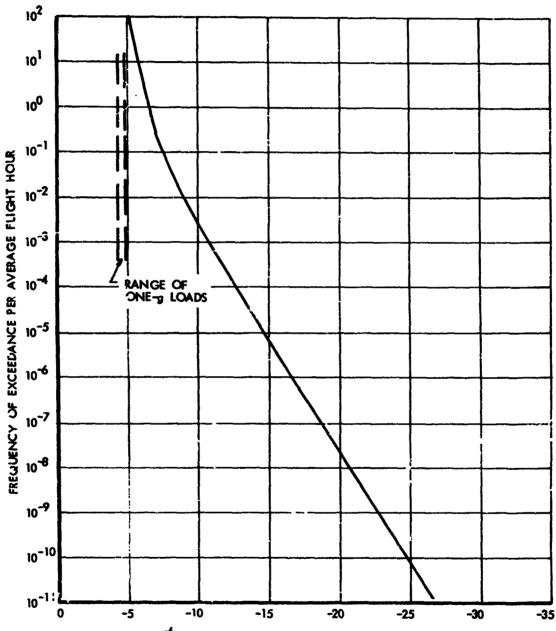
(a) WING SHEAR AT WS 119
FIGURE 9-8. FREQUENCY OF EXCEEDANCE OF MODEL 188 WING
AND FOREBODY LOADS



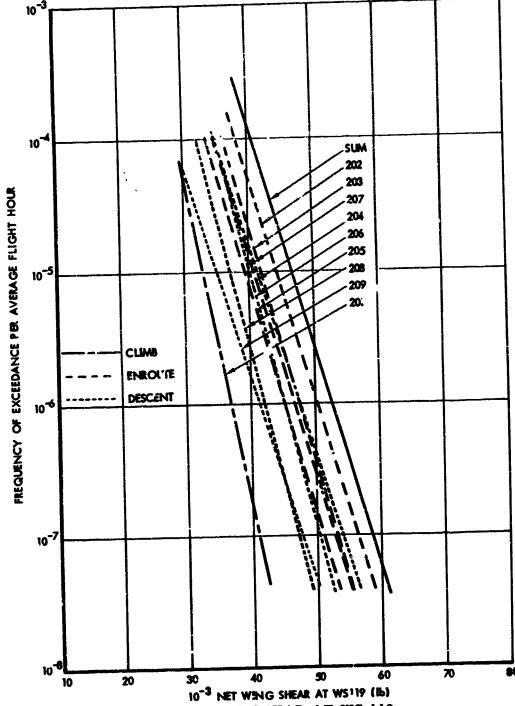
(b) WING BENDING MOMENT AT WS 119
FIGURE 9-8. CONTINUED

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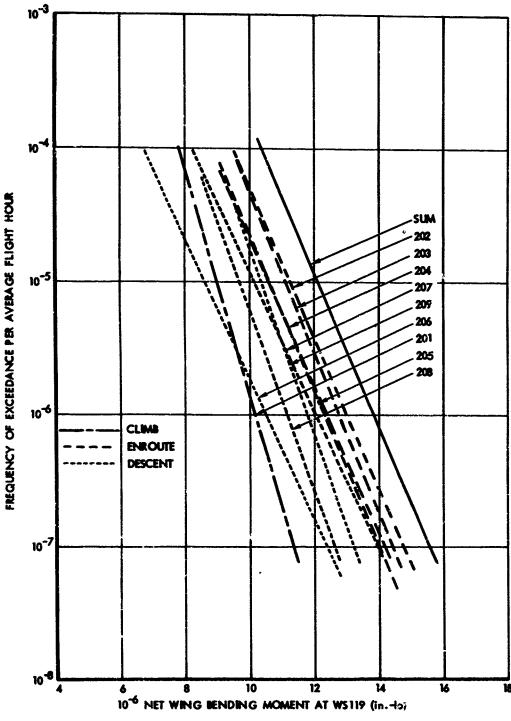
10<sup>-6</sup> FUSELAGE BENDING MOMENT AT FS 571 (in.-1b)
(d) FOREBODY BENDING MOMENT AT F.S. 571
FIGURE 9-8. CONCLUDED.



10 20 10-3 NET WING SHEAR AT WS 119 (Ib)

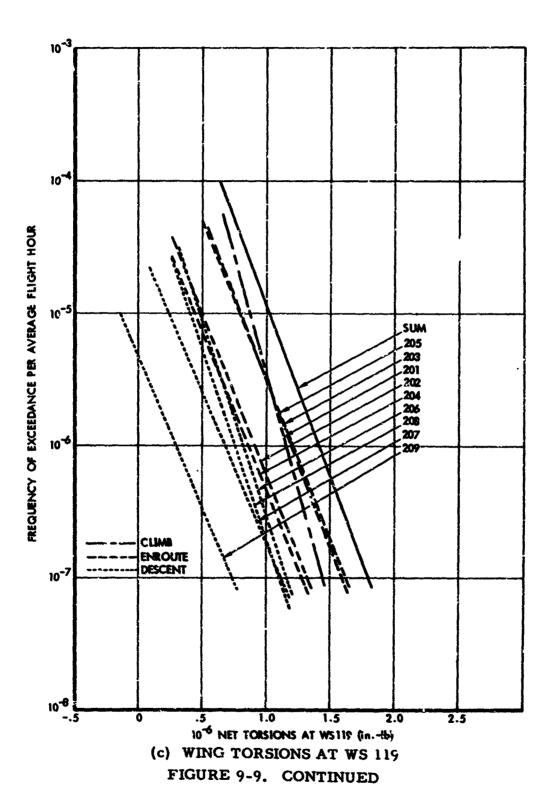
(a) WING SHEAR AT WS 119

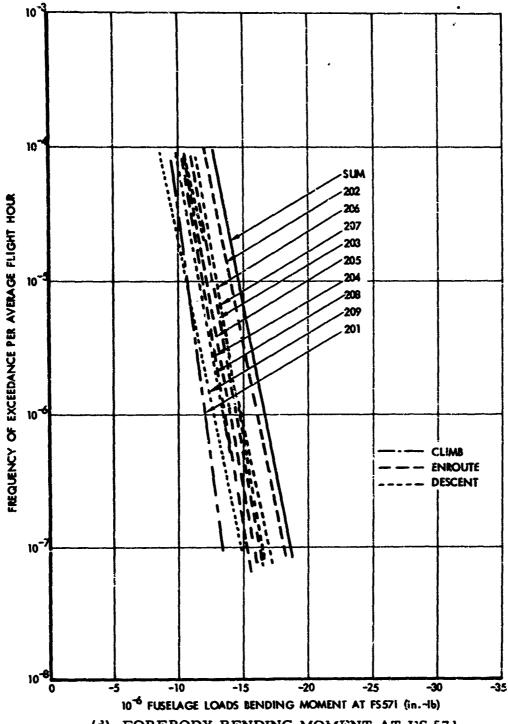
FIGURE 9-9. FREQUENCY OF EXCEEDANCE OF MODEL 188 WING AND FOREBODY LOADS, EXPANDED - SCALE PLOTS



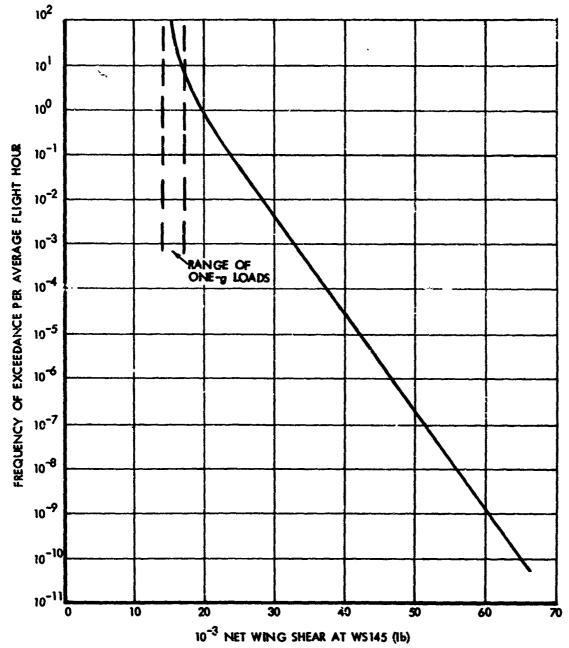
(b) WING BENDING MOMENT AT WS 119 FIGURE 9-9. CONTINUED

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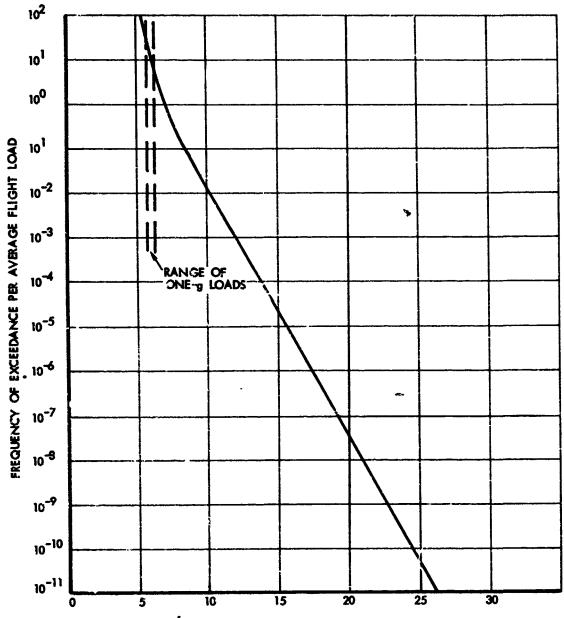




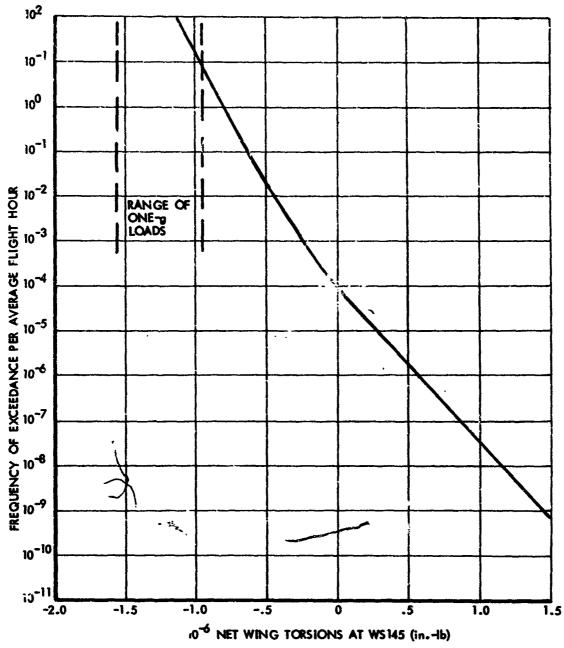
(d) FOREBODY BENDING MOMENT AT FS 571
FIGURE 9-9. CONCLUDED



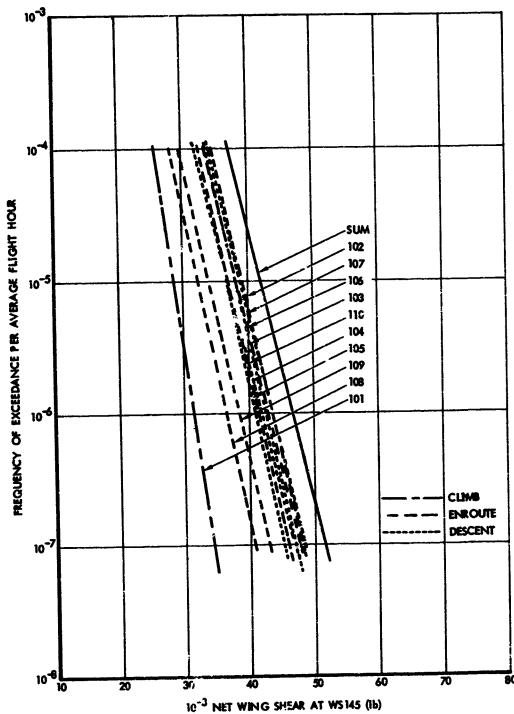
(a) SHEAR AT WS 145
FIGURE 9-10. FREQUENCY OF EXCEEDANCES OF MODEL 749 WING
LOADS



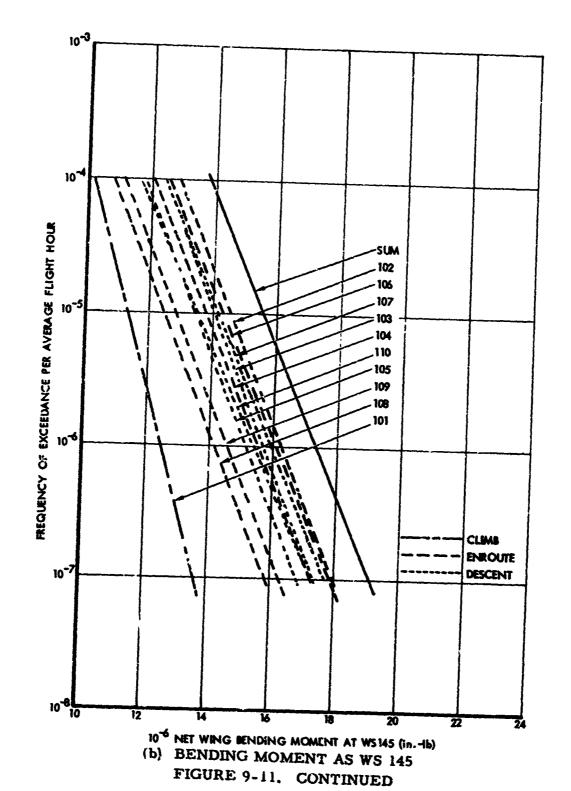
10<sup>-6</sup> NET WING BENDING MOMENT AT WS145 (in.-1b)
(b) BENDING MOMENT AT WS 145
FIGURE 9-10. CONTINUED

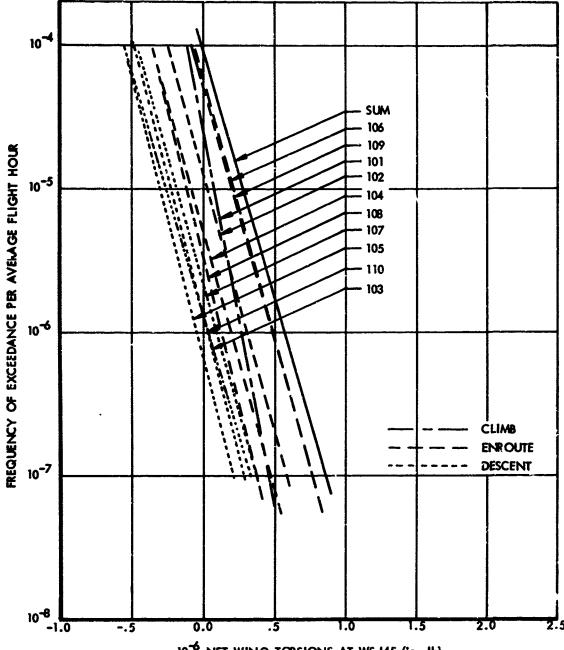


(c) TORSION AT WS 145
FIGURE 9-10. CONCLUDED



(a) SHEAR AT WS 145
FIGURE 9-11. FREQUENCY OF EXCEEDANCE OF MODEL 747 WING
LOADS, EXPANDED SCALE PLOTS





10<sup>-6</sup> NET WING TORSIONS AT WS 145 (in.-1b) (c) TORSION AT WS 145 FIGURE 9-11. CONCLUDED

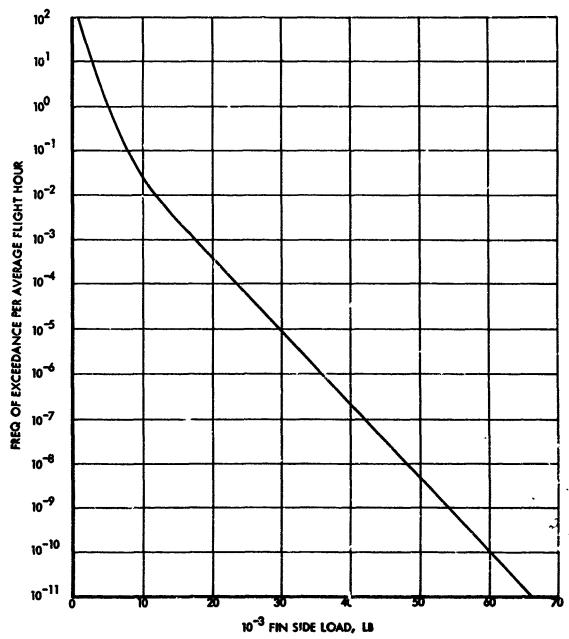
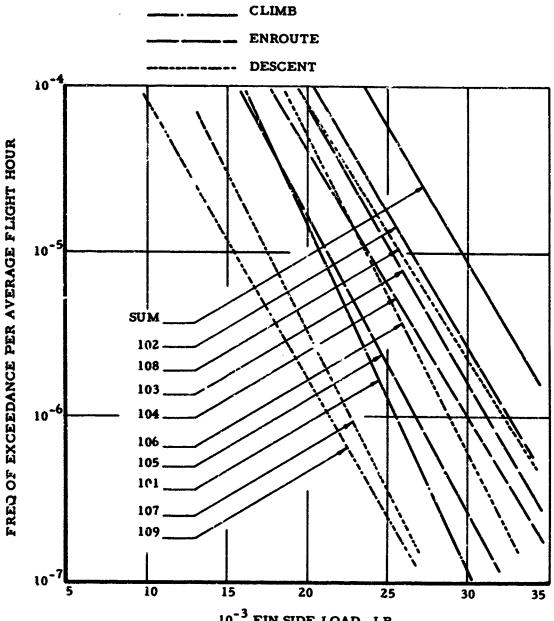


FIGURE 9-12. FREQUENCY OF EXCEEDANCE OF FIN SIDE LOAD, MODEL 188



10<sup>-3</sup> FIN SIDE LOAD, LB FIGURE 9-13. FREQUENCY OF EXCEEDANCE OF FIN SIDE LOAD, MODEL 188 - EXPANDED - SCALE PLOT

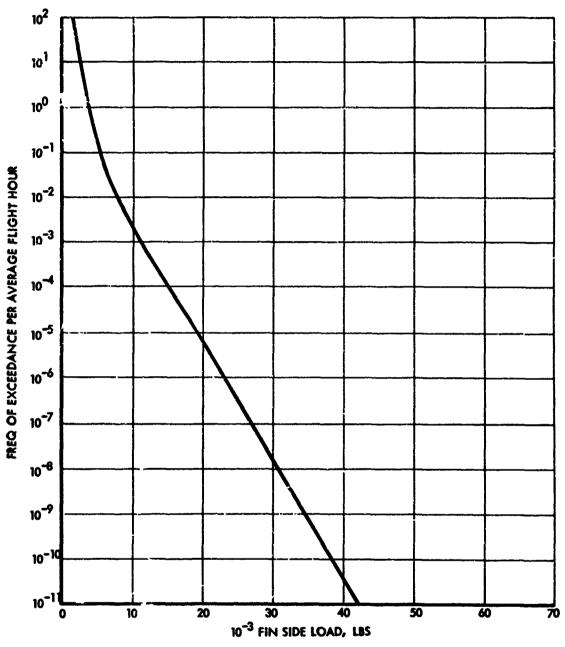


FIGURE 9-14. FREQUENCY OF EXCEEDANCE OF FIN SIDE LOAD, MODEL 749

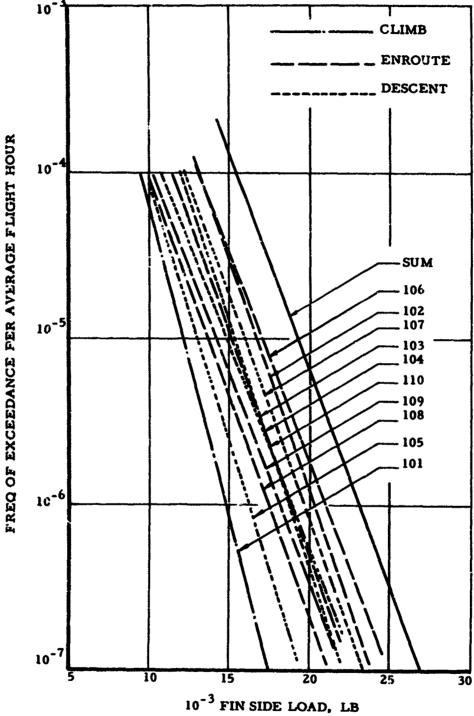


FIGURE 9-15. FREQUENCY OF EXCEEDANCE OF FIN SIDE LOAD, MODEL 749 - EXPANDED SCALE PLOT

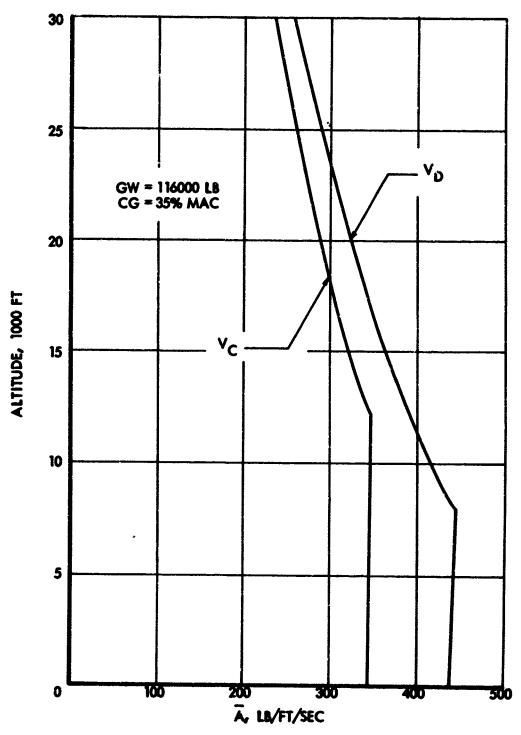


FIGURE 9-16. VARIATION WITH ALTITUDE OF A FOR FIN SIDE LOAD, MODEL 188

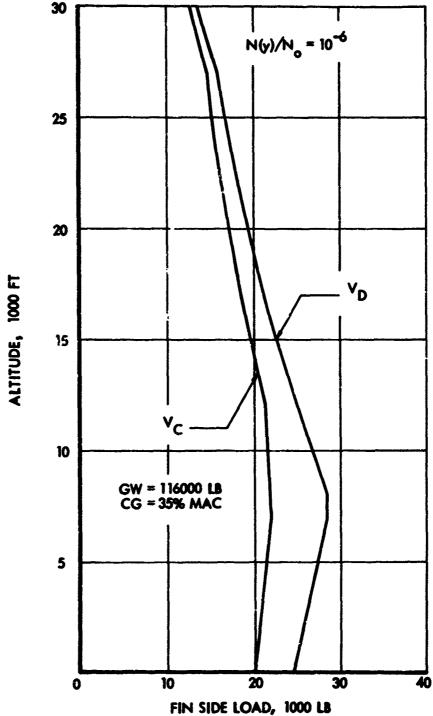


FIGURE 9-17. VARIATION WITH ALTITUDE OF FIN SIDE LOAD AT EXCEEDANCE RATIO  $N(y)/N_0 = 10^{-6}$ , MODEL 188

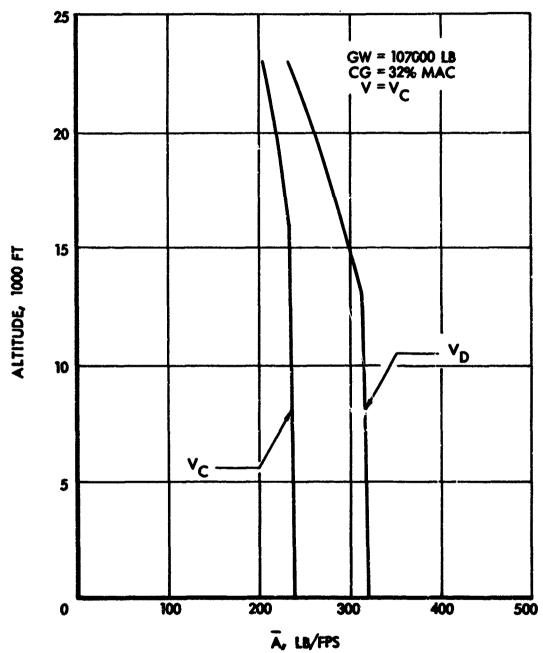
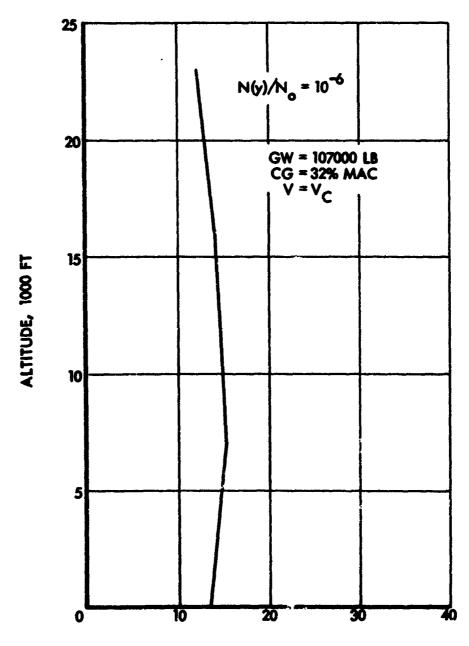


FIGURE 9-18. VARIATION WITH ALTITUDE OF  $\overline{A}$  FOR SIDE LOAD ON VERTICAL TAILS. MODEL 749



LOAD ON VERTICAL TAIL, 1000 LB FIGURE 9-19. VARIATION WITH ALTITUDE OF SIDE LOAD ON VERTICAL TAILS AT EXCEEDANCE RATIO  $N(y)/N_o = 10^{-6}$  MODEL 749

## 10 DESIGN TECHNIQUES - INTRODUCTORY DISCUSSION

In the analysis of the reference airplanes, described in Sections 6 through 9,  $\bar{A}$  and  $N_0$  values were obtained for loads at a large number of locations in the airplanes, and frequency of exceedance curves were obtained for these loads. In the design of a new airplane, results would be obtained in similar form. With the specification of a design level as discussed in Section 15 - design values of these same load quantities would follow at once. These would be obtained - depending upon the form of criterion - either by reading values from the exceedance curves at a design frequency of exceedance, or by multiplying the various  $\bar{A}$  values by the design value of  $\sigma_W \eta_d$ .

At this point, it might be expected that to apply these loads in design and stress analysis would be quite straight forward. The loads defined as described above would be plotted vs wing station, and stress analysis would proceed in the usual way. Unfortunately, however, in actual flight through turbulence, these design-level loads do not all occur simultaneously. As a result, the conditions defined by the simple plots just described can be quite meaningless as a basis for stress analysis. In what proportions the various design-level loads combine - or, as it might be put, how they are phased - remains undetermined.

For example, design-level values of transverse shear and of torsional moment at a given wing station are known. But these are essentially root-mean-square values, without sign. It is not known whether maximum up whear combines with maximum nose-up torsion, or with some intermediate value. If maximum up shear combines with maximum nose up torsion, the shear flows add in the front beam and subtract in the rear beam; if maximum up shear combines with maximum nose down torsion, on the other hand, the shear flows add in the rear beam.

Similarly, it is not known whether design-level shears and bending moments occur simultaneously at all wing stations. Nor is it known whether the shears integrate to give the bending moments. If not, existing stress analysis techniques may well be unusable. In the "unit beam" method, for example, the determination of shear flows does not utilize the familiar "VQ/I" formula. Instead, flange axial loads at various wing stations are first determined, by means of the My/I relation, and differences in axial load at adjacent wing stations are then used to establish the panel shear flows. Clearly, this method cannot be used unless the shears and the bending moments at adjacent stations occur simultaneously. Further, if the shears do not integrate to give the bending moments, no single set of panel loads can be found that could be applied to duplicate the condition in a static test. Here, then, is one of the major problems in applying power-spectral methods to practical detailed stress analysis. Statistically defined loads at a limited number of locations are

available. By what techniques can these loads now be utilized - or what other statistically defined quantities can be used in their place - to establish margins of safety at the many required locations throughout a wing or other major airplane component? The problem might be referred to more briefly as the integration of the power-spectral loads determination with the routines of detailed stress analysis, or, in still more abbreviated form, as the determination of a design technique.

As indicated by the above discussion, the essence of the problem is the establishment of the phasing of two or more load quantities. The term "phasing", incidentally, is used in this context and, in fact, throughout this report, not strictly in accordance with its usual exact definition. The terms "phase" and "phasing" are usually used to denote the angle by which a pure sinusoid leads or lags another pure sinusoid of the same frequency. The phase angle, however, also establishes pairs of simultaneously occurring values of the two variables. For example, if

 $x = 3 \sin \omega t$ and  $y = 2 \sin (\omega t - 45^{\circ}),$ 

then simultaneously occurring combinations of x and y are given by the ellipse shown on the "phase-plane" plot of Figure 10-1(a). It is seen that, as a result of the 45-degree phase difference between the two variables, the maximum value of y occurs only in combination with a reduced value of x, and the maximum value of x, only with a reduced value of y.

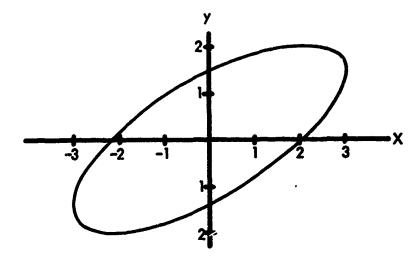
If x and y are now random variables - such as airplane loads in turbulence - the above definition of phase has no meaning, as the two variables are no longer pure sinusoids. There will still be a tendency, however, as illustrated in Figure 10-1(b) for the "maximum," or "equal probability," or "design level" values of the two variables not to occur simultaneously. The term "phasing", as used herein, relates to this tendency. More specifically, it implies a set, or sets, of factors that must be applied to design level values of two or more loads to give statistically appropriate combinations of these loads. Thus the term "unphased loads", would apply to the design level values of shear, moment, and torsion individually. "Phased loads" would be these values as modified by application of appropriate "phasing factors" to provide a statistically appropriate combination.

In attacking the phasing problem, either of two routes might be followed.

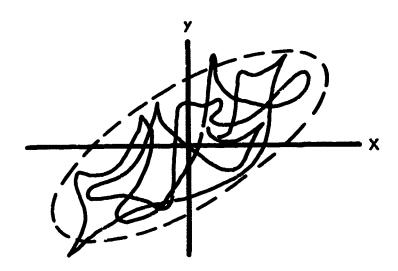
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BERKEY CERTAINS



(a) EQUAL FREQUENCY SINUSOIDS



(b) RANDOM VARIABLES
FIGURE 10-1. ILLUSTRATIVE PHASE PLANE PLOTS

One involves specific analysis of local areas of the structure. To obtain a correct shear flow, for example, the design-level values of shear and torsion are ignored, and the design-level value of the desired shear flow is determined directly. The shear flow - at each point of interest in the structure - is expressed as a linear combination of the shear, torsion, and bending moment acting at the wing section:

$$q = a S_z + b M_x + c M_y$$

This relation is introduced into the dynamic analysis with phase relations preserved, to give a transfer function for q. This, like the transfer functions for other load quantities, is multiplied by the gust power spectral density, giving a power-spectral density of q, which is then integrated to give the  $\bar{\rm A}$  and  $N_{\rm O}$  values.

By this procedure, design-level values of stresses at all desired locations throughout the structure can be determined.

The phasing problem, however, has only been deferred, rather than solved. Many structural elements are stressed simultaneously by both shear and axial stress, with limit or ultimate strength defined by "interaction curves" or "strength envelopes." The effect of phasing of the shear and axial stresses must, therefore, still be accounted for.

Statistical techniques are available for this purpose. These are developed and applied in Reference 1.

Under the design envelope form of criterion, when using these statistical techniques, it is found necessary to replace a single quantity,  $\sigma_{\rm W}\eta_{\rm d}$ , with values of  $\sigma_{\rm W}$  and  $\eta_{\rm d}$  individually. The joint probability density of the axial and shear stresses is determined analytically for the specified  $\sigma_{\rm W}$ ; a typical result is illustrated in Figure 10-2. The volume under the joint probability density surface outside the strength envelope - the part not shown in Figure 10-2 - is then the probability that the design strength is exceeded. A design value of this probability is then specified, equal to that associated with the design value of  $\eta_{\rm d}$ .

Under the mission analysis form of criterion, N(y) is redefined as the number of positive slope crossings of the strength envelope, rather than of a given value of a single load quantity.

These two procedures, because of their intimate dependence upon the joint probability functions, are referred to collectively, in this report, as the "joint probability technique."

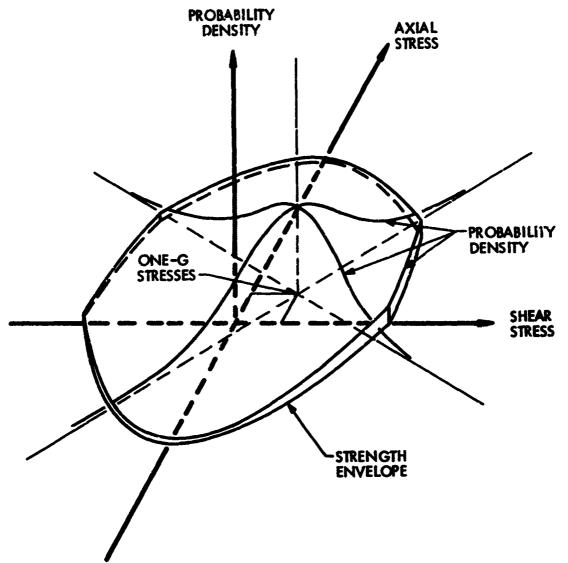


FIGURE 10-2. ILLUSTRATIVE JOINT PROBABILITY DENSITY FUNCTION AND STRENGTH ENVELOPE

An alternate route that might be followed in attacking the phasing problem involves the generation of specific design conditions that closely envelope the statistically defined loads. In order to properly phase the shear, bending moment, and torsion at each wing station, design level values of a limited number of internal stresses are also obtained. To phase the shear and torsion, for example, front and rear beam shear flows are included in the power-spectral analysis. Design combinations of shear and torsion are then established such that the resulting front or rear beam shear flow is just equal to its statistically defined design-level value.

This technique will be designated, in this report. the "matching condition" technique.

Both the matching condition and joint probability techniques are believed to offer entirely acceptable approaches from the standpoint of worthiness requirements. There may be a rather sizeable analysis he and cost advantage of one over the other; but which way this advantage would lie, and by how much, cannot be concluded with assurance at this time. The particular background and capabilities of the engineering organization involved could have a sizeable effect on the result of any such comparison.

Consequently, both approaches are developed at some length in the present study.

The matching condition technique is developed in Section 11. It is applied, for illustration, to the Model 188 wing and fuselage in Appendices C and D.

The joint probability technique is developed in Reference 1 and is applied therein to the Model 720B wing, fuselage, and vertical tail.

Some of the practical considerations that might be involved in making a choice between these two techniques are discussed in Section 12.1.

Each of the two techniques implies certain assumptions as to design philosophy. To assure consistency in application of the two techniques, these assumptions are explored in Section 12.2. How to obtain equivalent design levels under the two techniques is then discussed more explicitly in Section 12.3, and, in Section 12.4, both techniques are applied, for comparison, to a given location in the Model 720B wing.

## 11 THE MATCHING CONDITION TECHNIQUE

## 11.1 Basic Approach

A brief preview of the matching condition technique was given in the preceding section. Before actual cases are carried through for illustration, however, the concepts underlying the technique will be discussed more fully and the actual steps will be outlined in general terms.

In outlining the steps to be followed, it will be assumed that wing loads are to be determined for a straight-wing airplane with a single-cell, two-spar wing structure. It would appear, however, that the method could be applied almost without change to a swept wing and to multi-spar construction. It is believed that the same principles can be applied also to a low aspect ratio wing, although the details of the procedure would differ, as discussed in Section 16. The changes involved in extending the technique to fuselage and empennage loads would be primarily in the nature of simplifications, with the general approach remaining quite comparable.

It will also be assumed that the loads determination is for a new airplane. Thus it is presumed that design values of frequency of exceedance or of  $\sigma_w$   $\eta_d$  have already been established. For application to the reference airplanes, where the purpose is to establish limit-strength values of frequency of exceedance and  $\sigma_w$   $\eta_d$ , the same procedure would be followed. However, at least in principle, the analysis would have to be carried out at two different frequency of exceedance or  $\sigma_w$   $\eta_d$  values in order to interpolate to the zero margin of safety level. Also, in application to the reference airplanes, short cuts may be possible as a result of knowing which regions of the wing are likely to be critical.

The procedure is then as follows:

- By means of the power-spectral analysis, obtain design values of shear (S), bending moment (M), and torsion (T), at from 6 to 10 wing stations. Similarly, obtain design values of front and rear beam shear flows (q<sub>Tb</sub> and q<sub>Tb</sub>) at some or all or these wing stations. These "design values", if based on a mission analysis, are values occurring at the design frequency of exceedance. If based on a design envelope analysis, they are values of Ā x σ<sub>W</sub> η<sub>d</sub>.
- 2. Establish several say three "unit," or "elementary," spanwise distributions of shear, bending moment, and torsion. These might consist of the following:

- (1) Incremental loads due to a statically applied gust or a maneuver.
- (2) Loads due to inertia forces and displacement-dependent aerodynamic forces in the first elastic mode. If natural modes are used as generalized coordinates, these loads can be obtained directly from the model data. If arbitrary deflection shapes are used as generalized coordinates, the shape of the first elastic mode must be determined from values of the appropriate transfer functions at the first elastic mode frequency.
- (3) Loads due to inertia forces and displacement-dependent aerodynamic forces in the second elastic mode. These can be obtained in the same way as those for the first elastic mode.

These three distributions, or sets of loads, can be at any arbitrary level.

Designate these elementary distributions the  $E_1$ ,  $E_2$ , and  $E_3$  distributions, respectively. Designate the shears, moments, and torsions in the  $E_1$  distribution  $S_{E_1}$ ,  $M_{E_1}$ , and  $T_{E_1}$ , where, of course, each of these three loads will have different values at the various wing stations. Designate the loads in the other distributions similarly.

Compute for each distribution front and rear beam shear flows -  $q_{fbE_1}$ ,  $q_{rbE_2}$ ,  $q_{rbE_2}$ ,  $q_{fbE_3}$ , and  $q_{rbE_3}$ . These will be obtained at the wing stations where statistically defined values of the shear flows are obtained in Step 1.

3. By trial and error, using the  $E_1$ ,  $E_2$ , and  $E_3$  distributions as building blocks, generate several design conditions such as to match, or envelope closely, the statistically defined loads, including shear flows, obtained in Step 1.

Any single design condition will be defined by a certain amount,  $a_1$ , of the  $E_1$  distribution, plus a certain amount,  $a_2$ , of the  $E_2$  distribution, plus a certain amount,  $a_3$  of the  $E_3$  distribution. Thus for this one design condition,

$$S = a_1 S_{E_1} + a_2 S_{E_2} + a_3 S_{E_3}$$

$$M = a_1 M_{E_1} + a_2 M_{E_2} + a_3 M_{E_3}$$

$$T = a_1 T_{E_1} + a_2 T_{E_2} + a_3 T_{E_3}$$

Other conditions are defined by other sets of values of the coefficients  $a_1$ ,  $a_2$ , and  $a_3$ .

The superposition of elementary distributions to generate design conditions is exactly analogous to a procedure often used in static wing loads determination, in which the net loads are obtained by a superposition of various distributions such as an "additional" lift distribution, a "basic" lift distribution, an  $\mathbf{n}_{\mathbf{z}}$  inertia distribution, a pitch inertia distribution, various aeroelastic distributions, etc. Adopting the nomenclature sometimes used in the static loads determination,  $\mathbf{S}_{\mathbf{E}_{1}}$ , for example, would become (S/a\_1), the E\_1 distribution would be called simply the a\_1 distribution, and the above equations would be written:

$$S = \left(\frac{S}{a_1}\right) a_1 + \left(\frac{S}{a_2}\right) a_2 + \left(\frac{S}{a_3}\right) a_3$$

$$M = \left(\frac{M}{a_1}\right) a_1 + \left(\frac{M}{a_2}\right) a_2 + \left(\frac{M}{a_3}\right) a_3$$

$$T = \left(\frac{T}{a_1}\right) a_1 + \left(\frac{T}{a_2}\right) a_2 + \left(\frac{T}{a_3}\right) a_3$$

Ordinarily, no single condition can be obtained that will match all of the statistically defined loads. Consequently, several conditions will be required. One, for example, may match the shears, bending moments, and shear flows but contain lower torsions than the statistically defined design values; another may match the torsions and shear flows but contain lower shears and bending moments than required. Together, however, the two will envelope - closely - all of the statistically defined values. Or one such pair of conditions may envelope closely the loads in the inboard portion of the wing but be lower than required in the outer wing. This pair of conditions would then be complemented by a second pair that match closely the loads in the outer wing but are lower than required in the inboard region.

To illustrate how such an approach leads to realistic phasings of shear and torsion at a given wing station, reference is made to a typical shear-torsion plot as shown in Figure 11-1. Only combinations of positive (up) shear and positive (rose up) torsion are shown, the same

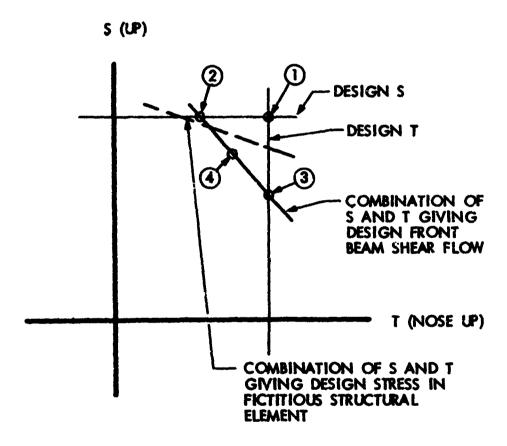


FIGURE 11-1. ILLUSTRATIVE SHEAR-TORSION PLOT

reasoning, however, will also apply to the remaining three quadrants. The design magnitudes of shear and torsion are shown by horizontal and vertical lines in the figure. The diagonal line represents the various combinations of shear and torsion that result in the design magnitude (per Step 1) of front beam shear flow.

Ordinarily, a single design condition containing the design magnitudes of both shear and torsion - that is, treating these as occurring simultaneously - will result in a front beam shear flow considerably in excess of the design value established in Step 1. Such a condition is represented by Point 1 in the figure. To avoid an overly conservative design, it is clearly necessary to reduce either the shear or the torsion or both. Any of Points 2, 3, or 4 will accomplish this purpose, as each results in the correct value of shear flow. However, the front beam shear web is only one element of a complex structure. Other lements may be stressed predominantly as a result of shear or bending

ements may be stressed predominantly as a result of shear or bending ant alone (these tending, probably, to be closely in phase), or saidly by torsion alone, or perhaps by interaction of shear flow and anding moment. Consequently, it appears appropriate that design conditions be selected to include Points 2 and 3. The first condition then matches shear (and, simultaneously bending moment) and shear flow, and the second matches torsion and shear flow. Together, the two conditions envelope closely all three load quantities at the given wing station. Actually, even Point 2 may be slightly conservative. However, it is far less conservative than Point 1, and any remaining conservatism probably has a rather negligible effect.

In establishing values of a<sub>1</sub>, a<sub>2</sub>, and a<sub>3</sub> to define each of the various design conditions, the relative amounts of shear and torsion at various wing stations are controlled by the relative values of a<sub>1</sub>, a<sub>2</sub>, and a<sub>3</sub>. For the Model 749 and Model 188, for example, it has been found that the static distribution contains relatively little torsion, whereas the elastic mode distributions contain sizeable torsions. Point 2, therefore, would result from a condition in which the static distribution predominates. Such a condition would be produced by an attempt to match shear, bending moment, and shear flow simultaneously. Point 3, similarly, would result from a condition in which one or more of the elastic mode distributions predominates. Such a distribution would be produced by an attempt to match torsions and shear flow simultaneously.

In matching design-envelope loads, it seems quite likely that about three elementary distributions, as employed in the above discussion, might suffice. (Each point of the design envelope, however, might require a different set of distributions.) In matching mission analysis loads, on the other hand, more unit distributions are likely to be required. The one-g level flight loads are now included in the statistically defined loads, so that at least one one-g or zero-g condition

will have to be included in the unit distributions to cover the so-called "basic" distributions due to built-in wing twist,  $C_{m_O}$ , aero-elastic effects at zero-g etc. Also, the statistically defined loads reflect contributions from various mission segments at a variety of speeds, altitudes, and especially fuel weights; consequently unit distributions based on more than one weight condition may be required.

It should be remarked that the  $E_1$ ,  $E_2$ , and  $E_3$  distributions can be quite arbitrary; the only requirement is that the resulting design conditions match the statistically defined loads to the desired degree of accuracy. If the  $E_1$ ,  $E_2$ , and  $E_3$  distributions do not provide an adequate match, they can be modified as necessary, or the resulting conditions can be modified arbitrarily. The latter is probably to be preferred, and can be looked upon as adding in a small amount of some additional, highly simplified distribution.

At the same time, there is a stainet advantage in starting with fairly reasonable distributions. In flying through turbulent air, an airplane responds statically to the low frequency components of the turbulence (long gradient gusts) and it responds dynamically in its various elastic modes to the higher frequency components of the turbulence. The two types of response - the static and the dynamic - generally have quite different distributions of load throughout the structure. Moreover, each elastic mode will have its own distinctive load distribution. In flight through typical turbulence there is a random interplay amongst these various distributions. It would appear that use of the actual distributions associated with motions in the various modes would lead most readily to a match with the statistically defined loads. More important, since the statistically defined loads are available at a fairly limited number of locations, the use of rational unit distributions tends to assure a realistic definition of stresses at the intermediate locations.

## 11.2 The Ficticious Structural Element Concept

In the previous section, proper phasing of torsion with shear or bending was dependent upon matching shear flows in the front and rear beams, and it was necessary to assume that the shear and bending moment would be in phase. Fortunately, an additional tool is available that broadens immeasureably the technique for establishing realistic phasings. This tool is the concept of a ficticious structural element.

It will be recalled from the previous discussion that design combinations of shear and torsion at a given wing station are established so that the resulting front beam shear flow matches its statistically defined value. This was illustrated by Figure 11-1. It was noted that

Point 1 would obviously be conservative as a design point, since the resulting front beam shear flow would be well in excess of the statistically defined value. Point 2 on the other hand would be a realistic design point, probably only very slightly conservative. This point gives the right shear and bending moment (these being assumed in phase) for whatever structural elements are not influenced by torsion, and also the right beam shear flow. Also, however, it gives about the right combination of bending and torsion for design of the upper and lower surfaces midway between front and rear beams. Thus the front beam is seen to serve as an indication of phasing to be applied at another location altogether.

This fact suggests that, for the purpose of establishing phasing, there is no need that a real front beam be present at all. For example, suppose it is desired to see how conservative Point 2 actually is. The shear flow in the real front beam might have been given by

$$q_0 = .014 S + .00020 T$$
 (11-1)

Now suppose we imagine a fictitious structural element such that its stress is given by

$$q_1 = .014 S + .00010 T$$
 (11-2)

- i.e., one that is relatively less sensitive to torsion. The statistically defined load for this element is determined in the same way as for the real front beam - that is, by including in the dynamic analysis the determination of its transfer function, power-spectral density,  $\bar{A}$  and  $N_{\rm O}$ . The dash line in Figure 11-1 represents combinations of S and T that give a value of stress equal to the statistically defined value in this fictitious element. (The dash line is defined by substituting the statistically defined value of  $q_{1}$  in Equation 11-2 and plotting S vs T.) In this case it is seen that Point 2 actually would be slightly conservative; if the fictitious element were actually there, its stress at Point 2 would be higher than defined statistically, precluding Point 2 as a valid design point.

Similarly, by defining a series of fictitious structural elements, employing a series of ratios of the coefficients in the expression of q, a complete design load envelope could be established.

Such an envelope has been computed for shear-torsion of the Model 188 wing at W.S. 83 and is shown in Figure 11-2(a). Only the increments over and above the 1-g load are shown; and the contribution of bending moment to the stress in the fictitious element has been assumed to be zero. The points labelled Condition I, Condition II, etc., on the figure are design conditions generated in Appendix C and can be disregarded for the present.

The solid lines in Figure 11-2(a) clearly circumscribe a figure of roughly elliptical shape which can be regarded - at least intuitively and without precisely defining the term - as a curve of equal probability.

In obtaining this figure, as can be seen, it was necessary to utilize 10 fictitious structural elements, in addition to the two already inherently available - i.e., those that sense shear only and torsion only. The coefficients a<sub>1</sub> and a<sub>2</sub> in the expression

$$q = a_1 S + a_2 T$$

were selected so that

$$\frac{a_{2}}{a_{1}} = 0.2 \frac{\bar{A}_{S}}{\bar{A}_{T}}, 0.5 \frac{\bar{A}_{S}}{\bar{A}_{T}}, 1.0 \frac{\bar{A}_{S}}{\bar{A}_{T}}, 2 \frac{\bar{A}_{S}}{\bar{A}_{T}}, 5 \frac{\bar{A}_{S}}{\bar{A}_{T}}$$

$$-0.2 \frac{\bar{A}_{S}}{\bar{A}_{T}}, -0.5 \frac{\bar{A}_{S}}{\bar{A}_{T}}, -1.0 \frac{\bar{A}_{S}}{\bar{A}_{T}}, -2 \frac{\bar{A}_{S}}{\bar{A}_{T}}, -5 \frac{\bar{A}_{S}}{\bar{A}_{T}}$$

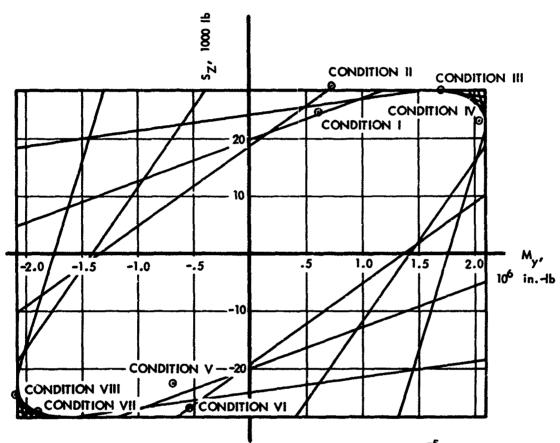
respectively.

The same procedure can now be used to test the assumption that shear and bending moment are in phase. The results for Wing Station 83 of the Model 188 are shown in Figure 11-2(b). It is quite clear that the assumption is an excellent one, as the "equal-probability" ellipse is indeed a very narrow one and its corner occurs virtually at the intersection of the maximum  $S_z$  and maximum  $M_x$  lines.

The same procedure has also been applied to examine the phasing of the remaining pair of quantities, bending and torsion. The result is shown in Figure 11-2(c). This figure is approximately geometrically similar to the shear torsion envelope, Figure 11-2(a), as expected in view of the shear bending phase relation depicted in Figure 11-2(b).

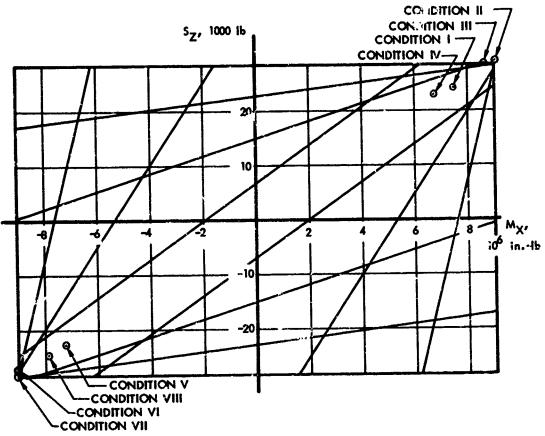
A similar set of figures applicable to Model 188 Wing Station 346, between the nacelles, is shown in Figures 11-2(d) - (f). Here the shear and bending moment are seen to be less closely in phase, but still closely enough for the in-phase assumption to lead to fairly realistic design loads.

Corresponding figures for the Model 749 are shown in Figures 11-3(a)-(f). These are generally similar to those for the Model 188. The dash lines on the figure are for the actual front and rear beam webs as structural elements, with the contribution of bending moment to the



NOTE: CURVES ARE MISSION ANALYSIS CASE 202 AT N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

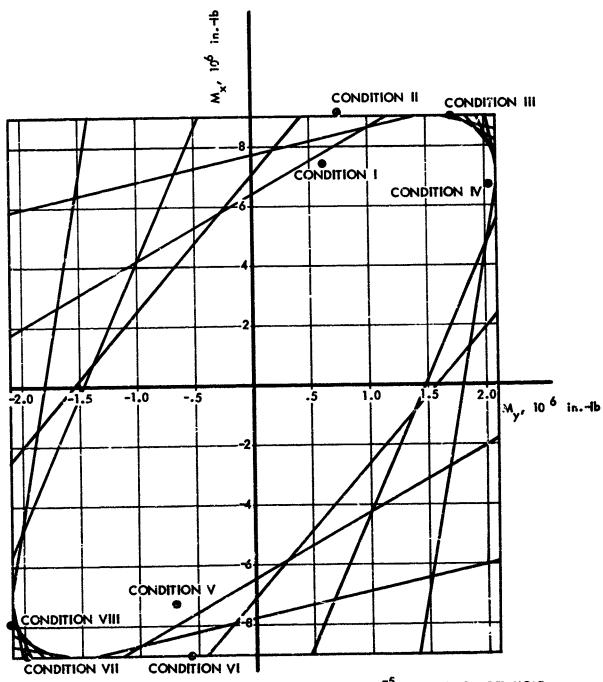
(a) WS 83, SHEAR-TORSION
FIGURE 11-2. "EQUAL FROBABILITY" ENVELOPES, MODEL 188



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NOTE: CURVES ARE MISSION ANALYSIS CASE 202 AT N(y) =  $10^{-5}$  EXCEEDANCES PER HOUR

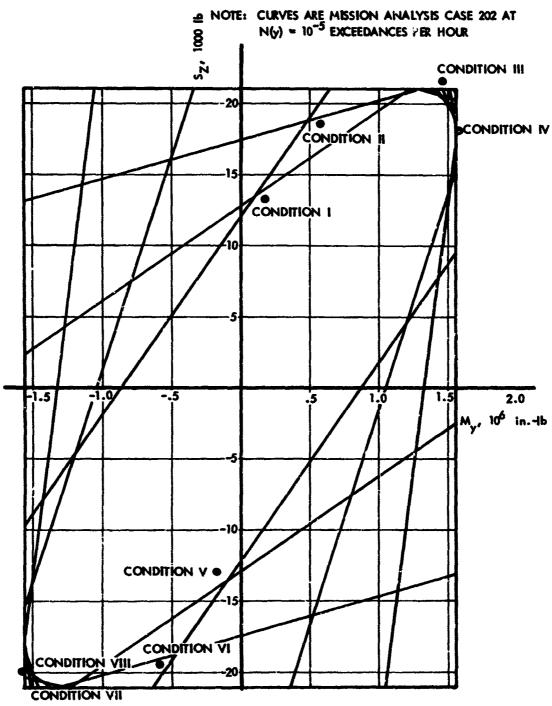
(b) WS 83, SHEAR-BENDING FIGURE 11-2, CONTINUED



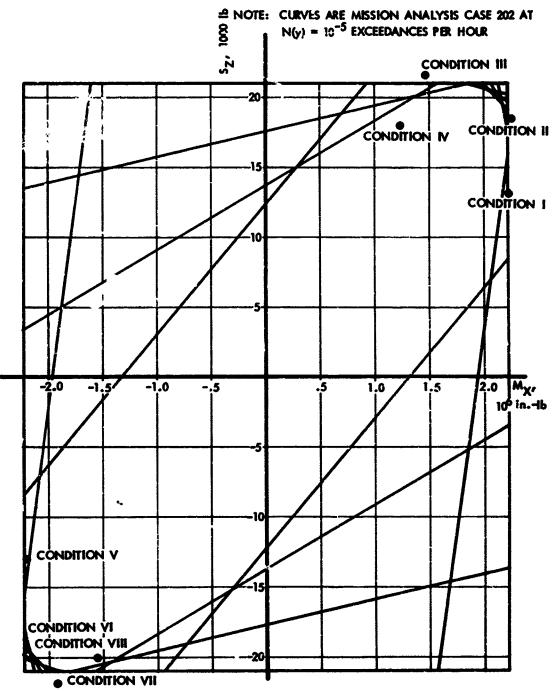
NOTE: CURVES ARE MISSION ANALYSIS CASE 202 AT N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(c) WS 83, BENDING-TORSION

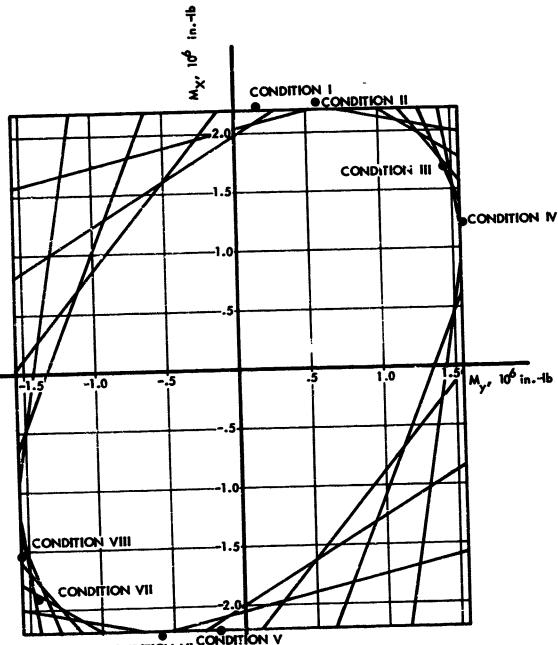
FIGURE 11-2, CONTINUED



(d) WS 346, SHEAR-TORSION FIGURE 11-2, CONTINUED



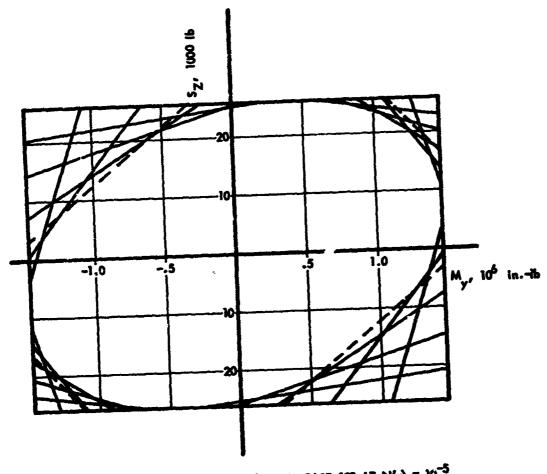
(e) WS 346, SHEAR-BENDING FIGURE 11-2, CONTINUED



CONDITION VI CONDITION V

NOTE: CURVES ARE MISSION ANALYSIS CASE 202 AT N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(f) WS 346, BENDING-TORSION FIGURE 11-2, CONCLUDED



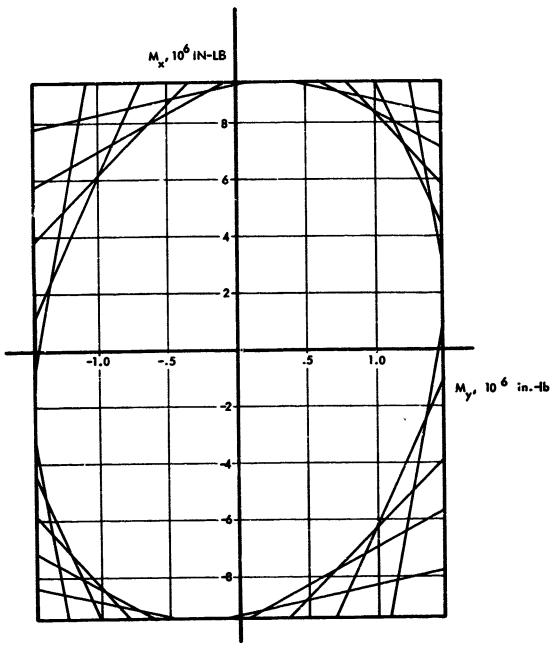
NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(a) WS 103, SHEAR-TORSION
FIGURE 11-3. "EQUAL PROBABILITY" ENVELOPES, MODEL 749

S<sub>Z</sub>, 1000 lb

NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT  $N(y) = 10^{-5}$  EXCEEDANCES PER HOUR

(b) WS 103, SHEAR-BENDING FIGURE 11-3, CONTINUED

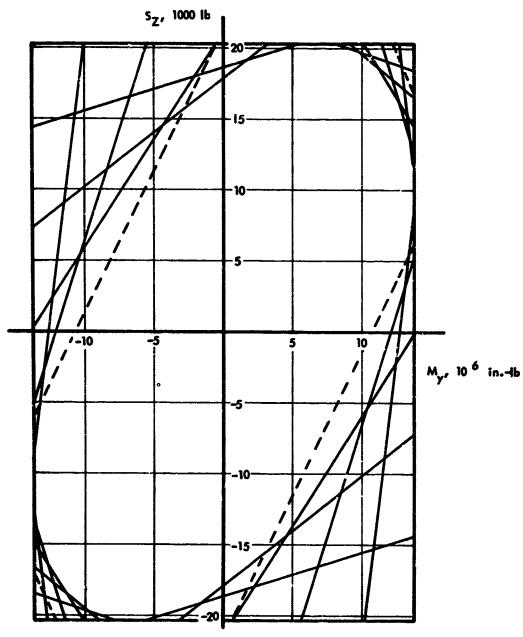


NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT

N(y) = 10<sup>-5</sup> EXCEEDANCES FER HOUR

(c) WS 103, BENDING-TORSION

FIGURE 11-3, CONTINUED

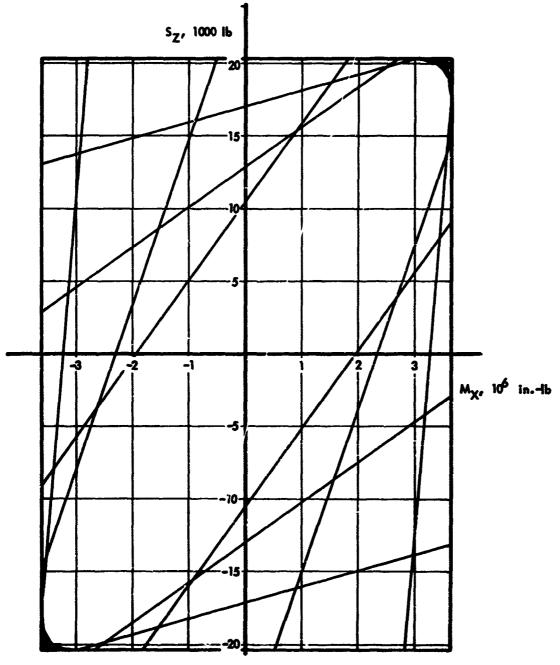


NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT

N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(d) WS 337, SHEAR-TORSION

FIGURE 11-3, CONTINUED

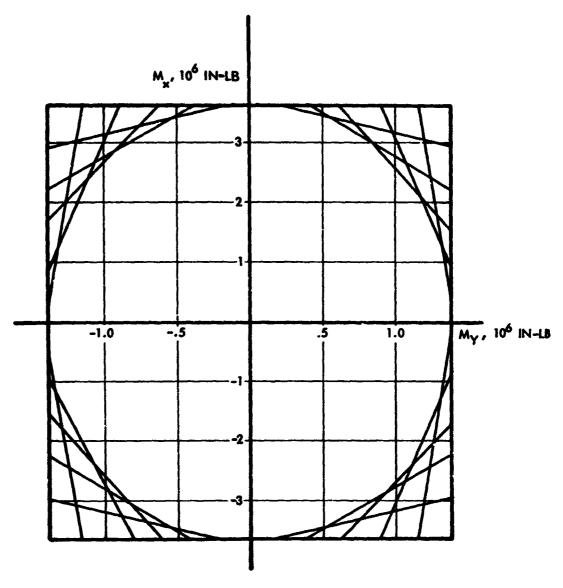


NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT

N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(e) WS 337, SHEAR-BENDING

FIGURE 11-3, CONTINUED



NOTE: CURVES ARE FOR MISSION ANALYSIS CASE 102 AT

N(y) = 10<sup>-5</sup> EXCEEDANCES PER HOUR

(f) WS 337, BENDING-TORSION

FIGURE 11-3, CONCLUDED

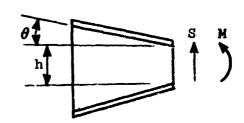
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shear flows included. In drawing the dash lines, the combinations of shear and torsion necessary to give the statistically defined shear flow are obtained on the assumption that bending moment is present equal to  $(\bar{A}_M/\bar{A}_S)S$ .

Reviewing the entire set of figures, the resemblance to ellipses is striking. In fact, to within the accuracy to which a graphical check can be relied upon, the figures are indeed ellipses. However, no analytical substantiation has been attempted. One might speculate that the figures are indeed true ellipses when obtained on a  $\sigma_w$   $\eta_d$  basis, but that differences in  $N_0$  for the various elements might create a slight distortion when the figures, as here, are obtained on an N(y) basis.

It should be emphasized that this technique does not depend at all on the presence of any actual structural component that might sense a linear combination of the two load quantities involved. But for the reader who might feel more comfortable if he could visualize such an element, examples can usually be invented. In the case of combined shear and bending, for example, one might consider the shear in the web of a sharply tapered I beam:

$$S_{\text{web}} = S - 2 \frac{M}{h} \tan \theta$$
$$= 1.00 S - \frac{2 \tan \theta}{h} M$$



Nor does the actual shape of the allowable stress interaction curve enter into consideration. We are dealing with applied loads only, and introduce the fictitious structural element only to provide information about the applied loads.

It is of interest to note that the two-dimensional treatment illustrated in Figures 11-2 and 11-3 could be immediately extended to three dimensions. In this case, an ellipsoid would be defined by superscribing planes. The three-dimensional treatment would appear to be too cumbersome, however, for practical use.

It might also be noted, however, that the fictitious structural element approach can be applied to stresses at a point in the structure, as well as to loads. Here the fictitious structural element would be one having

various relative sensitivities to axial and shear stresses at a point, rather than to external shear, moment, and torsion. It would appear that applying the approach in this way could be very useful in those situations where the shear and bending moment are found not to be closely in phase. The technique might be used to test design conditions for proper combination of shear, moment, and torsion. Or, if desired, it could be applied in somewhat the same manner as the joint probability approach, with no attempt made to develop consistent conditions over the entire wing. In this case, the advantage would lie in a possibly closer theoretical relationship to past design philosophy, as will be brought out more fully in Section 12.

In the practical application of the ficticious structural element concept, it may be found advantageous to eliminate the actual definition of ficticious elements and the calculation of A and No values for the stresses in these elements. Instead, each "equal probability ellipse" would be generated as an equal probability density contour utilizing the correlation coefficient,  $\rho$ , between the two load or stress quantities of interest. Computation of the correlation coefficient can readily be included in the dynamic analysis, using Equation B-13 of Reference 1; the ellipse is then defined by Equations B3a and B3b of Reference 1 at a suitable constant value of the probability density. The value of probability density to be used is that which brings the ellipse tangent to the straight line representing the design value of one of the load quantities of interest.

#### 11.3 Illustration of the Matching-Condition Technique

The use of the matching condition technique is illustrated in Appendices C and D by applying the technique to the generation of wing and fuselage loads for the Model 188.

In these illustrations, it is assumed that a very close match is desired, in order to avoid unnecessary conservatism in the resulting design loads. (In the case of the wing, since the resulting conditions are used in establishing limit and ultimate strength values of N(y) and  $\sigma_{\rm w}\,\eta_{\rm d}$  for the Model 188 as reference airplane, a close match is particularly necessary.) As a result, considerable care was taken to obtain a good match. The procedures followed are described and illustrated in some detail, in order to provide a useful guide to the engineer actually making such an application for the first time. The reader interested only in an over-all view of the procedures will find parts of the discussion that need not be followed thoroughly on the first reading. Section C.3, especially, would fall in this category.

## 12 MATCHING CONDITION AND JOINT PROBIBILITY TECHNIQUES - DISCUSSION

### 12.1 Practical Considerations in Selecting a Design Technique

Both the matching condition and joint probability techniques have been applied in this study. The matching condition technique is illustrated by application to the Model 188 in Appendices C and D, and the joint probability technique by application to the Model 720B in Reference 1. Each has been demonstrated to be practical for design use.

In the course of making these applications, various considerations pertinent to making a choice between the two techniques in any given case have become evident. These are discussed in the following paragraphs. The considerations noted are primarily of a practical nature. From the standpoint of rationality, there is probably little to choose; and numerical results, in the nature of structural sizes required to maintain zero or positive margins of safety, will be very nearly the same for both techniques. Differences in rationality between the two techniques are important more for the purpose of assuring a consistency in application between the two and are discussed more fully in Sections 12.2 through 12.4.

First, some practical consequences of selecting the joint probability techniques will be noted.

First, this technique requires that, potentially, every minute element of structure be carried through the power-spectral analysis. Unless simple and reliable means can be deviced to establish which elements are critical prior to making the analysis, the amount of computation can become prohibitive. Consequently, this technique would probably find use only in the final stages of design and analysis, and even then, care would be required to keep the amount of work within reasonable limits. Certainly where the airplane can be shown by simpler means not to be gust critical, the joint probability analysis would not be undertaken. It might be noted, incidentally, that, if the joint probability technique is to be used only in the final stages of design, a switch-over at some point will be required from a one-dimensional, or matching condition, point of view to a joint probability point of view. It would appear that some increased chance for confusion would result.

Second, when the joint probability technique is used, "design conditions", each consisting of an individual, consistent set of loads on an airplane component, are no longer defined. The concept of a design condition has long permeated the entire art of structural analysis. Inasmuch as the various design loading conditions are relatively uninfluenced by changes in the structure, it has been possible to keep the loads

determination function quite distinct from the structural design and stress analysis function. Design and optimization of the structure are thus facilitated. The usual refinements in the stress analysis methods as the design progresses are easily accommodated. And refinements in the load determination can proceed independently of those in the stress analysis. Salvage may be expedited. Thus the abandonment of the design condition philosophy could well introduce complexities into the design procedure; some of these are apparent and there may be others that will appear only as experience is gained with the new approach.

Furthermore, regardless of which technique is used for design and stress analysis, complete, consistent conditions will still be required for static and fatigue testing. Since the static test conditions must be generated eventually, it appears most expeditious to generate them in advance of the stress analysis stage. In addition, complete consistent conditions are needed for fatigue testing. While these would ordinarily be generated independently of the static test loadings, there is believed to be an advantage in developing both the repeated loads and limit design conditions according to the same general philosophy.

An interesting example of the difference in thinking required in using the joint probability technique is illustrated by Figure 12-1. This is essentially the same as Figure 10-2, except that it is redrawn in the form of contours of equal probability density. The heavy solid line shows a possible strength envelope for the particular element under consideration. If it were necessary to define a "critical" condition, one would have no hesitation in selecting, intuitively, point A. But now suppose that the structure were redesigned so as to reduce the compression allowable, resulting in the modified strength envelope shown by the heavy ash line. Neither the loading nor the allowable at the "critical" point are affected, yet the probability of exceeding the limit strength has been increased.

Turning next to the matching condition technique, it is apparent first that the generation of the enveloping conditions - although simple in concept - can easily grow to a rather sizeable task in practice, especially when a very close match to the statistically defined loads is considered necessary. The potential complexity of this approach is evident from the example presented in Appendix C.

Of more significance, application of the matching condition technique requires a considerable degree of judgment and skill - perhaps even ingenuity. And there may also be difficulty in ascertaining, for sure, when an adequate match has been achieved. A method that follows more rigorously and directly from basic principles would be more straightforward to apply and hence more acceptable for use by less-experienced personnel.

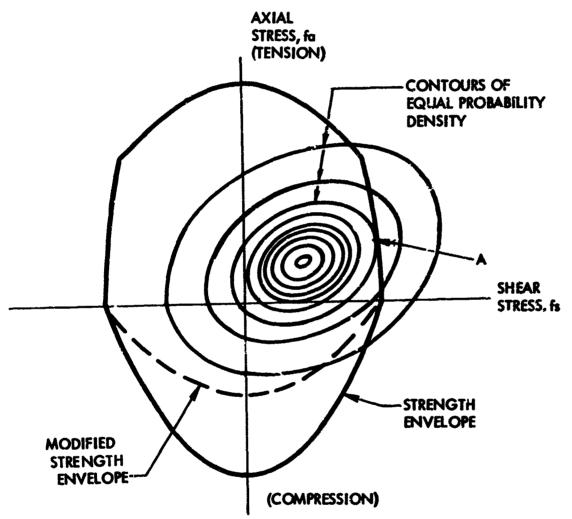


FIGURE 12-1. ILLUSTRATIVE JOINT PROBABILITY DENSITY FOR COMBINED STRESSES - TYPICAL STRENGTH ENVELOPE

These difficulties become particularly evident when realistic phase relations must be established considering simultaneously all three load quantities - shear, bending moment, and torsion. When appropriate simplifying assumptions can be made and substantiated - for example, that shear and bending moment are in phase - this problem does not arise. But otherwise, the approach can become extremely cumbersome. In contrast, when attention is focused on stresses at a point in the structure, the three load quantities combine to give just two stresses, axial (in the direction of the flange material) and shear.

At the same time, the generation of consistent design conditions is not believed to be prohibitively difficult. Certainly some leeway can be allowed in the precision to which the statistically defined loads are matched in the design conditions. Even without a perfect match, the loadings will be much more realistic in both level and distribution than provided by a static analysis, or even a discrete gust dynamic analysis. In fact, a vast improvement over a static gust design condition could be achieved quite handily, simply by comparing the static design condition with the statistically defined loads, adjusting the level up or down by a constant factor as indicated, and adding concentrated or distributed forces at a limited number of locations to introduce the major effects of the dynamic response. Or consider the design technique described in the introduction (pages 3 and 4), which was used successfully in a recent design substantiation. Design loads were first established by means of a discrete gust dynamic analysis. But what would have been done had the power-spectral analysis indicated a load increase to be necessary? For example, suppose an increase had been indicated in the wing torsion in the region between nacelles. Clearly, the design condition would have been "doctored up" by introducing an arbitrary pitching couple at the outboard nacelle and, if necessary, an opposite couple at the inboard nacelle. The result would have been a design condition that matched excellently the statistically defined loads. As a result, although there may remain some need for judgment in establishing just how good the match has to be, there seems to be little doubt that a satisfactory match can be obtained.

Furthermore, if there is serious doubt as to whether the enveloping conditions adequately reflect the phasing of the three load components, a limited number of fictitious structural elements can be introduced that sense appropriate combinations of all three load components. Or the fictitious elements can be introduced to define design combinations of axial and shear stress at critical locations in the structure.

# 12.2 Implications with Respect to Structural Design Philosophy; Rationality

In attempting to compare and evaluate the matching condition and joint probability techniques, it has been found that the two techniques will ordinarily yield numerical results that differ by some small amount. While this difference is not great enough to be significant from an airworthiness standpoint, it does give rise to the question of which technique is the more rational. In attempting to answer this question, it has become evident that the differences between the two techniques are not so much matters of rationality as of the structural design philosophy that each implies. In this section, emphasis is given first to identifying these differences in design philosophy. Some points concerning rationality are then brought out as the discussion proceeds. Background is thus provided for establishing the most consistent basis for use of the two techniques, both in comparing limit-strength levels of the Model 720B with the Model 188 and Model 749, and in new design.

12.2.1 Statistical Basis of Design Criteria. The objective of structural criteria can be regarded as the achievement of a satisfactorily low probability of exceeding design strength, either limit or ultimate, over some given period of time. This time might be an arbitrary period of operation such as one hour or 1000 hours, or one flight, or the life of one or more airplanes. In the present study, the design probability level, however it may be expressed, is to be established equal to that which has led to satisfactory safety records for currently operating transport aircraft.

It is inferred, of course, that the magnitude of structural loads to which an aircraft will be exposed can be described statistically. It is further inferred, moreover, that there is no absolute upper limit on the magnitude of loads that can be encountered. Some loads, to be sure, are inherently limited to a fairly well defined level. Braking loads, for example, are limited by the torque capacity of the brakes and by the tire-to-ground coefficient of friction. Maneuver loads are limited, at some level, by the wing or control surface forces aerodynamically attainable. But gust intensities have no known upper limit; maximum gust velocities continue to increase as more data are accumulated. Likewise, for modern transport aircraft at high speed, any aerodynamic limit on pull-up maneuver loads is at a level so far above the desired design strength as to be of no practical consequence. Similarly, there is no upper limit on the sinking speed that a pilot may inadvertently permit in a landing impact.

The concept of a "probability of exceeding design strength" is, of course, fundamental. Tet this expression is often used rather loosely, and various ambiguities arise when it is desired to interpret it exectly.

These ambiguities become particularly evident in attempting to compare the two design techniques developed herein. In the discussion that follows, some of these ambiguities will be brought to light, and the inference with respect to both design philosophy and validity of the methods will be examined.

12.2.2 The Concept of Independent Design Conditions. First, let us identify one important factor of current structural design philosophy. This is the concept that the many design conditions can be considered independently.

The probability of loss of an airplane in a given period of time - say 1000 hours - is, of course, the sum of the probabilities of its loss due to all causes.\* Thus the probability of loss of the airplane is approximately the sum of its probabilities of loss due to gust, maneuver, landing impact, etc. Certainly it is this overall probability of loss to which, ideally and rationally, the airplane should be designed.

But for many years it has been universal practice to accept a rather gross approximation to this ideal; each type of loading is considered individually, and no explicit attempt is made to consider the combined probability of occurrence of several types of load. For example, without assigning actual probability values, let us assume that gust and maneuver loads criteria are based on equal probabilities of exceedance of  $\text{desi}_\ell n$ load. If one airplane - say Airplane A - just meets the gust requirement but has great excess strength to withstand all other types of loading, then its overall probability of loss is approximately equal to its probability of loss due to gust alone. But now consider Airplane B. It likewise just meets the gust requirement, but in addition is equally critical for maneuver. Remote as the probability of loss may be in either case, there can be no doubt that the probability is twice as great for Airplane B as for Airplane A. To limit the probability of loss of Airplane B to that of Airplane A would require that the gust criteria be increased in severity whenever the maneuver loads are also critical.

Clearly, any attempt to adjust the level of design loads for a given condition according to how critical other conditions may be would be completely unmanageable in practice. To date, therefore, no attempt

<sup>\*</sup> Actually, this statement is true only approximately. More precisely, if the various probabilities are independent and are denoted  $p_1, p_2, \ldots$ , then the probability that the airplane is not lost is  $(1-p_1)(1-p_2)$ ..., and that it is lost is  $1-(1-p_1)(1-p_2)$ ... This, for small values of the p's, is approximately  $p_1+p_2+\cdots$ 

has been made to incorporate such a concert into structural criteria. Current criteria, however, can be regar. as approximating the objective of a fixed overall probability of exceedance; the degree of approximation depends upon how alike various airplanes are in the degree to which various conditions are equally critical.

12.2.3 Power Spectral Considerations - Idealized Airplane. Now let us consider what ramifications with respect to design philosophy may result from introducing power-spectral concepts into the gust loads determination.

First, consider the idealized case of a rigid airplane, free to plunge only, and short enough in overall length relative to the predominant gust wave length so that all points on the airplane can be assumed to encounter any given gust simultaneously. This idealized airplane does not necessarily represent any actual airplane, although it may be a fairly close approximation to airplanes of the DC-3 generation. Also, this idealization is essentially what has been assumed in determining design gust loads for many years.

For this idealized airplane, all loads are "in phase" and can be measured by a single quantity, the c.g. acceleration. As a result, no new problem of "design technique" enters. Once a design level of c.g. acceleration is established for a given airplane, based on a design probability of exceedance, all loads and stresses follow at once. The c.g. acceleration defines a total airload that is distributed in a particular way, and it also defines the inertia forces at all points in the structure. Consequently, when the c.g. acceleration reaches the value that corresponds to ultimate strength at some point in the structure, failure occurs. Only the "weakest link in the chain" is of interest. No matter how many other links may be equally weak, there will be no reduction in the c.g. acceleration at which failure will occur, nor will there be any increase in the probability that the design strength will be exceeded.

12.2.4 Power Spectral Considerations - Large, Flexible Airplane. For a large, flexible, dyramically responding airplane, however, the situation is more complex. Because of the random input and the partial independence of the responses in the many rigid and elastic modes, the stresses throughout the structure are not all in phase. The bending moment in the outer wing, the bending moment at the wing root, the load on an engine nacelle, and the loads in the fuselage forebody, for example, may all reach their maximum values at quite different times. Likewise, at any given wing station, the shear, bending moment, and torsion may reach their maximum values at different times. And even at a single

point within a given wing section, the shear and axial stresses may reach their maximum values at different times. Thus the many diverse stresses throughout the airframe, rather than following in direct proportion to the c.g. acceleration, tend to go their own individual ways. Now suppose that equal-probability design values are established for each of these many loads or stresses. Then in any given patch of turbulence - because of the random nature of the turbulence - one load, say load "A", might exceed its design value, while all others - B, C, D, etc. - remain below theirs. If at each point in the structure the strength is just equal to the design load, then the design load is certain to have been exceeded - in this case at Point A. But if sizeable positive margins are available at all points but one, there is a good chance that the one load to exceed its design level will be one for which a positive margin is available, and failure will not occur. It appears, therefore, that in the case of the large, flexible airplane the probability of loss is indeed increased as various "links in the chain" are reduced in strength to that of the weakest link. Thus it can be seen that if each point throughout the structure is designed to the same probability of exceedance of design load, the probability that some point will exceed its design load is greater than the probability that any one given point will exceed its design load.

To be sure, the various loads throughout the structure are not all entirely independent. The bending moment at wing station 105, for example, would obviously be very closely correlated with that at wing station 100. But there is enough independence amongst the various loads so that the probability of exceeding design load somewhere in the airplane is clearly greater, by some undefined amount, for the large flexible airplane than for the simple idealized airplane for which all loads are in phase.

To summarize, the safety of the airplane depends not only upon the probabilities of exceeding design load at individual points, but also on the degree of independence of the various loads and the extent of the structure for which positive margins are available as a result of other requirements.

If the pattern of existing criteria were to be followed, design would be to a number of independent conditions - such as an inner wing bending condition, a nacelle condition, perhaps a maximum axial stress condition and a maximum shear stress condition, and so on. Each condition would be established at a level corresponding to a design probability of exceedance. This, essentially, is what is done in the "matching condition" technique for utilizing statistically defined loads in stress analysis.

Such an approach lacks rationality, of course, in that it gives no explicit consideration to the <u>overall</u> probability of exceeding design strength. This lack of rationality, however, corresponds to the lack of rationality in designing to independent gust and maneuver conditions, which has been accepted as a practical necessity for many years.

It seems clear that no manageable way is about to be found to account explicitly for the overall probability of exceeding design load for such completely different conditions as gust and maneuver. But with the introduction of power-spectral methods, the treatment of gust loads has now become quite explicitly statistical; and it might be hoped that at least all the gust conditions could be treated jointly.

The joint probability approach provides a step in this direction. But this approach covers only two stresses at a point. To extend the technique to take account of loads and stresses at many points in the airplane would require a major advance in the state of the art which, even if accomplished, would undoubtedly lead to a much more complicated analysis.

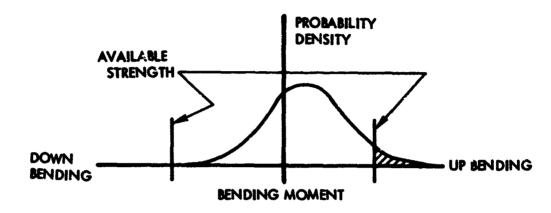
12.2.5 Upbending vs Downbending Loads. Before proceeding further, it will be worthwhile to look at one or two criteria problems that can arise even with respect to the idealized rigid airplane.

The discussion to this point has been implicitly confined to loadings due to vertical gust. Moreover, it has been implicitly assumed that only loads in the positive direction - or, in discrete-gust parlance, loads due to up gusts - are of concern. Now let us consider the problem introduced by considering both up gusts and down gusts.

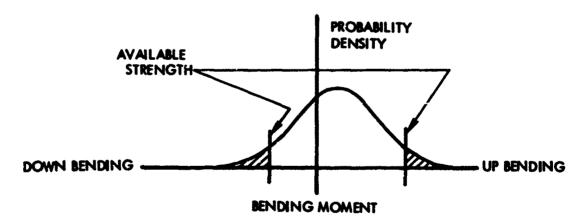
Figure 12-2 shows hypothetical probability densities of wing bending moment due to turbulence. In accordance with the definition of a probability density, the total area under each curve is unity; and the area beyond any particular value of bending moment - such as the shaded area in Figure 12-2(a) - represents the probability that the bending moment is in excess of this value. In both Figures 12-2(a) and 12-2(b) the short vertical lines denote the available strength.

Figure 12-2(a) applies to a structure which is critical in upbending but has substantial excess strength in downbending. The shaded area indicates the probability that the load is in excess of design strength.

Figure 12-2(b) applies to a structure subjected to the same loading but which has been redesigned so that the probability that design strength is exceeded is as great in downbending as in upbending. The overall probability that design strength is exceeded is clearly twice as great for the Figure 12-2(b) structure as for the Figure 12-2(a) structure.



a. UPBENDING CRITICAL



b. UPBENDING AND DOWN BENDING EQUALLY CRITICAL

FIGURE 12-2. ILLUSTRATIVE PROBABILITY DENSITY CURVES - WING BENDING MOMENT

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Past structural philosophy has, of course, been to design for up and down gusts independently, disregarding the increased probability of exceeding design strength if the structure is equally critical for both conditions. As will be more apparent later, the matching condition technique inherently treats the upbending and downbending conditions independently. Thus it is consistent with the past philosophy. The joint probability technique, on the other hand, inherently treats the upbending and downbending conditions jointly, taking account of the combined probability of exceeding limit strength due to both.

There is more involved, however, than design philosophy. The question also arises of whether the probability of exceeding the design strength is really twice as great for the Figure 12-2(b) structure as for the Figure 12-2(a) structure. What is actually in question is the statistical independence of the upbending and downbending loadings. For only if these loadings are statistically independent is the overall probability equal to the sum of the two individual probabilities.

There is fairly convincing evidence that the upbending and downbending loadings, are, in fact, not independent. Consider, for example, the extreme case of a random time history of bending moment confined to a very narrow frequency band, as will result when a mode is very lightly damped. An example of such a time history is shown in Figure 12-3. In effect, each positive peak is paired with an adjacent negative peak of very nearly the same value. In the limiting case, the structure of Figure 12-2(b) is no more critical than that of Figure 12-2(a), since no point can occur in the left-hand shaded area of Figure 12-2(b) unless there has already been a point in the right-hand shaded area on the preceding half-cycle.

Furthermore, an airplane actually flies through many patches of turbulence of varying intensity. Even if in any given patch the upbending and downbending loads were independent, there would appear to be a degree of dependence introduced by the variation of intensity between patches. It would appear that the difference in maximum loads resulting from differences in turbulence intensity would be much greater than the expected difference, within any one patch, between the maximum positive and the maximum negative loads. Once the airplane encounters that most severe patch of turbulence that takes any load to its design value, it is quite likely that both positive and negative loads would exceed design somewhere in the patch.

At this point, a word of clarification is pertinent with respect to the exact meaning of a probability density plot such as shown in Figures 12-2(a) and 12-2(b). What is indicated by such a plot - in particular, by the shaded area of such a plot - is the probability that, at a randomly selected instant, the load is in excess of a given value. This is essentially the same as the expected fraction of time, over a long

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FIGURE 12-3. ILLUSTRATIVE "NARROW BAND" RESPONSE

period, that the load is in excess of the given value. This probability is not the probability that this load level will be exceeded at some time during a given flight, or over a given number of flight hours, or even while flying through a given constant invensity patch of turbulence. Consequently, it is not the kind of probability that has the most direct significance from a structural criteria standpoint. However, it does have an indirect significance. For a constant  $\sigma_{\mathrm{w}}$  level, two airplanes having the same Figure 12-2 type probability that a load is in excess of design will also have the same design-strength values of  $N(y)/N_0$ . Since No tends to be fairly constant for various airplanes, as well as for various load quantities for a single airplane, the two airplanes will also have about the same frequency of exceedance of design load. Consequently they will also have the same probability that design load will be exceeded in a given number of flight hours.\* Furthermore, very roughly the same percentage change in load level would result from doubling the Figure 12-2 probability and doubling  $N(y)/N_0$ , as can be seen by study of Table 12-1.

In the above discussion of upbending vs downbending loads, the emphasis was on the type of probability illustrated by Figure 12-2. Similar observations would result, however, if the problem were approached on a frequency of exceedance basis. Figure 12-4 shows hypothetical frequency of exceedance curves for wing bending moment due to turbulence. Clearly, if the downbending strength is exceeded as often as the upbending strength, the overall frequency of exceedance of design strength is twice as great as when a large margin of safety is present for downbending. But if downbending and upbending peaks occur in pairs, as illustrated in Figure 12-3, the probability that design strength will be exceeded is actually no greater, even though the frequency with which it will be exceeded is twice as great.

Thus, from either the probability density or frequency of exceedance point of view, it is observed that:

(1) The overall probability that design strengt: .l. be exceeded is greater when upbending and downbending conditions are equally critical than when only one is critical, assuming that

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<sup>\*</sup> The probability that a load will be exceeded in a given number of flight hours, however, is not exactly equal to the average number of exceedances in the same number of hours. For an average number of exceedances, n, in a given time, t, of less than about 0.1, the probability is very nearly equal to n. But, clearly, the average number and the probability cannot be equal when the average number is greater than unity, as the probability cannot exceed unity. The exact expression for the probability is:  $P = 1 - e^{-nt}$ .

TABLE 12-1. EFFECT ON LOAD MAGNITUDE OF A FACTOR OF 2 IN CUMULATIVE PROBABILITY OR FREQUENCY OF EXCEEDANCE FOR A STATIONARY GAUSSIAN PROCESS

y/a	Cumulative Probability	Twice the Cumulative Probability	Resulting y/G	Relative Decrease in y/o
2	.0226	.0456	1.7	.3/2.00 = .15
3	.0003	.0026 .00006	2.8 3.65	.2/3.00 = .067 .15/4.00 = .0375

y/a	H(y)	Twice M(y)	Resulting y/o	Relative Decrease in y/o
2	.15	<b>.3</b> 0	1.55	.45/2.00 = .225
3	.0111	.0222	2.75	.25/3.00 = .083
4	.000333	.00066	3.52	.18/4.00 = .045

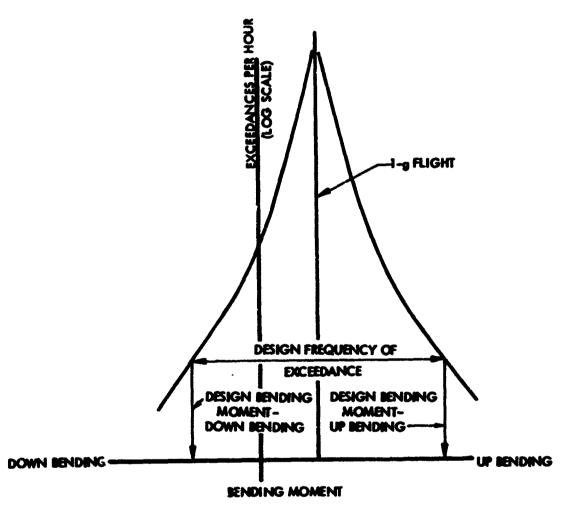


FIGURE 12-4. ILLUSTRATIVE FRZQUENCY OF EXCEEDANCE CURVES - WIND BENDING MOMENT

each condition is established independently to the same probability level.

(2) If, as appears probable, upbending and downbending loads are not statistically independent, the increased probability that design strength will be exceeded is less than would be indicated by the probability density or by the frequency of exceedance curve.

It would appear, however, that in most practicel cases, the actual probability of exceeding design strength may lie somewhat closer to that given by the total of upbending and downbending probabilities or exceedances than by upbending or desable address.

12.2.6 Vertical vs Lateral Gusts. A problem similar to the up vs down gust problem, which likewise arises even with the idealized rigid airplane, involves the joint consideration of vertical and lateral gusts.

Ordinarily vertical gusts will load primarily the wing, while lateral gusts will load the vertical tail. Under existing criteria, each would be considered independently.

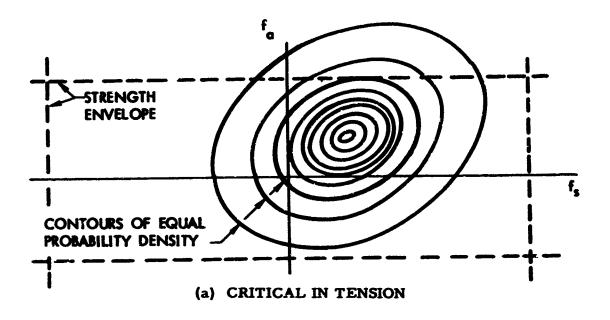
Within any constant-intensity patch of turbulence, the vertical and lateral components of the turbulence can be presumed to be uncorrelated. Consequently, an airplane for which zero margins are present for both lateral and vertical gust would have twice the probability of loss of an airplane critical for only one of the two conditions and having high margins in the other.

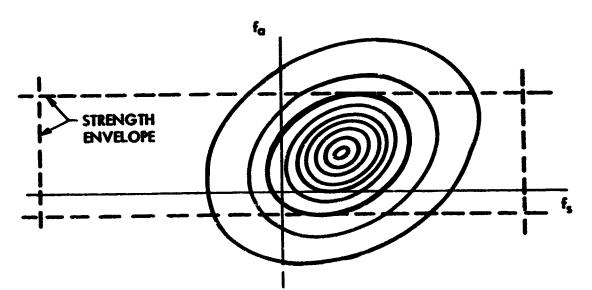
As in the up vs down-gust situation, some degree of dependency may be introduced, however, by the variation in turbulence intensity from one patch of turbulence to another.

12.2.7 Combined Stresses at a Point. In order to explore more explicitly the relation of the two techniques, several special cases involving different relations of strength envelope to joint probability density contours will now be considered.

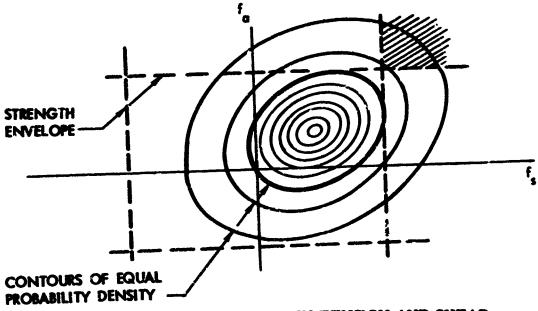
The first is shown in Figure 12-5(a). The rectangular shape of the envelope reflects the limiting case of no interaction, which would actually be approached in a pure tension field structure with closely spaced transverses, or in a truss structure with closely spaced transverses.

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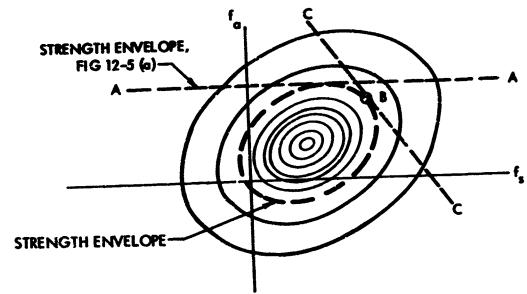


(b) EQUALLY CRITICAL IN TENSION AND COMPRESSION FIGURE 12-5. ILLUSTRATIVE JOINT PROBABILITY DENSITY FOR COMBINED STRESSES WITH VARIOUS STRENGTH ENVELOPES



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(c) EQUALLY CRITICAL IN TENSION AND SHEAR



(d) EQUALLY CRITICAL IN ALL DIRECTIONS FIGURE 12-5. CONCLUDED

It is important to note, incidentally, that, once the applied loading is described by probability density contours, and the strength characteristics by a strength envelope, it is entirely immaterial whether the actual load-carrying mechanism involves interaction or not. Thus the strength envelope in Figure 12-5(a) might be regarded as describing combined stress in a tension field panel, or individual stresses in the caps and cross braces of a truss. In the latter case,  $f_a$  could be replaced by cap load and  $f_s$  by load in a cross brace

A second feature of the strength envelope of Figure 12-5(a) is that the structure is critical in tension only, with large excess strength available in compression and in both positive and negative shear. Clearly, in this case there was no need to consider combined stress. One could have dealt with axial stress only; and, in fac:, the same probability of exceeding the design strength would have been indicated by either treatment.

Now consider Figure 12-5(b). This is the same as Figure 12-5(a), except that the compression allowable has decreased to where compression is as critical as tension. If the joint probability approach is used, the probability of exceeding design strength has doubled. (This is the same situation illustrated by Figure 12-2.) On the other hand, in this particular case, the influence of shear stress might be considered negligible and the usual one-dimensional treatment employed. The calculated probability then does not double - it remains the same as in Figure 12-5(a). Actually, because of the lack of independence of positive and negative loadings, the true probability lies somewhere between. But in any event, there can be a difference by a factor of two depending upon how the problem is treated - whether as a strictly one-dimensional situation or as the limiting case of a two-dimensional situation. Consequently, it would appear highly desirable that, when the joint probability technique is used to handle combined stresses, it also be retained for those parts of the structure subjected to a single stress only. Arbitrary decisions will thus be avoided as to which approach to use at locations in the structure where either might be justified logically but different margins of safety would result.

Next consider Figure 12-5(c). Here instead of a reduced compression allowable there is a reduced shear allowable, so that tension and shour are equally critical. Here again, if the joint probability approach is used, the probability of exceeding design strength has nearly doubled. (It has not quite doubled, because the volume shown shaded is common to both probabilities - that of exceeding design shear and that of exceeding design tension.)

Again, there is a substantial difference in the probability of exceeding design strength depending upon how one chooses to consider the problem - whether as a limiting case of combined stress or as two independent one-dimensional cases.

Here, too, there may well be a question of independence. Since positive and negative stresses appear not to be independent, it seems rather likely that axial and shear stresses may also not be independent. In fact, the example of a lightly damped system illustrated in Figure 12-3 would have a counterpart here in a situation involving a typical bendingtorsion flutter mode. If such a mode when only very lightly damped, as would ordinarily occur at speeds just below the flutter speed, large motions in the mode, relative to those that could be produced by the exciting forces acting statically, would develop. These motions would involve bending and torsional motions - and stresses - differing in phase by some constant angle. In Figure 12-5(c), for example, in any one cycle the stresses would follow very closely a single equal probabilitydensity ellipse, traveling once around the ellipse per cycle. Transfer from one ellipse to another would occur only gradually over a period of several cycles. Thus each exceedance of the strength envelope in positive shear would tend to be preceded or followed (depending upon the direction of travel around the ellipse) by an approximately equal exceedance in tension.

Finally, Figure 12-5(d) shows an extreme case for which the probability of exceeding design strength is very much greater under the joint probability than under the one-dimensional approach. The equal probability contours shown are the same as for cases (a) through (c) in the same figure. The strength envelope, however, is now assumed to coincide with one of these contours. The strength envelope assumed in Figure 12-5(a) is also shown; this is a single straight line and is denoted AA.

Even though the strength of the structure to withstand tension, compression or shear alone is no less for this case than for the cases shown in Figures 12-5(a) through (c), the probability of exceeding limit strength is much greater here than for the other cases.

At this point, certain contrasting characteristics of the joint probability and matching condition techniques, that may have been implied in the foregoing paragraphs, should be defined more clearly.

For the purpose of the present discussion, the important characteristic of the matching condition technique is not that statistically defined loads are matched by discrete design conditions - rather, it is that the quantities matched are single loads, in either actual or fictitious structural elements. The matching condition technique might perhaps better be designated - for the purpose of the present discussion - the

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"single parameter" technique. The term "single parameter" refers to the fact that in determining the probability of exceeding limit strength, the applied load statistics are defined by a single parameter,  $\sigma_{\rm X}$ , rather than by three parameters,  $\sigma_{\rm X}$ ,  $\sigma_{\rm Y}$ , and  $\rho_{\rm XY}$ . Analogously, the "joint probability" technique might be designated the "multi-parameter" technique. Similarly, the two techniques might be referred to as the "one-dimensional" and "two-dimensional" techniques, respectively. This terminology would reflect the fact that in the matching condition technique the probability density is a function of one load quantity only, whereas in the joint probability technique the probability density is a function of two load quantities jointly.

Neither of these pairs of terms, however, is completely descriptive. In the single parameter, or matching condition technique, it is to be understood that not only is the probability of exceeding limit strength defined for single load quantities only, but also for the positive and negative directions individually. Thus, in Figure 12-5(b), even though only a single load quantity and a single statistical parameter are involved, the joint probability technique can still be used, and still indicates twice the probability of exceeding limit strength as the matching condition technique.

To emphasize further that the single parameter philosophy does not necessarily involve the generation of matching conditions, it might be noted that it can actually be applied directly to stresses at individual locations in the structure. Thus the generation of complete design conditions could be completely bypassed, if desired. In this application, the fictitious structural element concept would, of course, be used, as illustrated in Figure 12-6. Instead of contours of equal probability density, there will now be a single applied stress envelope. Each point on this envelope is considered independently in the stress analysis; clearly, most of the envelope can be disregarded as obviously non-critical.

The quantitative differences resulting from use of the multi-parameter and single parameter techniques can now be emphasized by returning to Figure 12-5.

Consider, for example, the case shown in Figure 12-5(d), and suppose that a design probability of exceedance has been selected, equal to the volume outside the line AA. Under the single parameter approach, fictitious structural elements would be utilized to generate an "equal probability" ellipse as described in Section 11.2. Line AA would be one of the family of lines generating this ellipse. The ellipse thus generated would presumably coincide with one of the contours of equal probability density - in this case, the one indicated by the dash line, which is also the strength envelope. (That the ellipses obtained in these two ways

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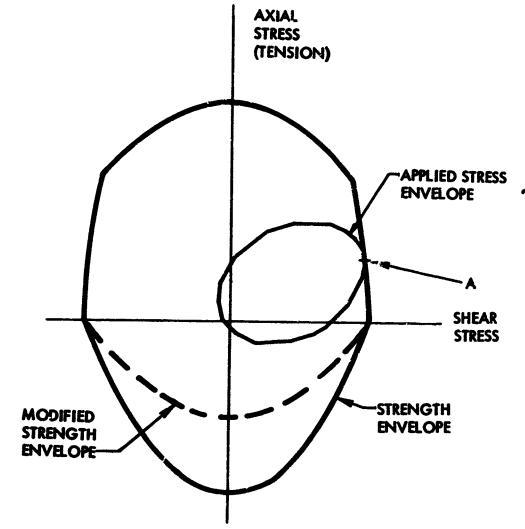


FIGURE 12-6. APPLIED STRESS ENVELOPE FOR COMBINED STRESSES

do coincide appears intuitively quite certain, although no proof has been made.) Design points would be defined at various points around this ellipse. Each point, such as B in the figure, is associated with a straight line tangent at that point (in this case CBC) representing constant stress in a particular fictitious structural element. The volumes outside all of these lines are clearly the same, as can be seen by uniformly stretching or contracting the figure in a direction such as to convert the ellipses into circles. This equality of the volumes, it would appear, would also follow from the fact that the constant-stress lines were each established initially at the same design probability of exceedance.

Each point on the design load ellipse is also, in this example, on the strength envelope. For every point, therefore, the margin of safety is zero.

The probability of exceeding limit strength, as indicated by the single parameter approach, is given by the volume outside any one of the straight lines circumscribing the ellipse.

Under the joint probability approach, on the other hand, the probability of exceeding limit strength is indicated by the volume outside the dash-line ellipse, which is very much greater.

For this limiting case, as well as for the intermediate case defined by Figure 12-5(b), the relative probabilities of exceeding limit strength given by the two approaches are indicated by the cumulative probability curves of Figure 12-7. The probability of exceeding limit strength according to the single parameter technique is given by the "Normal" curve in the figure. This is simply a plot of the expression,

$$P = 1 - \int_{-\infty}^{y} \hat{f}(y) dy$$

where f(y) is the "normal." or "Gaussian" probability density for any load quantity, y:

$$\hat{f}(y) = \frac{1}{\sqrt{2\pi}\sigma} \exp(-y^2/2\sigma^2)$$

(In these expressions, y is considered to be the gust increment only.)

If positive and negative loading directions are equally critical, the joint probability technique accounts for both the positive and the negative tails of the probability density function. Thus for the situation

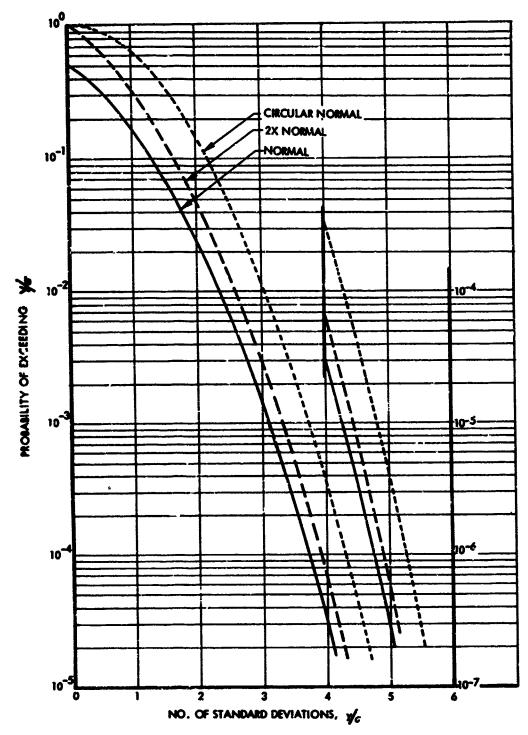


FIGURE 12-7. CUMULATIVE NORMAL PROBABILITY DISTRIBUTIONS

reflected by Figure 12-5(b) it results in a probability twice that given by the "Normal" curve. This is shown by the "2 x Normal" curve in Figure 12-7, which is the "Normal" curve shifted up by a factor of 2. It is given by the expression

$$P = 1 - \int_{-y}^{y} \hat{f}(y) dy$$

For the limiting case indicated by Figure 12-5(d), the "Circular Normal" curve applies. This is based on a circular two dimensional normal distribution. It denotes the volume under the probability density surface outside an equal probability density circle of radius y, as given by Equation 11.8.5 of Reference 24,

$$P = \exp(-y^2/2\sigma^2)$$

where  $\sigma$  is the rms value of, for example,  $f_a$ .

It can be seen from Figure 12-7 that, as the  $y/\sigma$  level increases, the ratio of the probabilities indicated by the "Circular Normal" and "Normal" curves increases gradually. On the other hand, the percentage difference between the two curves at a given probability level decreases. At the  $3\sigma$  load level, the difference in load between "Normal" and "Circular Normal" curves is seen to be roughly 20%. The percentage difference between the "2 x Normal" and "Normal" curves also decreases as the  $y/\sigma$  level increases. At  $y/\sigma = 3$ , it is seen to be roughly 7%. Manifestly, the relation of strength envelope to applied stress indicated by Figure 12-5(d) is extreme, and ordinarily it would not be even closely approached. Consequently the difference in load level between a single param ter analysis and a multi-parameter analysis at the same probability level is generally much smaller than it would be for this extreme case.

Either technique can of course be applied to a reference airplane and a probability level corresponding to limit strength established. It is important to note, however, that application of the two techniques to a new airplane, each at its appropriate probability level as derived from the reference airplane, will in general lead to different required strengths. And the required strength may be either higher or lower for the joint probability technique than for the matching condition technique.

Suppose, for example, that the strength envelopes for the reference airplane are generally like Figure 12-5(a) and for the new airplane like Figure 12-5(d). The design probabilities derived from the reference airplane will then be the same for both techniques. But for the new

airplane, the joint probability technique will tend to show a much higher probability of exceeding limit strength, requiring greater strength to achieve the same indicated probability.

On the other hand, suppose the situation to be reversed, so that the strength envelopes for the reference airplanes are generally like Figure 12-5(d) and for the new airplane like Figure 12-5(a). The design probability will now be greater as derived from - and for use with - the joint probability technique. For the new airplane, the two techniques will tend to show equal probabilities of exceeding limit strength. But the joint probability technique will have a higher allowable probability of exceeding limit strength, so that it will actually permit less strength in the new airplane than will the matching condition technique.

It is important to keep these differences in mind when comparing results of joint probability and matching condition analyses. In particular, care must be taken in determining limit strength  $\sigma_w \eta_d$  values based upon the joint probability treatment of the Model 720B, inasmuch as  $\sigma_w \eta_d$  has meaning, basically, only in terms of a single-parameter analysis.

Fortunately, however, as noted earlier, the numerical differences are not likely to be large. It is believed that in practical cases the strength envelope will seldom be of such a shape, relative to the probability density contours, as to more than double the probability of exceeding limit load, relative to the situation illustrated in Figure 12-5(a). The difference in strength required for the two situations would be indicated by the difference between the "Normal" and "2 x Normal" curves in Figure 12-7. At the  $3\sigma$  level, this is seen to be only 7%.

12.2.8 Summary. In attempting to evaluate and summarize the relative rationality of the two techniques, it is obvious that the single parameter technique fails to account explicitly for the reduction in safety produced by the presence of more than one "weak link in the chain." In this respect, it may provide a somewhat poorer measure of the relative safety of two airplanes than the joint probability technique. On the other hand, this deficiency is somewhat ameliorated by the following considerations:

- (a) No theory is currently available that does account explicitly for the presence of more than one "weak link in the chain", except at a single point in the structure.
- (b) This situation will continue to exist with respect to gust vs maneuver loads, where the consequences are even greater because of the unquestioned independence of the conditions.

- (c) Because of the lack of complete independence of the various stresses, and of positive and negative values of a single stress, even at a single point in the structure, it is not certain how much more realistic if any the joint probability treatment is than a single-load treatment as used in the matching condition technique.
- (d) To whatever extent various airplanes are similar in the degree to which various conditions are equally critical, the effect will be accounted for, at least in part, in establishing the design levels based on past satisfactory airplanes.

The matching condition technique does maintain a very convenient consistency within itself and with current structural design philosophy. It is consistent with the long standing philosophy of independent design conditions. Results are not subject to inconsistencies depending upon structural arrangement or arbitrary choice of treatment. And the commonsense one-dimensional treatment of the idealized rigid airplane falls out naturally as a special case.

The quantitative differences between the results obtained by the two techniques are small, especially when establishment of the respective design levels reflects an adequate understanding of the fundamental differences between the two approaches.

## 12.3 Establishment of Equivalent Design Levels

With the discussion in the previous section as background, specific consideration can now be given to how the joint probability results for the Model 720B should be used to obtain a limit-strength value of  $\sigma_{\rm W} \eta_{\rm G}$  for comparison with the values obtained for the Model 188 and Model 749.

It is to be emphasized that no direct relation between the design levels to be used in joint probability and single parameter analyses can be established except in terms of a given location in a given airplane. What particularly characterizes a given location in a given airplane is the relation of the strength envelope to the probability density contours. Various particular relations were noted in the previous section and shown in Figures 12-5(a) through (d).

In the presen" analysis, the airplanes for which the relation between joint probability and single parameter design levels must be established is clearly the Model 720B, for a combination of the following reasons:

a. It is the only one for which the joint probability analysis is available.

- b. Based on examination of the relation of the coungth envelope to equal-probability-density contours on an fa vs fs plot, it should be possible to estimate how the 720B would come out on a single-parameter basis.
- c. There is no readily available way to estimate how the 188 or 749 would come out on a joint probability basis.
- d. To preserve a tie-in with currently used approaches, it is desirable to express the final criterion on a  $\sigma_w \eta_d$  basis. This means converting the 720B results to this form, rather than converting the 188 or 749 results to a joint probability form.

One procedure that might be used to establish a limit strength  $\sigma_w$   $\eta_d$  value to associate with the results of a joint probability analysis can be outlined as follows:

- a. Pick a  $\sigma_W$  value arbitrarily, guided by the location of the peak of the curve of  $P(MS < 0, \sigma_W) \times \hat{f}(\sigma_W)$  vs  $\sigma_W$  as shown, for example, in Figure 19 of Reference 1.
- b. Obtain from the joint probability analysis the probability that (MS < 0) corresponding to this  $\sigma_{\rm W}$ . For the example shown in Reference 1, this can be read from Figure 16 therein.
- c. Enter the appropriate cumulative probability curve of Figure 12-7 and read  $y/\sigma$ . Inasmuch as  $\eta_d$  is, by definition (Section 4.2), the limit design value of  $y/\sigma$ , the value of  $y/\sigma$  thus obtained is  $\eta_d$ .
- d. The product of  $\sigma_{W}$  from Step (a) and  $\eta_{d}$  from Step (c) gives  $\sigma_{W} \eta_{d}$ .

This procedure is not exactly the same as used in Reference 1. It is basically similar, however, and appears to give almost identical results. It may be just as good a procedure, all-in-all, and, for the purpose of understanding the relation of single parameter to multi parameter design levels, it has the advantage of simplicity.

In using this procedure, the one operation that is not clearly defined is the selection of the appropriate curve in Figure 12-7 to use in Step (c).

After an  $\eta_d$  has been determined, its sole use will be in a single-parameter analysis to give a design value of  $f_a$  or of some other single stress, perhaps in a fictitious structural element. And positive and negative values of the stress will inherently be treated independently.

Consequently,  $\eta_d$  must be selected so as to give the right limit-strength value of this stress. More specifically, when used in a single-parameter analysis of the airplane from which it is derived, it must yield a value of stress in the critical structural element equal to the actual limit strength of that element.

For example, suppose that a design  $\sigma_W$  has been selected (Step (a) above), and that for the critical location in the structure the joint probability analysis gives F (MS<0) = .001.

Now suppose further that the structure for which the joint probability analysis was conducted has the characteristic indicated by Figure 12-5(a). In this case, the probability of exceeding limit strength is governed by stress in a single member that feels only tensile stress,  $f_a$ . The relation of stress to probability for this member is given by the "Normal" curve in Figure 12-7; and this curve duplicates exactly the probability that would be given by a joint probability analysis for various limit-strength values of  $f_a$ . Consequently,  $\eta_d$  is the  $y/\sigma$  value read from this particular curve at P=.001. With this value of  $\eta_d$ , and a value of  $\sigma_W$  as assumed in the joint probability analysis, the strength is indeed such that the joint probability analysis gives P=.001.

If, instead, the structure has the characteristic indicated by Figure 12-5(b), then to give the same P(MS < 0) the strength-envelope value of stress must have been higher, since the total area under the  $f_a$  probability density curve beyond the limit strength value must be no greater now for both positive and negative tails then for the positive tail only in the Figure 12-5(a) case. In other words, the horizontal dash lines in Figure 12-5(b) must be slightly farther apart than shown, to keep P(MS < 0) equal to .001. Use of the "2 x Normal" curve in Figure 12-7 results in the higher  $\eta_d$  value required to give this higher stress. It is clearly this higher stress that would have had to be designed to in the single parameter approach in order to provide the strength that was actually present and resulted in P = .001 in the joint probability analysis.

If the structure has the characteristic indicated by Figure 12-5(d), then the stress  $f_a$  must have been higher still, for the same reason. The "Circular Normal" curve would give the correct single-parameter allowable stress in this case.

Thus it is seen that for the purpose of obtaining limit strength  $\sigma_w \eta_d$  values for the Model /20E airplane, the choice of an appropriate curve in Figure 12-7 depends only on the relation of applied stresses (as described by equal probability density contours) to the strength envelope for the critical elements of that airplane.

The same concept and even the same specific conclusions apply if the determination of limit-strength  $\sigma_{\rm W}$   $\eta_{\rm d}$  is based not on a single  $\sigma_{\rm W}$  but instead, as in Reference 1, on what might be thought of as a weighted average  $\sigma_{\rm W}$ , with the weighting in accordance with  $\hat{T}$   $(\sigma_{\rm W})$ .

The procedure used in Reference 1 is an approximation to a more fundamental one that can be outlined as follows:

(a) Considering the fractions of flight time at various  $\sigma_W$  levels (as defined by the b and P values established in Section 5), obtain an over-all, or weighted-average, probability that the margin of safety is less than zero, based on the joint probability analysis:

$$P (MS < 0) = \int_{0}^{\infty} P \left[ MS < 0, \sigma_{W} \right] \hat{f} (\sigma_{W}) d \sigma_{W}$$

there the expression in brackets is to be read "probability that MS<0 for a given  $\sigma_{w}$ ." That this equation gives the over-all probability is evident if P (MS<0) is thought of as a fraction of time that MS<0. This fraction of time is the sum of the fractions of total time that MS<0 within the various  $\sigma_{w}$  bands. For each band, the fraction of the total time spent in the band is  $\hat{f}$  ( $\sigma_{w}$ ) d  $\sigma_{w}$ . The fraction of total time for which MS<0 in the band is then P (MS<0,  $\sigma_{w}$ ) x  $\hat{f}$  ( $\sigma_{w}$ ) d  $\sigma_{w}$ . The total probability that MS<0, for all bands, is obtained by summing over  $\sigma_{w}$ .

(b) Similarly, obtain the over-all probability that a lingle generalized load quantity, y/Ā, exceeds each of series of values of (y/Ā)<sub>i</sub>, which might be considered as potential limit-strength values:

$$P\left[y/\bar{A}>(y/\bar{A})_{\hat{1}}\right] = \int_{0}^{\infty} P\left[y/\bar{A}>(y/\bar{A})_{\hat{1}}, \sigma_{w}\right] \times \hat{f} (\sigma_{w}) d \sigma_{w}$$

- (c) Plot  $P\left[y/\overline{A}>(y/\overline{A})_i\right]$  vs  $(y/\overline{A})_i$ , as given by Step (b).
- (a, From the curve thus obtained, enter with the probability obtained in Step (a) and read  $(y/\bar{A})_i$ . This is  $\sigma_w \eta_d$ .

In Step (b) above, the quantity  $P\left[y/\bar{A}>(y/\bar{A})_i,\sigma_w\right]$  is evaluated in Reference 1 by means of Equation 12 therein, which can be written in generalized form as:

$$P\left[\frac{y/\bar{A}}{\sigma_{V}} > \frac{(y/\bar{A})_{\dot{1}}}{\sigma_{W}}\right] = 2 \int_{(y/\bar{A})_{\dot{1}}}^{\infty} \frac{1}{\sqrt{2\pi}} \exp\left[-\frac{1}{2} \left(\frac{y/\bar{A}}{\sigma_{W}}\right)^{2}\right] d\left(\frac{y/\bar{A}}{\sigma_{W}}\right) (13-1)$$

Once the integration indicated on the right hand side of this equation has been carried out, various values are assigned to  $\sigma_w$ ; P  $[y/\bar{A}>y/\bar{A}_i, \sigma_w]$  can then be plotted vs  $(y/\bar{A})_i$  for various values of  $\sigma_w$ ; or, as in Figure 17 of Reference 1, vs  $\sigma_w$  for various  $(y/\bar{A})_i$  values.

The integrand in Equation 13-1 is simply the normal probability density, and the factor 2 accounts for both positive and negative tails of the probability density in the cumulative probability. Thus it is seen that, in Reference 1, the "2 x Normal" curve in Figure 12-7 was, in effect, assumed. The selection of the appropriate cumulative probability curve in Figure 12-7 is thus required in this step; the same type of choice must be made as in Step (c) of the first rocedure, with the three curves of Figure 12-7 providing examples that can b. used.

The selection of the "2 x Normal" curve in Reference 1 implicitly assumes a relationship between the strength envelope and the probability density contours equivalent to that of Figure 12-5(b). An "equivalent" relation, in this context, would be any for which the volume outside the strength envelope is the same as that in Figure 12-5(b); Figure 12-5(c), for example, would be very nearly equivalent.

If the "Normal" curve had been used instead, values of  $\eta_d$ , and hence of  $\sigma_W \eta_d$ , would have been about 5% lower. This percentage follows from a comparison of  $y/\sigma$  values from the "Normal" and "2 x Normal" curves at a  $y/\sigma$  level of 3.5.

It is of interest to note the range of  $\eta_{\rm d}$  values inferred from the results given in Reference 1. For each case in Table 12 therein, the  $\sigma_{\rm w}$  value corresponding to the peak of the curve in Figures 75 through 78 was read. This divided into the  $\sigma_{\rm w}$   $\eta_{\rm d}$  value listed in the Table gave the corresponding  $\eta_{\rm d}$ . The values ranged generally from 2.8 to 4.2, with the majority falling in the range 3.0 to 3.7.

Limit strength values of  $\sigma_{\rm W}$   $\eta_{\rm d}$  listed in Reference 1, for the critical locations in the Model 720B, are as follows:

Wing  $\sigma_w \eta_d = 111$  at 22000 ft.

Pody and Tail, Vertical Gust  $\sigma_{\rm W} \eta_{\rm d} = 175$  at 22000 ft. (aftbody critical)

Body and Tail, Lateral Gust (tail critical)

Yaw damper off

 $\sigma_{\rm W} \eta_{\rm d} = 99 \text{ at 23000 ft.}$ 

Yaw damper on

 $\sigma_{\rm W} \, \eta_{\rm d} = 137$  at 23000 ft.

Care must also be taken in relating limit strength N(y) values as given by joint probability and single-parameter analyses. Clearly there will be more crossings per hour of a two dimensional strength envelope than of limit strength in any single member. Consequently, for any given airplane, the limit strength N(y) on a joint probability basis will be higher than on a single-parameter basis. It would appear that if the "2 x Normal" curve in Figure 12-7 is considered appropriate in establishing  $\sigma_W$   $\eta_d$  values to associate with the joint probability analysis, then the equivalent single-parameter N(y) values should be approximately 1/2 the joint probability values. Consequently N(y) values obtained for the Model 720B by means of the joint probability analysis should be multiplied by 1/2 for comparison with Model 188 and Model 749. Critical limit strength values for the Model 720B, on a single parameter basis, are therefore as follows:

Wing  $N(v) = 1/2 (2.3 \times 10^{-5})$ = 1.1 x 10<sup>-5</sup> cycles per hour

Body and tail, vertical gust  $N(y) = 1/2 (2.0 \times 10^{-9})$  (aftbody critical)

=  $1.0 \times 10^{-9}$  cycles per hour

Body and tail, lateral gust

Yaw damper off  $N(y) = 1/2 (8 \times 10^{-6})$  (tail critical)  $\approx 4 \times 10^{-6}$  cycles per hour

≈ 4 x 10°0 cycles per hour

Yaw damper on  $N(y) = 1/2 (2.4 \times 10^{-8})$ (afthody critical)  $= 1.2 \times 10^{-8}$  cycles per hour

#### 12.4 Comparative Application of the Two Techniques to the Model 720B

To provide a further numerical check of the effect of the choice of design technique on numerical results, the matching condition technique was applied to the Model 720b at one location, namely wing eta station .33. This analysis was for design envelope Case 27; this case was selected and the work performed before it was found that Case 24c was somewhat more critical.

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"Equal probability" ellipses relating torsion and shear, shear and bending moment, and torsion and bending moment were obtained using the fictitious structural element concept as described in Section 11.2. These are shown in Figure 12-8. Inasmuch as the analysis was for a design envelope case, all of the constant stress lines were for a given value of  $\sigma_{\rm W}$   $\eta_{\rm d}$ . This value was taken as 108.3, the limit-strength value obtained for this case based upon consideration of bending moments alone.

The joint probability analysis indicated that Element No. 9 (See Figure 68 of Reference 1) was critical for this case. The torsion-bending interaction (Figure 12-8(c)) was considered most indicative of the wing strength. As a result, a torsion-bending limit-strength envelope was determined; this was based upon stresses in Element No. 9, assuming shear to be in phase with bending moment.

It is seen from Figure 12-8(c) that the limit-strength value of  $\sigma_W \eta_d$  is somewhat greater than the assumed value of 108.3. The value that brings the ellipse tangent to the strength envelope is found to be 114.

Limit strength values of  $\sigma_{\rm W} \, \eta_{\rm d}$  based on Case 27 at wing eta station .33 can be summarized as follows:

Regie

Design	ow va
Bending moment alone (typical shear and torsion included)	108.3
Single-parameter treatment using ficticious structural elements, Figure 12-8(c)	114
Joint probability treatment, Table 12 of Reference 1, "2 x Normal" curve of Figure 12-7 assumed	118.4
Joint probability treatment, adjusted to basis of "Normal" curve of Figure 12-7	112

The last value is obtained by ratioing according to the  $y/\sigma$  values given by the "Normal" and "2 x Normal" curves of Figure 12-7 at P = .0005.

It is seen that the joint probability value of 118.4 differs from the single-parameter (i.e., matching condition) value of 118.4 by less than 44. If the joint probability value had been based upon the "Normal curve" in Figure 12-7, it is seen that the difference would have been less than 24.

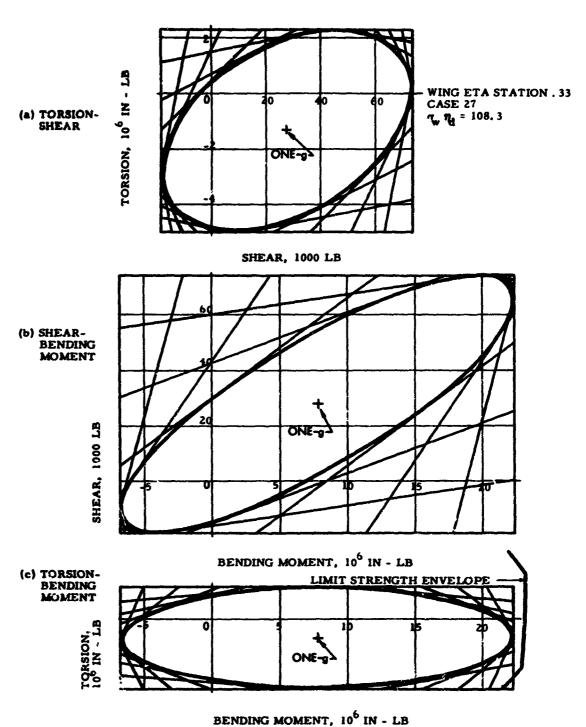
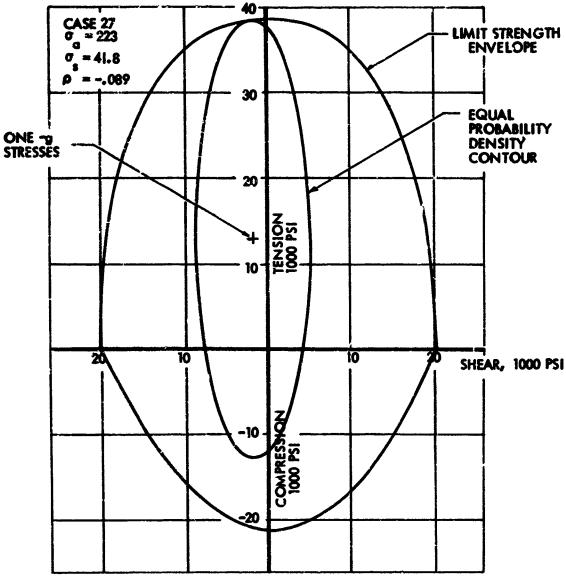


FIGURE 12-8. "EQUAL PROBABILITY" ENVELOPE, MODEL 720B

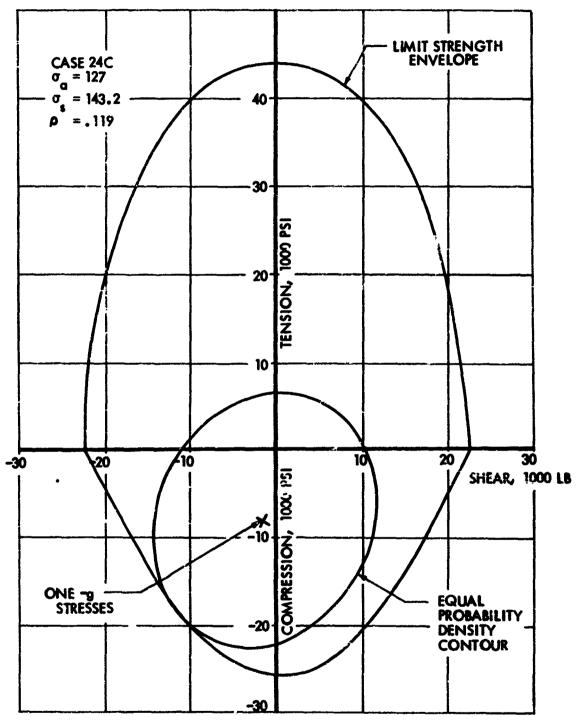
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To determine whether these relative values are what might be expected based upon the discussion in Section 12.3, the stress picture at Element No. 9 is examined in Figure 12-9(a). It is seen that the relation of the equal probability density contour to the strength envelope is quite close to that of Figure 12-5(a). The additional probability of exceeding limit strength due to the finite - as contrasted to infinite - strength in the compression and positive and negative shear regions of the strength envelope can be evaluated roughly by adding probabilities from the "Normal" curve in Figure 12-7 at the higher  $y/\sigma$  levels appropriate to these regions. The increment is found to be negligible. Consequently, in this case, the  $\sigma_{\rm W}$   $\eta_{\rm d}$  corresponding to the joint probability results should more properly have been obtained using a curve much closer to the "Normal" curve than to the "2 x Normal" curve in Figure 12-7. Thus the single-parameter value of  $\sigma_{\rm W}$   $\eta_{\rm d}$  of 114 is seen to bear a quite reasonable relation to the values of 112 and 118.4 obtained from the joint probability results.

It is also of interest to examine in the same way the stresses for the critical case, No. 24c, at its critical element, No. 122. The equal probability density contours and the strength envelope for this case are shown in Figure 12-9(b). Here, too, it would appear that a curve somewhere between the "Normal" and "2 x Normal" curves in Figure 12-7 should be used, but probably not quite as close to the "Normal" curve as for Case 27 and Element 9.



(a) WING ETA STATION . 33, ELEMENT 9, CASE 27
FIGURE 12-9. RELATION OF JOINT PROBABILITY DENSITY TO
STRENGTH ENVELOPE, MODEL 720B



(b) WING ETA STATION . 33, ELEMENT 122, CASE 24C FIGURE 12-9. CONCLUDED

# 13 ESTABLISHMENT OF LIMIT-STRENGTH AND ULTIMATE-STRENGTH LEVELS OF N(y) AND $\sigma_w \eta_d$

Limit strength and ultimate-strength values of N(y) and  $\sigma_w \eta_d$  are obtained for the Model 188 and Model 749 in Appendix E. For the wing, this determination generally involved estimating a design level (N(y)) or  $\sigma_w \eta_d$ , determining properly phased loads at this level at the potentially critical regions of the wing, performing stress analysis to obtain margins of safety, and adjusting the level as required to give a zero margin. Inasmuch as only the critical region of the structure is of interest, complete matching conditions generally did not have to be generated, and the matching condition concepts were applied on a more local basis. Fuselage loads were found to be less critical than wing loads so that a less exact analysis was permissible and phasing could generally be disregarded.

For the Model 720B, limit strength levels were obtained in Reference 1. These follow directly from the joint probability analysis. The limit strength values of  $\sigma_w \eta_d$  were obtained based upon assumptions discussed more fully in Section 12.3 herein, where the critical values are summarized. The limit-strength values of N(y) given in Reference 1 were divided by 2 to provide a reasonable estimate, consistent with the  $\sigma_w \eta_d$  determination, of the exceedances that would occur on a single parameter basis. This adjustment is shown in Section 12.3 for the critical locations in the s ructure.

Limit strength values of N(y) for all three airplanes, and ultimate strength values for the Model 188 and Model 749, are summarized in Table 13-1 and plotted in Figure 13-1.

Lateral gust values for the Model 720B are shown both for yaw damper off and for yaw damper on. Although use of the yaw damper is not required by the flight manual, its use is recommended; and apparently it has been the practice to utilize the yaw damper virtually 100% of the time. If it were assumed, for example, that the damper were in use 99% of the time, the limit-strength value of N(y) would be about  $(1/100)(4 \times 10^{-6}) + (99/100)(1.2 \times 10^{-6}) = 5.2 \times 10^{-6}$  exceedances per hour.

In order to give a quantitative indication of the effect of frequency of exceedance on load level, several typical exceedance curves are shown in Figure 13-2. Each of these is multiplied by a factor, in the horizontal direction, such to give a load value of unity at  $10^{-5}$  exceedances per hour. The vertical scale is selected to line up with that of Figure 13-1. Differences amongst the various curves are due largely to different ratios of one-g to incremental load.

TABLE 13-1. SUMMARY OF MISSION ANALYSIS RESULTS

Component and Airplane	Frequency of Exceedance, N(y), Per Average Flight Hour					
	Limit Strength	Ultimate Strength				
Wing						
188	2.1 x 10 <sup>-5</sup>	1.4 x 10 <sup>-8</sup>				
749	1.8 x 10 <sup>-5</sup>	4.2 x 10 <sup>-9</sup>				
720B	1.3 x 10 <sup>-5</sup>	-				
Body and Tail-Vertical Gust						
188 (Forebody)	6.0 x 10 <sup>-6</sup>	1.0 x 10 <sup>-9</sup>				
749 (Tail)	4.5 x 10 <sup>-9</sup>	1.7 x 10 <sup>-14</sup>				
720b (Aftbody)	1.0 x 10 <sup>-9</sup>	_				
Body and Tail-Lateral Gust						
188 (Afthody)	6.0 x 10 <sup>-5</sup>	5.0 x 10 <sup>-7</sup>				
749 (Tail)	2.5 x 10 <sup>-4</sup>	5.0 x 10 <sup>-6</sup>				
720B, Yaw Damper Off (Tail)	4.0 x 10 <sup>-6</sup>	_				
720B, Yaw Damper On (Body)	1.2 x 10 <sup>-8</sup>	-				

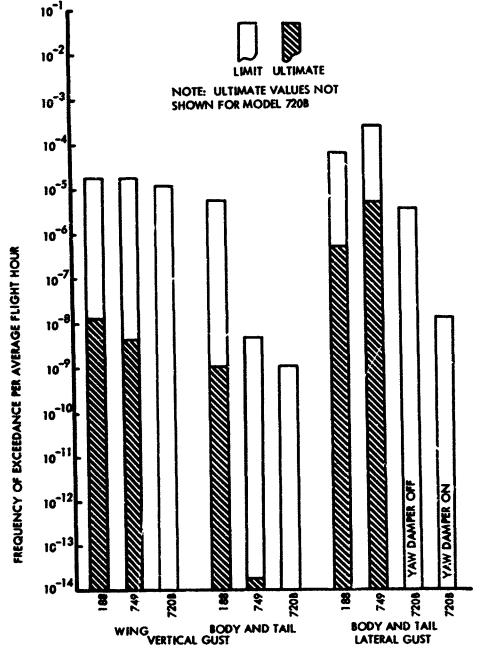


FIGURE 13-1. SUMMARY OF MISSION ANALYSIS RESULTS

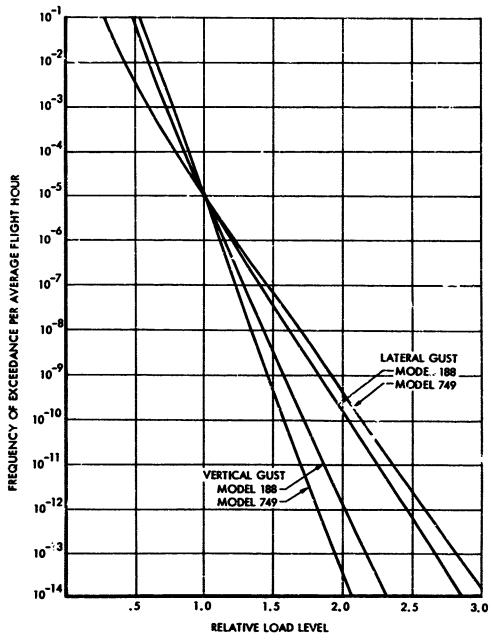


FIGURE 13-2. TYPICAL VARIATION OF LOAD LEVEL WITH FREQUENCY OF EXCEEDANCE

Limit and ultimate strength values of  $\sigma_W \eta_d$  are summarized in Table 13-2 and plotted in Figures 13-3 and 13-4. Only the critical condition for each major component is shown. Values of  $\sigma_W \eta_d$  shown in the last two columns of Table 13-2 and in Figure 13-4 are adjusted to a common altitude of 7000 ft. by moving along lines of constant  $N(y)/N_0$  in Figure 5-8.

Lateral gust values for the Model 720B are again shown both for yaw damper off and for yaw damper on. It should be noted that the 720B lateral gust cases were generally confined to the VC boundary of the speed-altitude envelope. It appears that the yaw-damper-off loads would be higher at somewhat-reduced speeds because of the lower Dutch roll damping. However, it is believed that the pilot would be aware of the reduced damping, would not like it, and would either put the damper on, if possible, or improve the damping himself by suitable control action.

Limit strength values of  $\sigma_w$   $\eta_d$  are shown for the Vc condition only. From the discussions in Appendix E and the data shown in Reference 1, it appears that all three airplanes can withstand a  $\sigma_w \, \eta_d$  at  $V_D$  of at least 25/50 the Vc value. (The factor 25/50 will be recognized as the ratio of currently specified Ude gust velocities at the respective speeds.) For the Model 188 wing, the VD value is just 25/50 of the VC value. For the Model 749 wing the VD value is slightly greater than 25/50 of the VC value. For the Model 720B, based on wing bending moment alone, it appears that the limit strength  $\sigma_{W}$   $\eta_{cl}$  is even greater at  $V_{D}$  than for the critical speed within the Vc boundary. It also appears that all three airplanes can withstand a somewhat higher  $\sigma_w \eta_d$  at  $V_B$  than at  $V_C$ , but not, in all cases, in the full 66/50 = 1.32 ratio of current  $U_{\rm de}$  values. The ratio for the Model 188 wing is well in excess of 66/50. For the Model 749 wing, the ratio is only about 1.25. However, a more pertinent ratio, in this case, is that of limit-strength ow nd at VB for the Model 749 to limit-strength  $\sigma_w \eta_d$  at  $V_C$  for the critical airplane (the Model 188); this ratio is  $(1.25 \times 88)/(62) = 1.77$ . (The number 62 is the limitstrength  $\sigma_w \, \eta_d$  for the Model 188 at  $V_C$ , adjusted to an altitude of 7000 ft.) This ratio, too, is well in excess of 66/50. For the Model 720B, the ratio of VB to VC limit strength  $\sigma_{\rm W} \, \eta_{\rm d}$ 's is roughly 1.15, as indicated by Figure 42 of Reference 1. For this airplane, too, the more pertinent ratio of limit-strength,  $\sigma_{\rm W} \, \eta_{\rm d}$  at  $\rm V_B$  to limit strength  $\sigma_{\rm W} \, \eta_{\rm d}$ at Vc for the Model 188, is well in excess of 66/50.

Generally, it is believed that the stress analysis methods used in establishing these results were realistic and reasonably consistent with the methods that would be used on new designs today.

A minor exception might be the Model 749 wing, where possibly some load redistribution from the critical element to less critical elements, not accounted for in the stress analysis, might occur. The critical elements are indicated in Appendix E to be the beam web and beam web splice; however, the critical stress was produced predominantly by wing bending moment rather than shear and torsion, and some slip in the web splice

TABLE 13-2. SUMMARY OF DESIGN ENVELOPE RESULTS

Component and Airplane	•	d, <sup>Fps</sup> de Indicated	σ <sub>w</sub> η <sub>d</sub> At 70	
	Limit Strength	Limit Strength	Ultimate Strength	
Wing				
188	60 @ 12000 Ft	101 @ 12000 Ft	62	100
749	88 <b>@</b> 7000 Ft	155 @ 16000 Ft	88	147
7208	111 @ 22000 Ft	-	107	-
Body and Tail-Vertical Gust				
188 (Forebody)	67 @ 12000 Ft	120 @ J2 <b>000 F</b> t	69	118
749 (Forebody)	110 @ 16000 Ft	186 @ 16000 Ft	108	174
720B (Aftbody)	175 € 22000 Ft	-	158	-
Body and Tail-Lateral Gust				
188 (Aftbody)	61 @ 7000 Ft	120 @ 7000 Ft	61	120
749 (Tail)	65 @ 7000 Ft	97 @ 7000 Ft	65	97
720B, Yaw Damper Off (Tail)	99 @ 23000 Ft	-	97	-
7208, Yaw Damper On (Tail)	137 @ 23000 Ft	-	128	-

LIM ULT

O • WING (VERTICAL)

O • WING (VERTICAL)

D • FUSELAGE AND TAIL - VERTICAL

▲ FUSELAGE AND TAIL - LATERAL

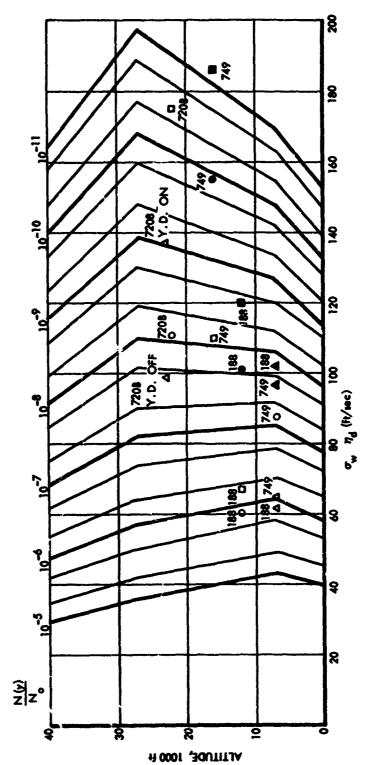


FIGURE 13-3. SUMMARY OF DESIGN ENVELOPE RESULTS

would permit the beam caps and surface material to carry additional load. The increase in limit-strength load due to this mechanism is probably no more than about 5%, however. Previous dynamic gust analysis of the Model 749 indicated an allowable bending moment nearer the wing root, governed by combined tension and shear in the lower surface, that would be reached at less than a 5% increase in the loads found to give a zero margin of safety in the present study.

It should also be borne in mind that, as noted earlier, fuselage loads and fuselage strength were both treated conservatively in the vertical gust analysis of the Model 188 and Model 749. Consequently, for these cases, the actual limit and utlimate strength  $\sigma_w\,\eta_d\,^{\prime}s$  are somewhat higher than indicated, and the actual frequencies of exceedance of limit and ultimate strength are somewhat lower.

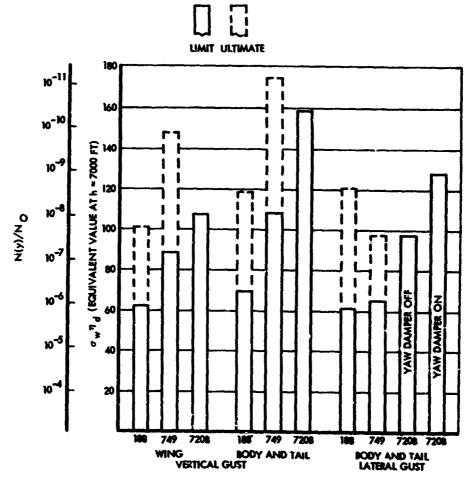


FIGURE 13-4. CONSOLIDATED SUMMARY OF DESIGN ENVELOPE RESULTS

#### 14 EFFECT OF PARAMETER VARIATIONS

#### 14.1 Vertical Gust, Model 188

The effect on loads of changes in airplane and mission profile descriptions has been investigated by variation of a number of the analysis parameters. The parameters selected for variation were those for which precise values might be difficult to obtain during the design stage and which might be expected to have a significant effect on loads. These parameters fall naturally into two categories - first, those descriptive of the airplane itself, and second, those descriptive of the airplane usage in the mission analysis.

 $\overline{A}$  and  $N_O$  values and one-g loads for the various parameter variation cases investigated are listed in detail in Appendix B, Table B-9. Select values are taken from this table for further analysis, comparison, and discussion in Sections 14.1.1 and 14.1.2 following.

14.1.1 Effect of Airplane Description Parameters. In determining the effect on loads of variation in the airplane description parameters, a single airplane condition is used as a reference. Mission analysis case 202, as defined in Table 6-2, was selected for this purpose. As indicated by Figures 9-9 (a) through (d), this leg generally contributed the major part of the total load exceedances. Results based upon this mission segment alone will therefore be applicable, to a close approximation, to the mission analysis as a whole. They should also approximate fairly closely the effect of parameter variations relative to the critical V<sub>C</sub> design envelope condition.

Airplane loads for which the effect of parameter changes are studied are wing loads at wing stations 119 and 346, fuselage loads at fuselage stations 571 and 1000, and accelerations at the center of gravity. The wing torsions are taken about the elastic axis. The bending moment at fuselage station 1000 is also a fairly good measure of tail load, inasmuch as the relieving inertia is only about 30% of the contribution from the tail airload. Where the direction of loading is pertinent, only wing upbending and fuselage downbending loads are considered. The wing and forebody loads are therefore "up gust" loads, and the aftbody loads are "down gust" loads. Except at design dive speed, these are the critical loading directions.

The results of the variations in the airplane description parameters are listed in Tables 14-1, 14-2, and 14-3.

Table 14-1 indicates the proportionate changes in  $\overline{A}$ ; these are simply percentage changes divided by 100. For wing torsions, a percentage expressed in the usual way is relatively meaningless because of the

TABLE 14-1. EFFECT OF PARAMETER VARIATIONS ON A VALUES, MODEL 188 VERTICAL GUST ANALYSIS

	Description of	A Reference -1									
Case	Variation From Reference Case	C.G. Accel		WS 119			WS 3.46		TR 57	1	75 1000
	V		8,	н́х	Х,"	Sg	ĸ	¥ς*	8	Хy	N <sub>y</sub>
202-1	Wing EI Decreased 20%	.004	.003	.007	-•012	.009	.004	008	.003	.002	012
202-2	Wing G Decreased 20%	.007	.016	•019	.010	.014	.025	0	.009	.007	037
202-3	Wing ET and GT Decreased 20%	.on	.028	.028	.002	.028	.030	003	.012	.011	OA1
202-4	Wing FA Shifted Forward 5% C	008	017	017	017	œ1	014	015	011	009	.031
202-5	Mode Desping fidded g = .03	006	020	017	040	-,029	006	042	008	008	~•010
202-6	Airplane CG Shifted .095 Aft	.024	-•ns	006	032	020	.118	026	.069	.085	.207
202-6 Rigid	Rigid - Airplane CG Shifted .09c Aft	.040	.000	.025	032	.019	.039	-,022	.087	.103	.177
202-7	Fuselage Aero Penetration Equal To Wing	-,008	-,008	006	007	008	006	013	005	004	.002
202-7 Rigid	Rigid - Fuselage Aero Penetration Equal to Wing	009	005	-,008	.004	007	009	.004	005	-,003	.021
202-9	Approximate Lift- Leg Function	.012	004	.105	084	a18	.330	089	.024	.ork	024
202-9 Rigid	Rigid Approximate Lift-Lag Function	.017	.017	.023	011	8.20.	.029	006	.a.8	.021	.050
505-70	Hacelle Aero Increased 305	.061	.140	.116	.166	.151	.055	.170	.074	.076	.003
202-10 Rigid	Rigid - Nacelle Aero Increased 30%	.027	.062	.041	.254	.096	005	.234	.030	.030	.004
505-11	Increase Speed From 282 to 324 Knots	.219	.272	.274	.167	.219	.260	.183	.218	.215	.100
202-13	Increase ZPV From 74500 to 86000 Ib	-,066	.265	.175	.138	-159	.102	.110	.145	.185	033
202SF	Stick Fixed No Elevator Notion	.059	.085	.080	.003	.038	.114	012	.153	.187	365

Wor spr all treatment of wing H,, see text.

TABLE 14-2. EFFECT OF PARAMETER VARIATIONS ON  $\rm N_{o}$  VALUES, MODEL 188 VERTICAL GUST ANALYSIS

	Description of	Wo'No Reference									
Case	Variation From Peferance Case	C.G. Accel	1	WB 119		,	NS 346		PS 5	72	PS 1000
			Sg	N <sub>x</sub>	нy	Sg	Жx	Х	S	н	H,
202-1	Wing XI Decreased 20%	1.03	1.02	•93	•99	.94	1.07	.96	1.03	1,02	.94
202-2	Wing GJ Decreased 20%	1.00	1.01	.96	.96	•95	.98	.96	1.00	•99	.83
¿u3	Wing EI and GJ Decreased 20%	1.04	1.03	.90	.94	.90	1,05	.91	1.03	1.02	.80
202-4	Wing EA Shifted Forward 5% C	1.01	1.04	1,03	1.00	1.03	1,05	1.02	1.05	1.08	1,13
202-5	Hode Dumping Added g = .03	•97	<b>.9</b> 8	•97	.98	.98	.98	•99	.98	.99	.97
202-6	Airplane CG Shifted .09c Aft	.97	1,00	.98	1.9+	1.00	.97	1.03	.98	-99	-95
202-6 Rigid	Rigid - Airplane CG Shifted .09c Aft	.96	.94	.94	1.07	.95	.95	1.07	.98	.97	.92
202-7	Puselage Aero Penetrition Equal to Ming	1.01	•99	1,00	1.00	1,00	1,01	•99	1,00	1.01	1.07
202-7 Rigid	Rigid - Fuselage Aero Penetration Equal to Wing	1,04	<b>.</b> 97	.98	.96	.98	1,00	.96	1.01	1,02	1.07
202-9	Approximate Lift- leg Function	.97	.92	•95	1,00	.96	.89	.98	1,00	1,02	1,00
202-9 Rigid	Rigid - Approximate Lift-Lag Function	•97	.91	.88	1.11	.88	.87	1.14	.97	1.01	1.20
202-10	Nacelle Aero Increased 30%	•99	•99	•99	.83	.98	1.03	.91	1.03	1.02	1.04
202-10 Rigid	Rigid - Nacelle Acro Increased 30%	1.02	1,02	1,02	.84	1.04	1.01	•77	1,02	1.02	1.04
505-17	Increase Speed From 282 to 324 Knots	1,06	1.01	.98	.97	.97	1.00	.șô	1,06	1.05	.88
202-13	Increase ZFW From 74500 to 86000 lb	•95	.90	.94	.89	.93	.93	42 <b>.</b>	-95	.92	-95
20287	Stick Fixed-lio Elevator Notica	.86	.96	.92	1,08	.97	.88	1.04	.97	.98	.53

TABLE 14-3. EFFECT OF PARAMETER VARIATIONS ON EFFECTIVE A VALUES, MODEL 188 VERTICAL GUST ANALYSIS

	Description of	T Rifective - 1									
Case	Yariation From Reference Case	C.G. Accel WS 119		l v	ls 346		<b>PS</b> 51	n	PS 1000		
			Sg	ĸx	μλ.	S <sub>2</sub>	××	<del>ሃ</del> ታ	8,	1,4	Ny
205-1	Wing El Decreased 20%	.011	.თ.ნ	009	014	00k	.021	017	.009	.006	025
202-2	Win, GJ Decreased 20%	.008	.თა	.009	.001	.002	.021	009	.009	.004	075
202-3	Wing KI and GJ Decreased 20%	•019	.035	.002	010	.005	.042	023	.020	,015	086
202-h	Wing EA Shifted Forward 5% C	006	009	011	017	015	003	011	٥	.008	.058
202-5	Node Damping Added g = +03	013	-,026	023	044	033	-•010	044	012	008	- <b>.0</b> 16
202-6	Airplane C.G. Shifted .098 Aft	.018	317	011	024	021	.010	020	.065	.085	.194
202-6 Rigid	Rigid - Airplane CG Shifted .097 Aft	.030	~.003	.014	019	.008	.028	-,008	.053	.099	.162
202-7	Fuselage Aero Penetration Equal To Wing	005	010	006	-,007	009	003	- <b>.</b> 015	005	001	.016
202-7 Rigid	Rigid - Puselage Aero F metration Equal to Wing	0	012	009	904	015	008	-,005	004	۰	.031
202-9	Approximate Lift- leg Function	.00k	023	.003	-,584	028	.002	093	.014	.018	024
202-9 Rigid	Rigid - Approximate Lift-leg Function	•000	002	003	.009	009	.002	.020	.013	.022	.080
202-10	Nacelle Aero Increased 30%	•057	.138	.114	.123	.154	.062	.147	.082	Bo.	.011
202-10 Rigid	Rigid - Macelle Aero Incressed 30%	•033	.085	.045	.230	.103	003	.166	.033	.032	.010
505-17	Increase Speed From 282 to 324 Knots	.248	276	.269	.160	.270	.261	.178	.235	.230	.090
202-13	Increase ZFW Prom 74500 to 85000 Lb	068	•235	.157	.134	.140	.083	.096	.131	.161	044
202SF	Stick Figed-No Elevator Motion	,020	.074	.066	.019	.030	.030	004	.245	.162	449

For special treatment of wing  $\mathbf{N}_{\mathbf{y},\mathbf{r}}$  see text.

possibility of a value close to zero for the reference case. Instead, the proportionate change in the torsion A is obtained by dividing the actual change by an appropriate measure of the allowable strength in torsion. This measure is obtained by multiplying the reference case shear A at the given wing station by the ratio of maximum design torsion to maximum design shear at that station. The ratios of maximum design torsion to maximum design shear used for this purpose are 100 inches at wing station 119 and 91 inches at wing station 346.

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Table 14-1 is primarily of interest with respect to the design envelope oriterion, as A is a direct measure of the gust increment of load in this application.

In Table 14-2, the effect of the parameter variations on  $N_O$  is indicated by ratios of  $N_O$  to reference case  $N_O$ . It should be emphasized that large percentage changes in  $N_O$  have a far smaller percentage effect on loads. For example, Figure 13-2 indicates that a change in  $N_O$  by a factor of 2 results in only about a 5% change in load at a given frequency of exceedence.

To indicate the combined effect of changes in  $\overline{A}$  and  $N_O$  on mission analysis gust incremental loads, "effective" A changes are shown in Table 14-3. These "effective" A changes include not only the effect of the A change itself but also the effect of the No change on the incremental load at a given frequency of exceedance. The No contribution was obtained by calculating the increase or decrease in A required to exactly offset the increase or decrease in No\_at a load exceedence level of 10-5 exceedences per hour. The effective A change thus calculated was then divided by the reference case  $\overline{A}$  to indicate the proportionate change. Reference case wing torsion A's were defined in the same special way in preparing Table 14-3 as in preparing Table 14-1. Generally the effective A changes indicated by Table 14-3 are very nearly the same as the actual A changes indicated by Table 14-1. It should be remarked that the effect of parameter changes on the one-g loads is not included in the information provided in any of the three tables. It was felt that the relative effects of a parameter change on the gust increment and on the one-g loads could well be peculiar to a given configuration and that in the present study emphasis should be placed on the effect on the gust increment.

The magnitudes of the parameter variations for which load changes are indicated in Tables 14-1 through 14-3 are rather arbitrary. They do not necessarily bear any particular relation to the expected uncertainty in establishing values for use in the analysis, and in all cases a sufficient variation was selected to assure that the differences indicated would not be clouded by possible inaccuracies in the solutions.

In cases 201-1, 202-2, and 202-3, the wing stiffness was decreased by 20 percent, first in bending, then in torsion, and finally in both

bending and torsion. These stiffness changes are fairly sizeable, and design-stage calculations would probably give stiffnesses closer to actual values, in most instances, than reflected by the differences considered here. As can be seen from Table 14-1, the  $\overline{A}$ 's are affected very little by these changes. The average change is approximately 2-1/2 percent, with a decrease in stiffness giving an increase in load. Table 14-3 shows comparable small changes in the effective  $\overline{A}$  values.

In case 202-4, the position of the wing elastic axis was shifted forward 5 percent of the local chord. This amounts to ll inches at the root and 5 inches at the tip. Design-stage calculations would be expected to locate the elastic axis to within 2 or 3 percent chord. Torsions are compared using the reference case elastic axis as the load axis in both cases. The effects of this variation are also seen to be small, averaging 2 percent on either an  $\overline{A}$  or effective  $\overline{A}$  basis.

Case 202-5 indicates the effect of adding structural damping in the wing bendin; and torsion modes. A structural damping coefficient of .03 was used; this is the value of g in the expression (1 + ig)k and corresponds, at the resonant frequency, to a relative viscous damping of .015. This value is probably close to what is actually present. It also probably represents about the expected degree of uncertainty in establishing a value for design use. The effect is seen to be about a 2 percent reduction in incremental loads.

In case 202-6, the airplane center of gravity is moved aft 9 percent of the mean aerodynamic chord. This is 15 inches and is roughly half the available range of travel between forward and aft limits. This case serves two purposes. Besides giving an indication of the effect of a change in airplane center of gravity, it also indicates the effect of a change in the static stability of the airplane. In interpreting the results of this change, it should be noted that fuselage panel weights were not changed. Thus the fuselage load changes reflect the effect of the stability change, or of a change in wing center of gravity, but do not realistically reflect the effect of varying the c.g. position by moving payload.

In a design envelope analysis, the c.g. position can be regarded as known precisely. In a mission analysis, it can probably be estimated to within at most 5 percent of the mean aerodynamic chord and perhaps usually somewhat closer. The static stability would probably be known to within about 3 to 5 percent of mean aerodynamic chord.

The rather large change investigated results in only about a 2 percent change in the incremental wing loads. This change is an increase and results from the lower natural frequency of the short-period mode due to the decreased static stability. If this change results from an actual center of gravity shift, it will tend to be offset by a decrease in the one-g flight loads due to a shift of load from the wing to the tail.

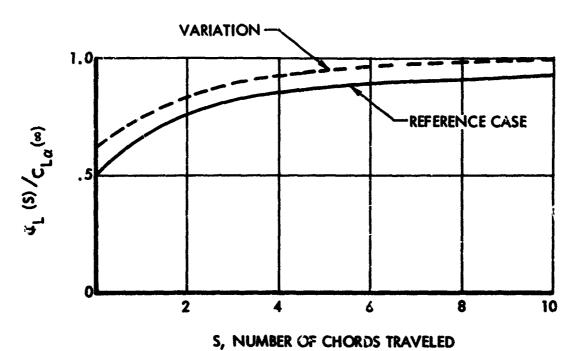
The change in loads on the forebody is somewhat greater, amounting to about 8 percent. This may be due primarily to a first order effect noted in determining design discrete-gust loads. If the wing and tail are assumed to encounter the gust simultaneously, a sizeable pitch acceleration is produced by the offset between the airplane aerodynamic center and the center of gravity. As the center of gravity moves aft (or the aerodynamic center forward), there is an increase in nose-up pitching acceleration on the forebody (or a decrease in nose-down pitching acceleration), resulting in an increase in the down inertia forces. It is quite interesting to note that the fuselage bending moment at station 1000, which is also a measure of the tail load, increases much more markedly still, by about 19 percent. This may be due to the lower short-period frequency, which delays and/or reduces the development of pitch velocity which would alleviate the tail angle of attack produced by the gust. This parameter change was investigated on both a flexible-airplane and a rigid-airplane basis; the effects are seen to be comparable. As in all cases where a rigid airplane as well as a flexible airplane comparison is shown, the reference loads for the rigid-airplane comparison are obtained for the rigid-airplane.

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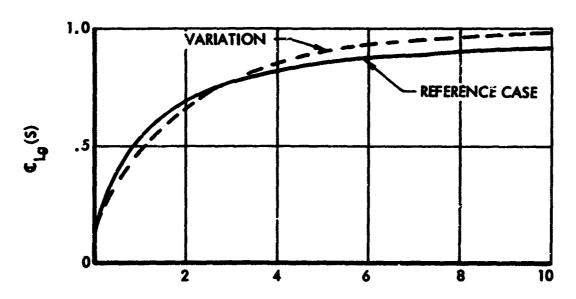
Case 202-7 indicates the changes in wing and aftbody loads that might result from inability to properly distribute the fuselage airloads and account for the earlier penetration of the nose into the gust. In the reference analysis, what is believed to be a realistic representation was used. Case 202-7 indicates the effect of shifting the forebody lift back to the region of the wing, while retaining the same static stability. It is seen that the effect on the loads is very small, averaging less than 1 percent.

Case 202-9 shows the effect of changes in the unsteady lift growth functions used in the analysis. A comparison of the lift growth functions used in the reference case and in case 202-9 is shown, on an indicial basis, in Figure 14-1. The functions used in the reference case are two and three term exponential approximations to the Wagner and Kussner functions respectively, matching the theoretical functions for the low Mach number, high aspect ratio case. The functions used in case 202-9 are one-term approximations selected to better reflect the actual Mach number and aspect ratio of the Model 188 (M = .53 at case 202 speed and altitude, AR = 7.5). The results shown in Tables 14-1 and 14-3 indicate that this particular set of changes has a quite negligible effect on loads. It might be remarked, however, that at substantially higher Mach numbers and lower aspect ratios, the lift growth functions may depart substantially from those shown in Figure 14-1, and considerably more variation in load could result from use of unrealistic data.

Case 202-10 indicates the effect of a 30 percent increase in the aerodynamic forces on the propellers and the forward portions of the nacelles. The airplane static stability was unchanged. This variation was



(a) WAGNER FUNCTION



S, NUMBER OF CHORDS TRAVELED

(b) KUSSNER FUNCTION FIGURE 14-1. LIFT-LAG FUNCTIONS USED IN PARAMETER VARIATION STUDY introduced as a result of difficulty encountered in the design of the Model 188 in securing sufficiently reliable data on pitching moment inputs to the wing due to the nacelles and propellers. With proper recognition of the problem, it would appear that nacelle and propeller aerodynamic forces should be predictable in the design stage to within 15 or 20 percent. It might be noted, too, that in the design of the Model 188, it was the pitching moments, rather than the forces, that were difficult to evaluate, whereas in case 202-10 both were increased in the same proportion.

Fairly substantial load increases are seen to result from this change. On a rigid airplane basis, the torsions and shears both increased significantly, due to the direct effect of the additional airload input at the nacelles. It might be noted, incidentally, that the percentage increases in forebody load and in c.g. acceleration are roughly the same as the 3.1% increase in airplane  $C_{Lq}$  due to the additional nacelle airload. For the flexible airplane, although the increase in the torsions is somewhat less, the other loads generally increase by about twice as much as for the rigid airplane. Examination of the power-spectral density curves for c.g. acceleration and wing station 119 bending moment indicates that about half this increase is due to static aeroelastic effects and half due to first elastic mode response. To place these rather large increases in perspective, it should be noted that the Model 188, as a very highly powered propjet airplane, develops nacelle aerodynamic forces that are unusually large in comparison with other airplanes, especially the pure jets.

Cases 202-11 and 202-13 were calculated primarily for the investigation of the effects of speed and payload assumptions on the mission analysis results, as described in the next section. They are included in Tables 14-1 through 14-3 as a matter of interest and convenience.

The 15% speed increase reflected by Case 202-11 is seen to produce sizeable load increases. The c.g. acceleration increase of 22% is closely in accordance with the 15% increase in speed and the 6% increase in CLq due to the higher Mach number. The various wing loads generally increase by somewhat larger percentages. It is interesting to note, and will become evident in the next section, that the increase in gust incremental wing loads is substantially offset by a reduction in the one-g flight loads due to a greater aeroelastic nose-down wing twist at the higher speed.

The increase in payload to the placard amount, reflected by case 202-13, is also seen to result in fairly sizeable wing load increases; the effect on one-g loads is actually by a somewhat larger percent.

Case 202-SF indicates the effect of a "stick-fixed," relative to a "stick-free," pilot technique. It is seen that, with the stick fixed,

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the effective A's for wing loads increase by from roughly 3 to 8%. This results primarily from the reduction in static stability due to the loss of the effect of the control column bob weight. An even greater increase is indicated for the forebody loads, which is consistent with the effect of a static stability change as shown by Case 202-6.

14.1.2 Effect of Mission Description Parameters. The effect on loads of changes to the mission profile description is investigated by changing a number of the pertinent mission profile characteristics in turn. Several of the changes considered could be investigated without analysis of additional flight conditions Three additional flight conditions, however, required analysis. Two of these cases, 202-11 and 202-13, are listed in Tables 14-1 through 14-3. The third, case 202-12, consists of case 202 with altitude increased to 16,500 ft. and equivalent air speed decreased to 258 knots.

The effect of these changes on loads is measured by comparing net loads calculated with and without the mission change, at a frequency at exceedence of  $10^{-5}$  exceedences per hour. Loads are compared at the same locations as in the preceding section. The results of the changes in mission description are given in Table 14-4 as ratios of load after the change to load before the change. For wing torsions, because of the possibility of a reference value close to zero, increments instead of ratios are given. To place these increments in perspective, it is noted that the limit design wing torsions are approximately -5.0 x  $10^{5}$  in. lb. at wing station 346.

As in Section 14.1.1, the magnitudes of the parameter changes selected for investigation are rather arbitrary and the significance of each must be considered individually.

The first modification made was to consider the airplane to be used 100% of the time in the short-range, non-fuel-through mission defined in Table 6-1. Although this mission accounts for only 28% of the total flight hours, it was found to be the major contributor to the load exceedences. A surprisingly small increase in load resulted, averaging only about 3%. It should be pointed out, however, that a converse change, namely operation 100% of the time in a long-range-mission, might be expected to have a slightly greater effect, as indicated by the next case considered.

In case 2, using the case I mission as a reference, the cruise altitude was increased from 11000 to 16500 ft. The cruise speed was also modified, in accordance with Figure 6-4. The climb and descent times were increased realistically. Load calculations were carried out assuming all flight time to be in this short mission. It is seen that the increase in cruise altitude results in a load reduction of about 9%.

TABLE 14-4. EFFECT OF MISSION FROFILF VARIATIONS ON NET LOADS AT N(y) = 10-5 CYCLES PER HOUR, MODEL 188 VERTICAL GUST ANALYSIS

		;	TYTA	VERTICAL GUST ANALYSIS	UST AN	ALYSIS				
				Net Wi (U2) Be	Net Wing Load (U. Bending)			α)	Net Fuselage (Down Bending)	je (8)
Case	Profile Variation	စ	_] }	X N	_×l	A My Change Inlet Load (10 <sup>6</sup> In.Lb)	nge oad .Lb)	20 S	×,	X X
		WE 119	946 8W	911 8W	346 SW	VB 119	NS 346	172 87	Τ.	FS 1000
٦.	Chauge to Short Range Flights	1.030	1.007	1.038	1,000	60°-	20	1,047	1.048	1.038
OJ.	Change in Cruise Altitude From 11000 to 16500 Ft	.913	.913	. 898	•937	• 070	090*	1,022	1.046	.893
m	Change in Cruise Speed From 282 to 324 Knots (Short Range)	1,129	7*096	1,056	1,057	520°	æ90 <b>∙-</b>	1,318	1.327	1,170
æ	Change Payload to Give Min. Zero Fuel Weight	1.250	1.184	1,180	1.148	.510	- 292	1,225	1,262	.980
5	Increase Reserve Fuel From 11000 to 17000 1b	066•	1.042	1,000	1.042	• 050	.030	.927	.997	ήη <b>6</b> •
9	Effect of 10 Min Additional Hold Time Each Flight	966*	•993	.992	ή66•	010	020	•992	•990	.996
7	Increase Descent Legs From Two to Four	1.020	066•	1.010	1,005	.160	0	1	l	1

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In case 3, the cruise speed was increased to the Vc placard. Again, the case 1 mission was used as a reference: No change was made in descent speed, as the descent segment contributed rather negligibly to the load exposure. It is believed that average cruise speeds can probably be estimated to within about 5% in the design stage, which is only one-third of the variation reflected by the case 3 figures. Table 14-4 indicates that wing loads increased only 6 to 12% due to the 15% speed increase in comparison with the 16 to 28% increase shown for case 202-11 in Table 14-3. The smaller increase here is due to the offsetting changes in the one-g flight loads. The forebody loads, on the other hand, do not benefit from a reduction in the one-g flight contribution, and still show sizeable increases.

Case 4 considers the effect of increasing the payload to a value as limited by the placard zero fuel weight. The zero fuel weight thus increases from 74500 lbs. to 86000 lb., or by 16%. The payload increases from 12500 lb. to 24000 lb. or by 92%. The gross weight at the midpoint of cruise increases from 87500 lb. to 99000 lb., or by 13%. The comparison is again based on the short-range-mission alone. Payload is probably the most difficult of all mission description parameters to predict accurately. However, it is believed that predictions of average payload should be reliable to within about 15% of total payload, or about one-third the variation made here. The figures in Table 14-4 show increases in wing net load of 15 to 25% and comparable increases in fuselage net load. Comparing the results of Table 14-4 with those of 14-3, it is seen that the net loads increase by somewhat greater percentages than the gust increments because of the relatively greater effect of zero fuel weight on one-g loads than on the gust increment.

In case 5, the assumed reserve fuel is increased from 11000 lb. to 17000 lb. The average reserve fuel quantity can probably be predicted to within about half this increment. The comparison is again based on the short range mission alone. It is seen that outer wing loads, where the increased inertia relief due to the added fuel is less effective, increase about 4%, while the inner wing loads remain approximately constant. Fuselage forebody loads actually decrease due to the lower acceleration at the higher gross weight.

In case 6, a low speed holding time of 10 minutes is added to each of the 5 missions included in the overall operation of the airplane as defined in Table 6-1. The comparison, of course, is based on the overall mission. The decrease in loads is generally less than 1%. This result is to be expected, and in fact, illustrates the relation between loads and exceedances indicated by Figure 13-1. The increase in flight time per 100 flights is from 6850 minutes to 7850 minutes, or in the ratio 1.15; therefore, the overall N(y) will decrease in the ratio 1/1.15, and, as indicated by Figure 13-2, the loads decrease by less than 1%.

Case 7 was included to determine whether a finer breakdown into mission segments might be required. A relatively extreme case is considered. The descent from 16000 ft. in the fuel-through 100-minute flight described in Table 6-1, was originally broken into only two segments for analysis. Over this altitude range, however, both the speed and the turbulence parameters vary markedly. Consequently, it appeared that a finer breakdown might be necessary to adequately determine the \_rd exceedance relationship. This descent leg was therefore broken into four segments, lumped at altitudes of 13500, 10000, 7000, and 2000 ft. (For this analysis, only one additional case was required, No. 207-1; this case was the same as No. 207 except that the altitude was changed to 2000 ft. and the speed to 202 knots.) The resulting load comparisons, based upon the descent leg of this one mission, are shown in Table 14-4. Going to the finer breakdown is seen to have only about a 1% effect on the loads. Moreover, for the Model 188 the descent leg actually accounts for only a minor fraction of the load exceedances, and the resulting effect on the total mission loads would be much smaller still.

### 14.2 Lateral Gust, Model 188

Because of the expected greater susceptibility of swept wing airplanes to lateral gust parameter changes, the major coverage of the lateral gust part of the parameter variation program was conducted based on the Model 720B.

The effects of certain parameter changes for the Model 188, however, were also considered to be of interest.

In Section 8.2.2, the effects of various pilot techniques were investigated, in order to assure that the dynamic analysis of the reference airplanes would be on a sound basis. Also, for the same purpose, the sensitivity of the lateral gust loads to the rate of growth of the lift produced by change in angle of attack was investigated; the sensitivity was found to be much greater than would have been expected, and accordingly a more realistic lift growth function was incorrected into the analysis.

An additional parameter of which the effect of variations is of interest is the Dutch roll damping. Variations in damping were introduced by introducing into the analysis a fictitious yaw damper giving a yaw couple proportional to yaw velocity. Values of damper coefficient, expressed in the form  $(b/2V)(C_{n,j,damper}/C_{n,j,tail})$ , of -.1, +.2, and +.5 were investigated. Missical analysis case 201 was used as a reference, and the lift growth functions used were the original functions before the above-described modification was incorporated. The results are shown in Figure 14-2. To obtain the damping values at which the fin A's were plotted, a stability solution of the equations of motion was first obtained, with instantaneous lift growth assumed. A constant  $\Delta \zeta$  was then

subtracted to account for the effect of the lag in the lift growth. This decrement in  $\zeta$  was selected such that the relation of  $\overline{A}$  values for fin side load for the two lowest- $\zeta$  cases in Figure 14-2 was in accordance with the simple theoretical relationship,  $\overline{A} \propto \zeta^{-1/2}$ . The decrement in  $\zeta$  was also very close to the value inferred by applying this relationship to fin side load  $\overline{A}$ 's given by analyses with and without the lift lag functions included.

At low  $\zeta$  values, the theoretical proportionality is seen to apply quite closely. But as  $\zeta$  increases beyond about .2, the tail load begins to decrease much more slowly. This result is qualitatively in agreement with Figure 1 of Reference 25, although there the leveling off occurs at a slightly lower  $\zeta$ . (To convert the scale used in Figure 1 of Reference 25 to a  $\zeta$  scale, it can be noted that the quantity  $1/c_1/2$  used therein is equal to approximately 9.0  $\zeta$ ).

#### 14.3 Vertical and Lateral Gust, Model 720B

The effects of variations of various parameters on the vertical and lateral gust loads of the Model 720B are discussed in Reference 1.

## 14.4 Effect of Mathematical Model, Model 749

In addition to variations in method or input data that can be investigated utilizing a given mathematical model, there are also subtle differences amongst various mathematical models, even when the models may all be of the same general level of complexity. In order to gain an impression as to the differences in loads that might result from this source,  $\overline{A}$  and  $N_0$  values for wing loads and ai plane c.g. accelerations were obtained for the Model 749 by means of both the Lockheed and Boeing mathematical models. Mission analysis case 106, as defined in Section 6, was used for this comparison.

Inasmuch as the Boeing model did not include provision for nacelle structural damping or elevator float, it was decided that the comparison should be based upon analyses in which the nacelle structural damping was assumed zero and the elevator was considered fixed. Accordingly, the Lockheed analysis was repeated on this basis. This analysis is designated Case 106x.

In addition, in conducting the Boeing analysis, it was found impractical to represent the nacelle and propeller aerodynamics and to include aerodynamic pitching moments on a rigid fuselage. As a result, in the Boeing analysis, the nacelle and propeller aerodynamic forces were

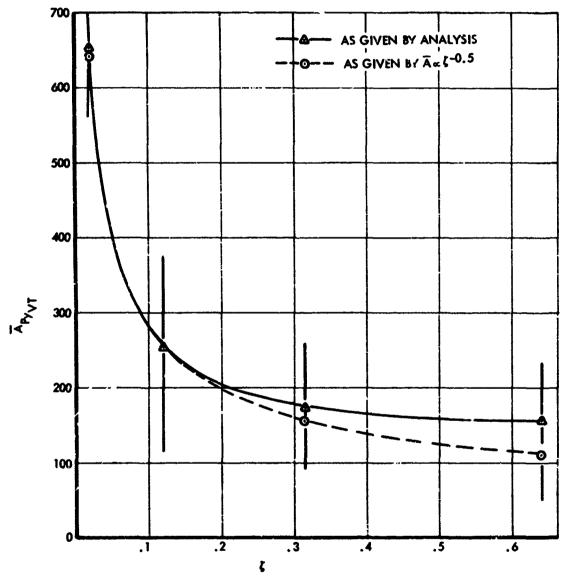


FIGURE 14-2. EFFECT OF DUTCH ROLL DAMPING ON TAIL LOAD

applied to the fuselage. Fuselage lift was then lumped with the innermost wing segment and the tail was relocated in order to maintain the proper total-airplane pitching moment derivative, dC<sub>m</sub>/d<sub>a</sub>. Moreover, since the Boeing analysis treated wing and tail induction effects on a unified interest basis, it inferred a value of wing downwash at the tail is trappened not to agree with that given by the Lockheed sources. In the difference in downwash given by the two analyses and thus maintain the same tail lift due to a change in airplane angle of attack. The Lockheed analysis was also performed with these additional changes, in order to provide the most meaningful comparison. The resulting case is designated 106y. The actual differences in input data between Cases 106x and 106y are indicated by the following summary, in which all CLovalues are referenced to the wing area and 1/c designates the distance in wing chords from the wing elastic axis to the tail aerodynamic center:

	Case 106x	Case 106y
C <sub>L<sub>a</sub></sub> , wing	5.17	5.28
CLa, nacelles (total for four)	.21	0
C <sub>La</sub> , nose	.10	0
CLa fuselage center section	49	18
$^{\mathtt{C}}_{\mathtt{L}_{\boldsymbol{\alpha}}}$ , tail	1.09	1.65
$1 - c \epsilon / d_{\alpha}$ , tail	.60	·33
$(C_{L_{\alpha}})(1 - de/d_{\alpha})$ , tail	.65	-54
$\mathtt{C}_{\mathtt{L}_{m{a}}}$ , total for airplane	5.64	5.64
<b>£</b> /c	3.32	2.31
Short period undamped natural frequency, cps	.46	.44
Short period damping ratio, (	•73	70

The short period frequency and damping values given are computed on the basis of instantaneous lift growth.

A and  $N_{\rm O}$  values obtained by the Lockheed analysis for cases 106x and 106y are listed in Table B-3 (Appendix B).

 $\overline{A}$  values given by the Boeing analysis and by the corresponding Lockheed analysis (Case 106y) are compared in Figure 14-3. The N<sub>O</sub> values are compared in Figure 14-4. The N<sub>O</sub> values are seen to agree excellently. The  $\overline{A}$  values agree in the general shape of the spanwise variations, but the Boeing values are significantly higher. At W.S. 191, indicated in Section E.2.2 (Appendix E) to be the critical location in the wing, the Boeing  $\overline{A}$ 's are about 1.36 times the Lockheed values.

To provide a rough indication of the source of this difference - that is, whether it is in the rigid airplane or elastic mode response characteristics - the comparison of A values is repeated on a rigid airplane basis in Figure 14-5. ("Static-elastic" values as given by the Boeing analysis are also shown, as a matter of interest; these are obtained by setting equal to zero, in the analysis, all forces, aerodynamic and inertia, produced by velocities and accelerations in the elastic modes.) It is seen that the percentage differences between the Boeing and Lockheed analyses are substantial on a rigid airplane as well as a flexible airplane basis. Although the exact percentages vary somewhat with the spanwise location and with the load quantity, it appears that, on the average, differences in elastic mode response would account for about a 5 percent difference between Boeing and Lockheed A values; the balance of the difference in the flexible-airplane values is then due to the differences in rigid-airplane response characteristics.

The differences in elastic mode response may be due largely to the reduced aerodynamic damping in the Boeing analysis due to the inclusion of aerodynamic induction effects in the elastic mode response. In the Lockheed analysis, strip theory is used, with panel  $C_{L\alpha}$  values taken so as to give the correct lifts when the entire wing is given an increment in angle of attack. These values are too high, however, to define correctly the forces due to motions in the elastic modes. For motion in the first bending mode, for example, the two nodal points are comparable to additional wing tips, in separating position pressure and negative pressure regions; as a result, an effective aspect ratio, for roughly estimating the reduction in  $C_{L\alpha}$  due to spanwise flow, for motion in this mode, would be only 1/3 of the actual aspect ratio of the complete wing. Consequently, the actual aerodynamic damping is somewhat less than obtained by the strip theory analysis.

Good qualitative agreement of the elastic mode responses between the two analyses is indicated by plots of the various power-spectral density functions (not shown). The frequencies of the various elastic mode response peaks were found to agree very closely, and the general shapes of the curves were quite similar.

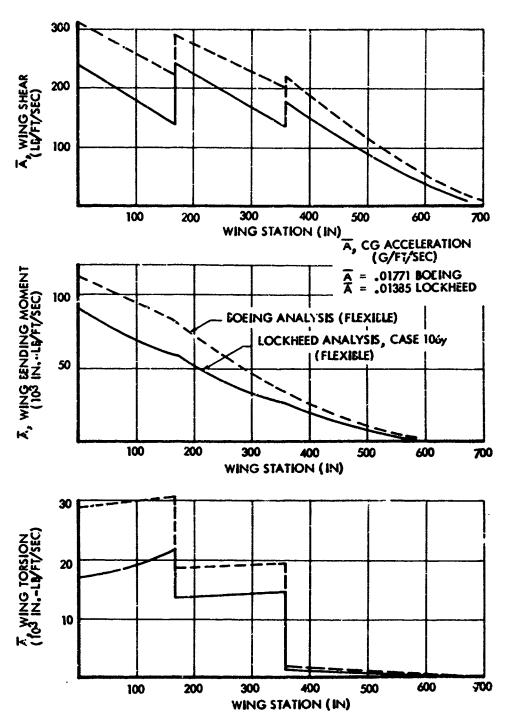
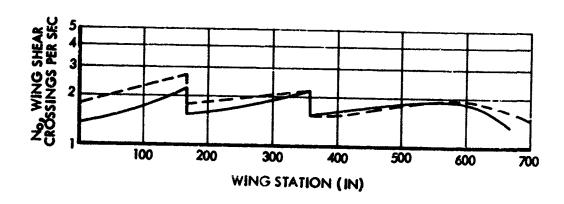
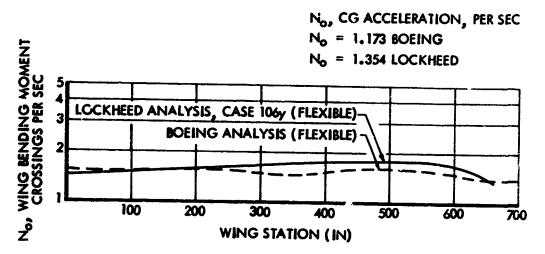


FIGURE 14-3 COMPARISON OF  $\overline{A}$  VALUES GIVEN BY BOEING AND LOCKHEED ANALYSIS OF THE MODEL 749





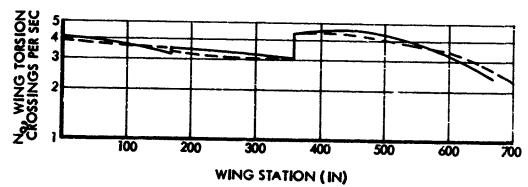


FIGURE 14-4. COMPARISON OF NO VALUES GIVEN BY BOEING AND LOCKHEED ANALYSIS OF THE MODEL 749

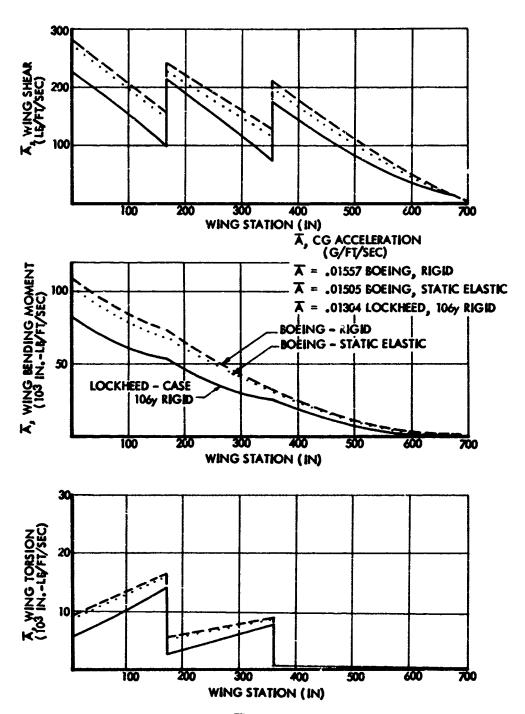


FIGURE 14-5. COMPARISON OF  $\overline{A}$  VALUES GIVEN BY BOEING AND LOCKHEED ANALYSES OF THE MODEL 749 - RIGID AND STATIC ELASTIC ANALYSES

The reasons for the sizeable differences in the rigid-airplane results are not clear. In an effort to gain an understanding of these differences, the rigid airplane analysis was repeated making various changes in the treatment of the aerodynamics. For this purpose, use was made of a separate two-degree-of-freedom mathematical model. In this model, the airplane is free to plunge and pitch. The airplane is broken down into several aerodynamic elements, such as wing, tail, nose, and remainder of the fuselage. Gust penetration, transient lift growth, and downwash are handled separately for each element. Analyses were conducted for both the "Lockheed Configuration," Case 106x, and the "Boeing Configuration", Case 106y.

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Results are shown by means of plots of power-spectral density of c.g. acceleration in Figures 14-6, 14-7, and 14-8, and tabulations of  $\overline{A}$  for c.g. acceleration in Table 14-5.

A comparison of power spectral densities for the Boeing analysis and the directly comparable Lockheed analysis is shown first, in Figure 14-6.

In Figure 14-7, comparisons of ten-degree-of-freedom (rigid) with two-degree-of-freedom power spectral densities are made, in order to provide a check of the ten-degree-of-freedom results. For Case 106y, the Ā values agree to within 1 percent and the power spectral densities are also in reasonably close agreement. For Case 106x, the two analyses are in less exact agreement, with the Ā values differing by about 7 percent. The possibility of the differences being due to the use of local wing chord as a basis for the transient lift growth in the ten-degree-of-freedom analysis was investigated by repeating the ten-degree-of-freedom analysis basing all wing lift growths on the mean aerodynamic chord as in the two-degree-of-freedom analysis; the effect of this change, however, was found to be slight.

It is also interesting to note from Figure 14-7 that Cases 106x and 106y differ considerably from each other in c.g. acceleration  $\overline{A}$  values and power spectral densities - even through the mass parameter, mean chord, and short period frequency and damping are virtually identical for both cases.

Figure 14-8 shows the effect on Case 106y results of various changes in the lift growth and downwash assumptions. The effects of the transient lift growth assumptions are seen by comparing curves A, B. C, D, and E. The peculiar two-hump shape displayed by Curve A (the basic case, also shown in Figures 14-6 and 14-7) is seen to result from introduction of the Wagner lift growth function. A plot of the Wagner function vs frequency, however, does not show any obvious reason why such humps should appear.

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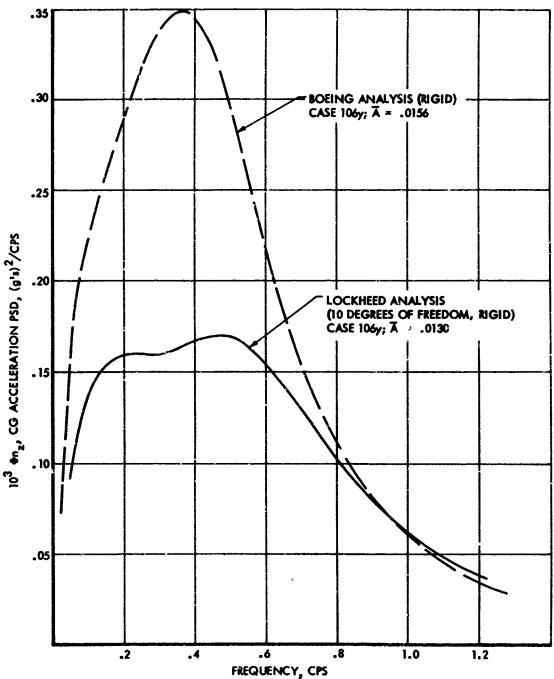


FIGURE 14-6. COMPARISON OF POWER SPECTRAL DENSITY OF CG ACCELERATION AS GIVEN BY BOEING AND LOCKHEED ANALYSES, MODEL 749

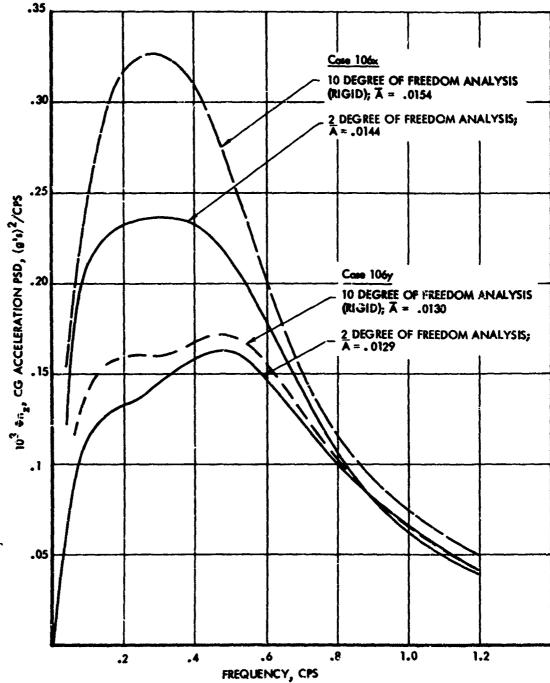
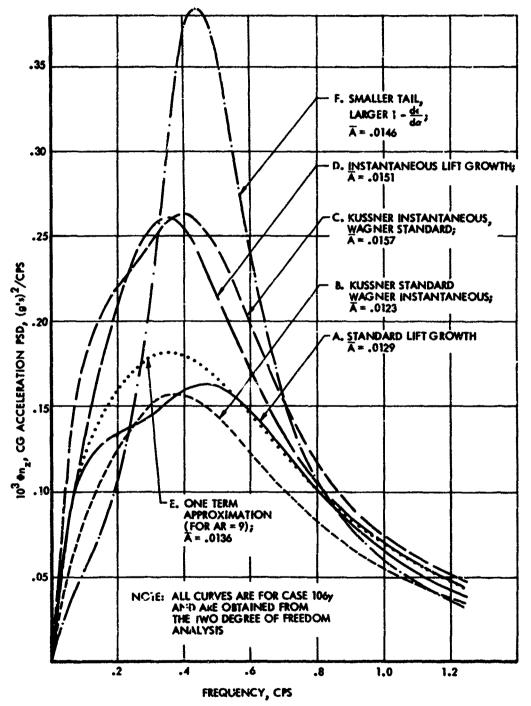


FIGURE 14-7. COMPARISON OF POWER SPECTRAL DENSITY OF CG ACCELERATION AS GIVEN BY TWO AND TEN DEGREE OF FREEDOM ANALYSES, MODEL 749



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FIGURE 14-8. EFFECT OF LIFT GROWTH AND DOWNWASH ASSUMPTIONS ON POWER SPECTRAL DENSITY OF CG ACCELERATION, MODEL 749

EFFECT OF ANALYSIS ASSUMPTIONS ON RELATIVE & VALUES FOR CG ACCELERATION, MODEL 749, CASE 106 **TABLE 14-5.** 

						Relative A*	**	
Case	Analysis	Lift or	Lift Growth Assumptions	35	Case 106x		1	Case 105y
		Kussner Function	Wegner Function	Wing Chord	(Lockheed Configuration	(Lockheed Configuration)	(Bot Config	(Boeing Configuration)
					Free to Plunge Only	Free to Flunge and Pitch	Free to Plunge Only	Free to Flunge and Pitch
<	2 DOF	3-Term	2-Term	MAC	8.	68.	1.00	8.
м	2 DOF	3-Term	Instantaneous	MAC	.95	8.	×.	.76
U	2 DOF	Instantaneous	2-Term	MAC	1.08	1.07	1.09	86.
A	2 DOF	Instantaneous	Instantaneous	MAC	1.04	1.04	7.6	₹.
ы	2 DOF	1-Term	1-Term	MAC	•	ı	1.02	₫.
Ł	2 DOF	3-Term	2-Term	MAC	•	•	3.00	ъ.
o	10 DOF Rigid	3-Term	2-Term	<b>K</b>	,	%.	ı	.83
×	10 DOF Rigid	3-Term	2-Term	Local C	•	%	,	.81
н	Boeing Rigid	As described in App Reference 1	As described in Appendix A of Reference i	- 4.	•	ı	•	76.

\*Relative  $\overline{A}$  of 1.00 corresponds to  $\overline{A}$  of .0161 g's/fps. \*\*In case  $\overline{F}$ , tail area is divided by 1.83 and (1 -  $d\varepsilon/da$ ) is multiplied by 1.83.

Inasmuch as the two-hump shape was much less pronounced for Case 106x than for Case 106y, it appeared that the difference in wing downwash assumptions between the two cases might be a significant factor in determining whether the Wagner lift growth would produce such a shape. Consequently, a case was run in which the tail area and the wing downwash at the tail were changed to the values associated with Case 106x, while the tail location was retained as in Case 106y. The result is shown by Curve F. For this case, the short perior frequency decreased slightly, to .42 eps. The damping ratio,  $\zeta$ , however decreased markedly, to .46.

While these results do not point to concrete conclusions, they do suggest that the differences between Boeing and Lockheed  $\overline{A}$  values might be due to an inter-related effect of differences in treatment of transient lift growth and aerodynamic induction. If the  $\overline{A}$  differences are indeed due to such a cause, rigid-airplane gust load factors are very much more sensitive to the assumptions made in these areas than had been realized heretofore.

The difference in rigid-airplane  $\overline{A}$  values between the Boeing and Lockheed analyses tends to be somewhat greater for wing load quantities, especially for bending moment in the critical region, than it does for e.g. acceleration (ratio of 1.36 vs 1.28). As a result, it appears that part of the difference in wing load  $\overline{A}$ 's may be due to a difference in the way in which the wing was divided into panels for analysis and masses and aerodynamic forces assigned to these panels.

The lack of closer agreement between the Bosing and Lockheed analyses does, of course, raise the question of the adequacy of the analyses upon which the calculated limit-strength values of N(y) and  $\sigma_{\rm W}$   $\eta_{\rm d}$  for the three reference airplanes were calculated. It might appear that the Poeing analysis, with its more sophisticated treatment of aerodynamic induction effects, should give the more reliable results. However, it is believed that the Model 749 and Model 188 results obtained in this report may be very much closer to the correct values than would be implied by the comparisons shown in Figure 14-3, for the following reasons:

- 1. The two-hump shape of power-spectral density function given by the Lockheed analysis for Case 106y, and not appearing in the Boeing results, does not appear in the Lockheed analysis of Case 106x. If the Boeing analysis had actually been made for the configuration described by Case 106x, instead of the ficticious Case 106y, the difference might have been much less.
- 2. Airplane  $C_{L_{a}}$  in the Boeing analysis is actually about 2 percent greater than in the Lockhezd analysis, because the effect

on wing  $C_{L_{\alpha}}$  of upwash from the tail was not included in the Lockheed analysis (or in the tabulation given earlier of Case 106x and Case 106y  $C_{L_{\alpha}}$  values).

- 3. The lumping of masses and aerodynamic forces is very likely less realistic in the Boeing analysis of the Model 749 than in the Lockheed analysis of this airplane and the Model 188 and the Boeing analysis of the Model 720B.
- 4. The overestimation of the aerodynamic damping by the Lockheed analysis is at least partially offset, in determining limit-strength levels, by the fact that the structural damping is not included.

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### 15 RECOMMENDED GUST DESIGN CRITERIA

In this section, three alternate forms of gust loads criteria are developed in detail. Finally, the selection of a recommended form is discussed.

### 15.1 Mission Analysis Criterion

15.1.1 Design Level of N(y). In establishing a design value of N(y), it is necessary to decide first whether the proposed gust loads criterion should be on a limit or an ultimate basis.

It is quite apparent, from a brief study of exceedance curves such as shown in Figures 9-8, 9-10, 9-12, and 9-14 (keeping in mind the limit strength N(y) values obtained in Section 13) that airplanes occasionally experience gust loads substantially in excess of limit strength. The satisfactory safety record of current transport aircraft with respect to gust loads would undoubtedly not have prevailed were it not for the additional strength beyond limit provided by the 1.5 ultimate factor of safety.

As a result, there would be some logic in defining gust loads criteria on an ultimate rather than a limit basis.

On the other hand, the considerations favoring an ultimate basis for gust loads apply also, to greater or less degree, to various other loading conditions. At some future time, a thorough reconsideration of the limit load concept, as it applies to structural criteria generally, may be in order. For the present, it is believed desirable to restrict the scope of criteria changes to those directly related to the incorporation of the continuous turbulence description of the atmosphere.

Accordingly, design load levels will be defined herein on a limit basis. Should it be desired to convert at any future time to an ultimate basis, the results obtained in the present study will provide a ready means of establishing appropriate design levels.

It might be added that a further reason for hesitating to go to an ultimate basis for a gust loads criterion at this time is the progressively decreasing reliability of the model of the atmosphere as the load level increases.

Although it is proposed that an ultimate level not be considered explicitly in a gust criterion, it must be borne in mind that the safety of the aircraft still depends primarily upon its capacity to withstand

ultimate loads. As a result, there should be at least qualitative assurance that for the new airplane, as for current designs, the structural deformation and damage as the ultimate load level is approached are not so great as to prevent safe return of the airplane. Similarly, under conditions of turbulence corresponding to loads in excess of limit, functioning of all systems should remain such as not to jeopardize safe return of the airplane.

In setting a limit design value of N(y), consideration is given first to a value for vertical gust analysis. For all three airplanes, the wing is more critical than the fuselage or tail. Limit strength values of N(y) for the three airplanes, summarized in Figure 13-1, are as follows:

<b>Mo</b> del 188	$2.1 \times 10^{-5}$ cycles per hour
<b>M</b> odel 749	1.8 x 10 <sup>-5</sup> cycles per hour
Model 720B	1.1 x 10 <sup>-5</sup> cycles per hour

These three values are remarkably close to each other. The full range from the lowest to the highest value corresponds to a variation in net load of only about 5%. In view of the satisfactory operational experience of all three airplanes, the least severe value - that is, the highest - is the lational choice for future design. Accordingly, a value of  $2 \times 10^{-5}$  is considered appropriate.

All evidence to date is that the atmospheric turbulence producing limit or ultimate loads on transport aircraft is essentially isotropic, and it has been so assumed in the present analyses. Consequently, the same value of N(y) should logically be used for lateral gust loads as for vertical gust loads.

For both the Model 188 and Model 749, however, as indicated in Figure 13-1, loads in excess of limit strength occur more frequently for lateral gusts than for vertical gusts. N(y) values for the three airplanes for lateral gust loads are:

Model 188	6 x 10 <sup>-5</sup> cycles per hour
Model 749	2.5 x 10 <sup>-4</sup> cycles per hour
Model 720B (yaw damper off;	9 x 10 <sup>-6</sup> cycles per hour

It is seen that, even with yaw damper off, the Model 720B is considerably less critical than the Model 188 and Model 749. Considering the latter two airplanes, an appropriate limit design value of N(y) would lie in the

range  $6 \times 10^{-5}$  to 2.5 x  $10^{-l_1}$  exceedances per hour. Again, the least severe value - that is, the highest - is the rational choice for design. Thus a value of 2.5 x  $10^{-l_1}$  would be selected.

This is higher by a factor of 12.5 than the value of  $2 \times 10^{-5}$  considered appropriate based on vertical guat. Based on Figure 13-2, it represents a load level of roughly 76% of that associated with the  $2 \times 10^{-5}$  exceedance rate.

Three alternatives are available at this point:

- (1) Design for both vertical and lateral gusts at the less severe N(y), of 2.5 x  $10^{-4}$  exceedances per hour, at which limit strength of the reference airplanes is reached due to lateral gusts.
- (2) Design for vertical gust loads at the vertical gust frequency of exceedance of limit strength,  $N(y) = 2 \times 10^{-5}$  exceedances per hour; and design for lateral gust loads at the lateral gust frequency of exceedance of limit strength, 2.5 x  $10^{-4}$  exceedances per hour.
- (3) Design for both vertical and lateral gust at the more severe N(y), of 2 x  $10^{-5}$  exceedances per hour, at which limit strength is reached due to vertical gusts.

The first of these - use of the less severe frequency of exceedance - is, on the surface, the logical course. If 2.5 x 10-4 exceedances per hour is really the exceedance rate for limit strength due to lateral gust loads, there is no apparent reason why this same exceedance rate should not be equally acceptable for vertical gust loads. (In fact, it might even be argued that an even less severe limit frequency of exceedance of vertical gust loads might be justified, in order to maintain a more nearly comparable frequency of exceedance of ultimate load.) This course, however, is considered unacceptable. Experience in conducting vertical gust analyses and comparing the results with measurements on airplanes in flight has been accumulating for many years. The state of the art of lateral gust analysis, however, is much less advanced. Furthermore, it appears that the results of a lateral gust analysis may be considerably more subject to variation depending upon the aerodynamic input data used and, even more, upon the assumptions made regarding pilot action. Consequently, a reduction in the design levels to be used for wing design, based on the results of the lateral gust analysis cannot be justified at this time.

The second alternative, to have different values of N(y) for vertical and lateral gust analysis, would appear to nave some merit, especially as an interim measure. However, this alternative, too, is considered unacceptable, for two reasons.

First, the conclusion has already been reached that the higher (less severe) N(y) derived from the lateral analysis cannot be justified for use in the vertical analysis, because of concern that the lateral analysis may overestimate theloads. But if the lateral gust analysis does overestimate the loads, advances to be expected in the state of the art of lateral gust analysis will undoubtedly lead soon to analyses that do not overestimate the loads. At that time, if an artificially high value of N(y) has been adopted - in effect to compensate for conservatism in the analysis - unsafe loads will result. If the higher N(y) value cannot be justified for vertical gust loads, a comparable hazard exists with respect to its use for lateral gust loads.

Second. the lack of theoretical consistency would be liable to lead to confusion in application. Complexities would arise, for example in application to stresses produced by the rembined action of lateral and vertical gusts. Fortunately, the greater part of the structure of current aircraft can be considered to be stressed either by vertical gusts alone or by lateral gusts alone. Yet even in present aircraft, some regions, such as the aftbody and the engine nacelles, can be stressed by lateral and vertical gusts simultaneously. For proposed delta and arrow wing configurations with vertical fins on the wind tips, rational superposition of vertical and lateral gust loads would be imperative.

Thus the second alternative, like the first, is seen to be unacceptable.

This leaves, as a final alternative, adoption of the lower (more severe) value of N(y) for both lateral and vertical gust analysis.

As indicated by Figure 9-12 in combination with the discussion in Appendix E, Section E.5, design of the Model 138 to this more severe criterion would have resulted in an 11% increase of strength of the vertical tail. Similarly, as indicated by Figure 9-14, an increase in tail strength of 32% would have been required for the Model 749.

To adopt a criterion that present satisfactory aircraft do not meet is not an attractive course of action. On the other hand, the percentage increase in strength that would be indicated for the Model 188 is probably no greater than the range of uncertainty that characterizes many theoretical loads determinations. Further, as noted above, it is quite possible that future improvements in our capability of predicting lateral gust loads may lead to lower predicted loads at the same frequency of exceedance.

It is believed that reasonable means could be found, even now, to reduce calculated lateral gust loads to leve's comparable to limit strength of the Model 188 and Model 749, if a new airplane similar to those were to be designed today. The high tail loads shown by the analysis are associated with low damping in the Dutch roll mode. But with this low damping, the yaw response will tend to be a fairly pure sinusoid of only gradually varying amplitude. The relatively narrow band width of the yaw response relative to the vertical gust response is illustrated in Figures 15-1 and 15-2. It would appear that such a motion, at typical Dutch roll frequencies, could be controlled fairly effectively by the pilot. Flight tests reported in Reference 25, in fact, confirm this possibility. For a large swept wing airplane flying at M = 0.6 at 21,000 ft., use of a yaw damper effected roughly a 50% reduction in loads, relative to a damper off, "hands-off" case. But act on by the pilot, without the damper, also reduced the loads, by about half this amount, or 25%. An arbitrary increase in the relative damping constant,  $\zeta$ , by .05, through inclusion of a rudder angle preportional to yaw velocity, would appear to be a simple yet realistic way to account for pilot action, as long as the Dutch roll frequency does not exceed about .3 or This would increase the Dutch roll damping for the Model 188 .4 cps. (for Mission Analysis Case 202) from very roughly  $\zeta = .14$  to  $\zeta = .19$ . The tail load would then decrease roughly in the ratio  $\sqrt{.14/.19} = 1/1.17$ . For airplanes having greater damping, pilot action would be less effective because of the broader frequency band of the yaw motion. But in such cases, the addition of the constant  $\zeta = .05$  would have a much smaller - or even negligible - effect on the loads.

15.1.2 Treatment of Stability Augmentation. When stability augmentation systems are relied upon to reduce the gust loads, provision must be made for malfunction of the system. This can be done easily in a mission analysis by including an appropriate amount of flight time with the system inoperative. Selection of the percent of time that the system is inoperative must, of course, be based upon substantiable estimates of the reliability of the system.

In the incorporation of a stability augmentation system in the dynamic analysis, care must be taken to account for the effect of "saturation" of the system on loads at the limit design level. Such saturation may result from a specifically limited system authority, other nonlinearities within the system, or aerodynamic nonlinearities in the control surface force-displacement relationship. Time history studies in which these nonlinearities are specifically included may be helpful in establishing adequate linearizations for use in the power spectral analysis. Some earlier experience (unpublished) indicates that, as the gust intensity is increased beyond the level where the control system "stops" are first reached, the effectiveness of the stability augmentation system decreases quite slowly. Consequently, no sudden decrease in effectiveness as the ultimate load level is approached is to be expected.

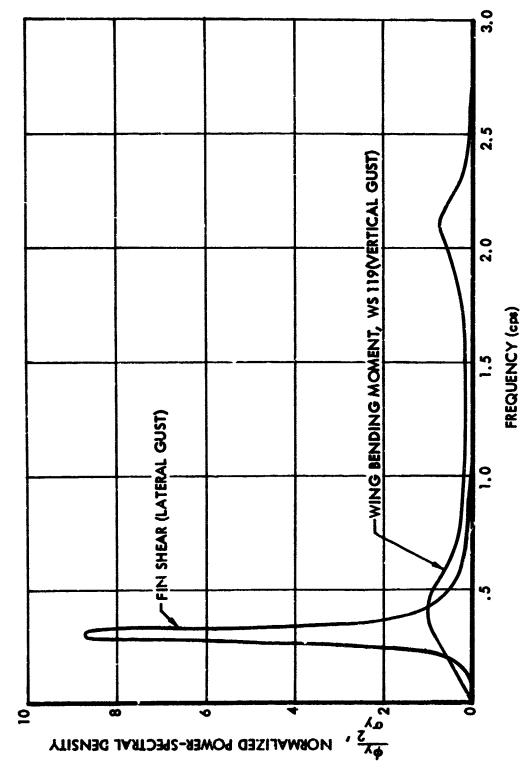
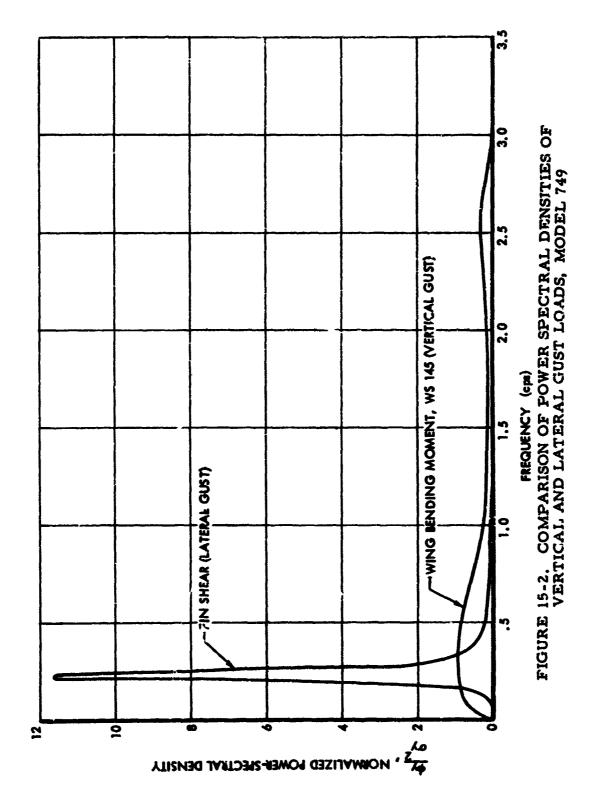


FIGURE 15-1. COMPARISON OF POWER SPECTRAL DENSITIES OF VERTICAL AND LATERAL GUST LOADS, MODEL 188



15.1.3 <u>Fail Safe Design Level</u>. The use of a mission analysis form of gust criterion can be expected to facilitate a rational determination of fail safe design levels. Such a determination would relate the fail safe frequency of exceedance to the inspection period and to the expected frequency of occurrence of potentially dangerous cracks. The procedure to be used is not self-evident, however, and its development is beyond the scope of the present study.

For the present, therefore, it is suggested that the fail safe level be set to be roughly consistent with existing fail safe requirements. Currently specified  $U_{\rm de}$  values (for the altitude range 0 - 20,000 ft.) are as follows:

Speed	U <sub>de</sub> , Fail Safe	U <sub>de</sub> , Limit	Ratio
$v_{\rm B}$	49 fps	66	. 74
$v_c$	33 fps	50	.66
$\mathbf{v}_{\mathbf{D}}$	15 fps	25	.60

From Figures 9-3(b), 9-10(b), 9-12, and 9-14, a factor of .66 applied to the gust increment, at a limit-strength frequency of exceedance of  $2 \times 10^{-5}$  cycles per hour, is found to give approximately  $1 \times 10^{-3}$  cycles per hour. This value is therefore suggested for use as a design ultimate fail safe frequency of exceedance.

15.1.4 Modified Design N(y) For Use in Joint Probability Analysis. In Section 12.3, it was pointed out that the joint probability technique will indicate a greater number of crossings of the limit load level per hour than will the matching condition technique. With the joint probability technique, all crossings of the strength envelope are counted, whereas with the matching condition technique, crossings are counted for only one straight line at a time.

In establishing limit strength values of N(y) for the reference airplanes, it was necessary to bring all three airplanes onto a common basis for comparison. For this purpose, the Model 720B N(y) values were converted to a matching condition, or single parameter, basis, by dividing by an estimated ratio of joint probability exceedances to single-parameter exceedances. This ratio was taken as 2.0.

Use of some such factor would also be appropriate for new design in order to avoid a conservative result when the joint probability technique is used. If, for example, the factor of 2.0 were retained, the design frequency of exceedance for use with the joint probability technique would be  $2.0 \times (2 \times 10^{-5} \text{ cycles per hour}) = 4 \times 10^{-5} \text{ cycles per hour}$ .

As a result of the discussion in Section 12.4, however, it appears that a factor of 2.0 is too great and that a value of 1.3 to 1.5 would be more

appropriate. The resulting difference in incremental load, however, then becomes so small (only 2 or 3%) that use of separate values of frequency of exceedance is not warranted. Consequently, the same value -  $2 \times 10^{-5}$  cycles per hour - will be used with both the matching condition and the joint probability techniques.

15.1.5 Combined Vertical and Lateral Gust Loads. In the past, it has not been customary to superimpose loads due to vertical and lateral gusts. Various important parts of an airplane, such as the wing and the vertical tail, obviously are loaded almost exclusively by vertical gusts or lateral gusts alone. But various parts of the fivelage, as well as engine nacelles on propeller driven airplanes, clearly are stressed by both vertical and lateral gusts. Power spectral theory now provides excellent guidance as to the manner in which gusts in the two directions combine; and it has become clear that failure to account for such combination can lead to structure that is under-strength relative to that required, for example, for the wing and vertical tail. It is generally accepted that, within any patch of turbulence, vertical and lateral gust velocities can properly be assumed to be uncorrelated. Under this condition, it can be shown that the appropriate design stress in any structural element is

 $\sqrt{f_v^2 + f_L^2} \quad ,$ 

where  $\mathbf{f}_V$  and  $\mathbf{f}_L$  are the design-level stresses due to the vertical and lateral components of turbulence individually.

Combinations of vertical with lateral gust loads were not considered explicitly in the analysis of the reference airplanes. It is believed that for these airplanes, such consideration would lead to only right modifications in the limit strength values of N(y) and  $\sigma_w\eta_d$ . And as brought out in Section 15.1.1, an increase in N(y) (or a decrease in  $\sigma_w\eta_d$ ) as given by the lateral gust analysis would probably not affect the value selected for future design.

In the design of a new airplane, however, it is believed that combination of vertical and lateral gust loads must be realistically or conservatively accounted for in those portions of the vehicle for which such combination is potentially critical. It is seen from the expression given above for the total incremental stress that this stress can be as much as 1.414 times  $f_v$  or  $f_L$  alone, for the limiting case in which  $f_v$  and  $f_L$  are equal.

The above discussion applies to a design envelope type of criterion (Section 15.2) as well as to a mission analysis type of criterion.

15.1.6 Suggested Formal Requirement. The following is suggested as a formal statement of a gust loads requirement based upon the mission analysis concept.

- (a) The limit gust loads shall be determined utilizing the continuous turbulence concept in accordance with the provisions of Paragraphs (b) through (h) following.
- (b) The expected utilization of the airplane shall be represented by one or more flight profiles in which the payload and the variation with time of speed, altitude, gross weight, and center of gravity position are defined. These profiles shall be divided into mission segments, or blocks, for analysis, and average or effective values of the pertinent parameters defined for each segment.
- (c) For each of the mission segments defined under Paragraph (b) and each of the load and stress quantities selected in accordance with Paragraph (e) below, values of A and No shall be determined by dynamic analysis. A is defined as the ratio of root-mean-square load to root-mean-square gust velocity and No as the radius of gyration of the load power-spectral density function about zero frequency. The effects of all pertinent rigid and elastic degrees of freedom shall be included. The power-spectral density of the atmospheric turbulence shall be as given by the equation,

$$\Phi (\Omega) = \frac{\sigma^2 L}{\pi} \frac{1 + \frac{8}{3} (1.339 L\Omega)^2}{\left[1 + (1.339 L\Omega)^2\right]^{11/6}}$$

where

= power-spectral density

σ = root-mean-square gust velocity

 $\Omega$  = reduced frequency, radians per foot

L = 2500 ft.

(d) For each of the load and stress quantities selected in accordance with Paragraph (e) below, the frequency of exceedance shall be determined as a function of load level by means of tracquation,

$$N(y) = \sum_{i=1}^{n} t N_{O} \left[ P_{1} \exp \left( -\frac{y - y_{one-g}}{b_{1}\overline{A}} \right) + P_{2} \exp \left( -\frac{y - y_{one-g}}{b_{2}\overline{A}} \right) \right]$$

where

y = net value of the load or stress

yone-g = value of the load or stress in one-g level flight

N(y) = average number of exceedances of the indicated value of the load or stress in unit time

= Symbol denoting summation over all mission segments

t = fraction of total flight time ir the given segment

 $N_0,\overline{A}$  = parameters determined by dynamic analysis as defined in Paragraph (c)

 $P_1, P_2$ , = parameters defining the probability distribution of root-mesn-square gust velocity, to be read from Figures 5-3 and 5-4 herein.

The limit gust loads shall be read from the frequency of exceedance curves at a frequency of exceedance of  $2 \times 10^{-5}$  exceedances per hour. Both positive and negative load directions shall be considered in determination of the limit loads.

- (e) A sufficient number of load and stress quantities shall be included in the dynamic analysis to assure that stress distributions throughout the structure are realically or conservatively defined.
- (f) If the joint probability technique, as described in Sections 10 and 12 herein and more particularly in Reference 1, is employed, the frequency of exceedance of limit strength shall not be greater than 2 x 10-5 exceedance per hour.
- (g) For structural components that are stressed significantly by both the vertical and lateral components of turbulence, the resultant stress shall be determined assuming that, within any patch of turbulence, the vertical and lateral components are uncorrelated. For example, in a structural element subjected to a single stress, the resultant stress shall be taken as given by

where  $f_v$  and  $f_L$  are the stresses due to the vertical and lateral components of turbulence respectively.

- (h) If a stability augmentation system is utilized to reduce the gust loads, a conservative estimate shall be made of the fraction of flight time that the system may be inoperative. The flight profiles of Paragraph (b) shall include flight with the system inoperative for this fraction of the flight time. When a stability augmentation system is included in the analysis, the effect of system nonlinearities on loads at the limit load level shall be realistically or conservatively accounted for.
- (i) The fail safe gust loads defined in FAR 25.571(c)(2) shall be replaced by loads defined as in Paragraphs (a) through (h) above at a frequency of exceedance of 1 x 10<sup>-3</sup> exceedances per hour.

### 15.2 Design Envelope Criterion

15.2.1 Design Levels of  $\sigma_{\rm w}\eta_{\rm d}$  at Speed  $V_{\rm C}$ . For the design envelope criterion, as for the mission analysis criterion, design levels will be defined herein on a limit load basis. The reasons for preferring a limit to an ultimate basis are the same for the design envelope criterion as for the mission analysis criterion and are discussed in Section 15.1.1. Precautions necessary in designing to a limit criterion are also noted in Section 15.1.1.

Design values of  $\sigma_w \eta_d$  for use at the design cruise speec,  $V_C$ , are considered of basic importance and will be developed first. In the next section, the treatment of  $V_B$  and  $V_D$  gust conditions will be discussed.

limit strength values of  $\sigma_W \eta_d$  at speed  $V_C$  for the major components of the three reference airplanes are summarized in Figures 13-3 and 13-4. The limit design value to be established for  $\sigma_W \eta_d$  will, of course, vary with altitude in accordance with the lines of constant  $N(y)/N_O$  shown in Figure 13-3 and in Figure 5-8. In discussing possible selections of limit design  $\sigma_W \eta_d$ , the various constant  $N(y)/N_O$  lines in Figure 13-3 (or Figure 5-8) will be identified. for convenience, by the  $\sigma_W \eta_d$  value at 7000 ft. Thus reference to a  $\sigma_W \eta_d$  value of 70, for example, will

1 1

actually denote a  $\sigma_w \eta_d$  variation with altitude as given by the line  $N(y)/N_0 = 5 \times 10^{-7}$ .

As in the discussion of a limit design value of N(y), attention will be directed first toward limit-strength results for vertical gust.

For all three airplanes, the wing is seen to be more critical than the fuselage or tail. Limit strength values of  $\sigma_W \eta_d$  for the three airplanes (adjusted to an altitude of 7000 ft.) are as follows:

Model 188

62 fps

Model 749

88 fps

Model 720B

108 fps

Again, the logical selection is the lowest value, or 62 fps.

Whatever value of  $\sigma_W\eta_d$  might be picked based upon the analysis of the reference airplanes, there is a possibility that a new airplane might normally operate closer to its design envelope than do the reference airplanes. There can be no assurance, of course, that an adequate strength level will be defined for such an airplane. But the only means of providing for this contingency would be to establish a  $\sigma_W\eta_d$  level higher than can be met by the existing airplanes. A new airplane similar to the reference airplanes could then neet the criterion only by an increase in strength (and weight) or by a reduction in speed and payload placards, with the attendent loss in operating flexibility and economy.

This dilemma is inherent in the design envelope approach, and possibly it should not be taken too seriously. It may well be that economic pressures will continue to demand operating placards - and hence design envelopes - considerably in excess of normal operational speeds and payloads. Nevertheless, it is pertinent to inquire whether perhaps the lowest figure in the above list of limit strength  $\sigma_{W}\eta_{d}$ 's may not represent an operation where placard speeds and payloads are more than ordinarily in excess of the normal operational values.

For this purpose, the Model 108 is compared with the Model 749. For the five Model 198 mission analysis cases contributing most to the total load exposure in Figure 9-9 (b), the average ratio of V<sub>C</sub> placard speed to mission speed is 1.14. For the seven Model 749 mission analysis cases contributing most to the total in Figure 9-11(b), the average ratio is 1.10. Thus the amount by which the Model 188 placard speed exceeds the normal operational speed is only 14%, which is judged to be rather typical. Further, the ratio of placard to typical speed for the Model

188 is only 4% greater than for the Model 749, and it is known, because of the source of the data, that the Model 749 mission speeds were taken on the high side if enything. It is concluded that the ratio of placard to normal operational speeds for the Model 188 is not out of line.

With respect to payloads, it appears that neither the Model 188 nor the 749 ordinarily carry significant amounts of cargo. A bare-minimum zero fuel weight placard that might more closely reflect actual operations of the two airplanes could be derived as follows. It would make provision for capacity passengers (96 in the Model 188, 62 in the Model 749) at 200 lb. plus a nominal 500 lb. of cargo:

	Model 188	Mcdel 749
Operating weight empty	62000 1ь.	68640 lb.
Passengers	19200	12400
Cargo	500	500
Zero fuel weight	81700	81500

The actual placard zero fuel weights, used in the analysis, are 86000 lb. and 86464 lb. respectively. It is seen that the difference between the placard zero fuel weight and the bare-unnimum dusign zero fuel weight as derived above is almost identical for the two airplanes. Again, there is no evidence that the Model 188 is out of line, even though the normal operational zero fuel weight is somewhat lower for the Model 188 (74500 lb.) than for the Model 749 (78100 lb.).

Consequently, the value of  $\sigma_{\rm W}\eta_{\rm d}$  of 62 fps at 7000 ft. appears to be a legitimate value for limit design.

For lateral gust loading, the limit strength values of  $\sigma_w \eta_d$  (adjusted to an altitude of 7000 ft.) are:

Model 188	61 fps
Model 749	65 fps
Model 720B (yaw damper off)	99 fps

As these values are approximately equal to or greater than the appropriate vertical gust design value of 62 fps, the vertical gust value is simply retained for use in lateral gust analysis. The evidence of possible conservatism in current methods of lateral gust analysis, discussed in Section 15.1.1, is still pertinent, however.

It is concluded that the appropriate limit design value of  $\sigma_{\rm w}$   $\eta_{\rm d}$  for both vertical and lateral gust analysis is defined by a constant  $\rm W(y)/\rm H_0$  line in Figure 5-8 such as to give a  $\sigma_{\rm w}$   $\eta_{\rm d}$  of approximately 62 at an altitude of 7000 ft.

15.2.2 Gust Conditions at V<sub>B</sub> and V<sub>D</sub>. As indicated in Section 4.2, it is considered appropriate that a design envelope criterion include design gust intensities at V<sub>B</sub> and V<sub>D</sub> as well as at V<sub>C</sub>, paralleling in this respect the current discrete gust requirements.

With respect to a design intensity at  $V_D$ , the limit strength  $\sigma_w\,\eta_d$  at  $V_D$  for the critical airplane (the Model 188) is just 25/50 of the Vc value. Consequently, it is recommended that the current ratio of  $V_D$  to Vc design  $U_{\rm de}$ 's be retained in the power-spectral criterion.

This ratio can be applied throughout the altitude range; or it can be applied at a single altitude considered representative of current aircraft and a constant  $M(y)/M_0$  line in Figure 5-8 followed. In the latter case, the ratio of  $V_D$  to  $V_C \sigma_w \eta_d$ 's would vary slightly with altitude.

This approach is perhaps slightly more reasonable; but the difference is fairly small, the logic is not compelling, and the decision is perhaps best based on convenience.

With respect to a design intensity at  $V_B$ , it was noted in Section 13 that the lowest limit-strength  $\sigma_W \eta_d$  at  $V_B$  for any of the three reference airplanes is well in excess of 66/50 of the  $V_B$  limit strength value for Model 188 (62 fps at 7000 ft), selected in Section 15.2.1 above as the  $V_C$  design value. As a result, it is considered appropriate to retain, in the power spectral criterion, the 66/50 ratio of  $V_B$  to  $V_C$  gust intensities that was selected when the present discrete-gust criteria were established. This ratio, like that for the  $V_D$  intensity, can be applied as a constant ratio at all altitudes, or it can be applied at a single representative altitude and a constant  $N(y)/N_O$  line in Figure 5-8 followed.

For consistency with present discrete gust criteria, it is proposed that the  $V_B$  speed be defined as the lowest speed at which stall would not occur at a load level given by the  $\sigma_{_{\!\! U}}$  value defined for design at  $V_B$ . An example of how this speed might be determined is given in Appendix Z, Section Z.1.3.

15.2.3 Adjustment of Design Loads for Differences in  $N_0$ . The maximum load to be expected in traversing either a given patch of turbulence, or a series of patches of various intensities, depends not only upon  $\bar{A}$  but also upon  $N_0$ . The higher the  $N_0$  value, the higher will be the expected maximum load. In Section 4.2, the design value of a load quantity y was given as

$$y_{design} = \overline{A} (\sigma_w \eta_d)$$
 (15-1)

To account for the effect of  $\mathbf{M}_{\mathbf{O}}$ , the appropriately modified expression is

$$y_{\text{design}} = \overline{A} (\sigma_{w} \eta_{d}) \left[ 1 + \frac{2.306 \, h_{2}}{\sigma_{w} \, \eta_{d}} \log_{10} \frac{H_{c}}{N_{o}_{\text{ref}}} \right]$$
 (15-2)

In this expression,  $\sigma_w$   $\eta_d$  is the design value established as in Section 15.2.1 or 15.2.2, independently of N<sub>O</sub>. N<sub>O</sub> is the N<sub>O</sub> value for the load quantities that established the limit-strength  $\sigma_w$   $\eta_d$  for the critical reference airplane. The appropriate value of N<sub>O</sub> is approximately 1.4 cps. This was determined by examining the N<sub>O</sub> values for bending moments, shears, torsions, and front beam shear flows in the critical region of the Model 188 wing (WS 83-167).

The above expression (Equation 15-2) is derived by considering the generalized exceedance curve at the appropriate altitude, as given, for example, in Figure 5-5. With the design N(y) considered fixed, it is clear that the design  $N(y)/N_0$  will vary depending on  $N_0$ ; hence the design y/A and the design y will also vary with  $N_0$ . This variation takes the simple form indicated by Equation 15-2 because in the region of limit load the generalized exceedance curve is a straight line governed by the storm turbulence contribution alone.

For an average  $b_2$  value of 10 and an average design  $\sigma_w$   $\eta_d$  of 60 (appropriate average values over the altitude range 0 to 30,000 ft.), the factor in the brackets in Equation 15-2 becomes

$$\left[\begin{array}{cc} 1 + .39 \log_{10} \frac{N_0}{N_{o_{ref}}} \end{array}\right]$$

Based on this expression, a factor of 2 increase in  $\mathbb{N}_0$  is found to result in an 11% increase in design incremental load or stress.

It is of interest to note that, under a mission analysis criterion, a factor of 2 increase in No results in only about a 7% increase in incremental load, in contrast to the ll% increase under the design envelope criterion. This difference results from the fact that, in Equation 15-2,  $\sigma_{\rm w}$  is equal to  $y_{\rm design}/\bar{A}$ , where  $\bar{A}$  is inherently smaller for typical mission segments than for critical design envelope points.

The "exact" expression for y design given by Equation 15-2 is available for use if desired. However, it is believed preferable, if the design envelope criterion is used, to retain the simpler form given by Equation 15-1. Any increase in accuracy due to consideration of Ho is in part illusory. It has already been noted that, under a mission analysis criterion, the effect of a difference in Ho is less than under a design envelope criterion. Since the mission analysis criterion probably gives the truer picture of the strength actually required, use of Equation 15-2 would appear, therefore, to over-correct for differences in No. Further, numerical values of No are subject to considerable uncertainty. They are often sensitive to the upper limit of integration used in their numerical evaluation, and in fact, there is a very good possibility that the theoretical value will be infinite in some practical cases. As a result, it is believed that, in choosing between Equation 15-1 and 15-2 for design use, the practical advantages offered by use of Equation 15-1 outweigh the greater theoretical accuracy of Equation 15-2.

15.2.4 Treatment of Stability Augmentation. When stability augmentation systems are relied upon to reduce gust loads, provision must be made for malfunction of the system. As in the mission analysis form of criterion a percent of flight time that the system will be inoperative must be assumed. This must be substantiable, based upon either analysis or actual service records of the reliability of the system.

The objective now should be to establish  $\sigma_w \eta_d$  levels such that the over-all frequency of exceedance of design limit load, at each design envelope point, is no greater for an airplane with stability augmentation than for an airplane without. This frequency of exceedance is, of course, measured by  $\pi(y)/\pi_0$  in Figure 5-8.

As a first approximation, at least, it would appear plausible simply to establish a reduced value of  $\sigma_{_{\rm H}}$   $\eta_{_{\rm d}}$  for use with the system inoperative.

With the sytem operating, the "basic"  $\sigma_W\eta_d$  value as established in Section 15.2.1 would be retained. An appropriate system-off value of  $\sigma_W\eta_d$  would be determined by means of Figure 5-8. Letting p denote the fraction of time the system is inoperative, the system-off  $\sigma_W\eta_d$  would simply be defined by an  $N(y)/N_0$  value equal to 1/p times the "basic"  $N(y)/N_0$ . For example, suppose the basic  $N(y)/N_0$  to be  $1.0 \times 10^{-6}$  and p to be .01.  $N(y)/N_0$  for system-off design would then be  $(1/.01)(1.0\times10^{-6})$  =  $1.0 \times 10^{-4}$ . The resulting system-off  $\sigma_W\eta_d$  (at 7000 ft.) would be 28 fps, as compared to the 64 fps value system on. Based upon system-off operation alone, the overall  $N(y)/N_0$  is then  $(1.0 \times 10^{-4})(.01)$  =  $1.0 \times 10^{-6}$ , which is the same as the design value system-on.

If the system-on loads are well below the system-off loads (each obtained using its appropriate  $\sigma_W \eta_d$ ), the contribution of the system-on loads to the overall  $N(y)/N_0$  will be negligible and can be disregarded. The airplane with a stability augmentation system will then have an overall  $N(y)/N_0$  (at the given design envelope point) no greater than the airplane without, and the objective will have been met.

This simple approach can be seen to be unconservative, however, if the system-off and system-on operation are equally critical. For the given example, the overall  $N(y)/N_0$  is now 1.99 x  $10^{-6}$ , obtained as follows:

System on: 
$$N(y)/N_0 = (.99)(1.0 \times 10^{-6}) = .99 \times 10^{-6}$$
  
System off:  $N(y)/N_0 = (.01)(1.0 \times 10^{-4}) = 1.00 \times 10^{-6}$   
Net:  $N(y)/N_0 = 1.99 \times 10^{-6}$ 

This value of  $N(y)/N_0$  is nearly twice as great as the assumed "basic" value of 1.00 x 10-6 that would apply to an airplane that did not depend upon a stability augmentation system. In fact, it is rather clear that under the above simple approach, whenever the system-on loads are critical, the airplane having a stability augmentation system is bound to be less safe than the airplane that does not require such a system. This conclusion is valid no matter what the system-off design level may be except, of course, if the system-off design level were no lower at all than the system-on level or if the system were absolutely reliable. One might, of course, consider system-on and system-off operation to be two different flight conditions to be treated independently, just like two different gross weights. But in treating two gross weights, the same  $\sigma_{\mathbf{u}}\eta_{\mathrm{d}}$  value is used for both, whereas here consideration is being given to a reduced severity for one of the two conditions. It is hard to see how a criterion could be justified that would clearly permit a higher frequency of exceedance of limit strength for an airplane that depends upon a stability augmentation system than one that does not.

If, in the above example, the design  $N(y)/N_0$  values for both system-on and system-off cases were decreased by a factor of 2 (resulting in increased  $\sigma_W \eta_d$ 's), the net  $N(y)/N_0$  would then be approximately 1.0 x 10<sup>-6</sup>, as desired. To accomplish this decrease would require an increase of strength. Based upon the system-on loads, it can be seen that the required increase in strength would be in the ratio 70.5/64 = 1.10. Based on the system-off loads (actually off scale in Figure 5-8) it would be somewhat higher. The actual required ratio would be between the two values, probably about 1.12. No reasonable decrease in  $N(y)/N_0$  (i.e., increase in  $\sigma_W \tau$ ) for the system-off case alone will give a net  $N(y)/N_0$  equal to the desired value.  $N(y)/N_0$  values or  $\sigma_W \eta_1$ 's for both system-off and system-on cases must be modified.

If it were desired as a matter of convenience to alter only the system-cff  $N(y)/N_0$ , the 12% unconservatism could be reduced. For example, if the system-off  $N(y)/N_0$  were to be specified as 1/2p, instead of 1/p, times the basic value, then the overall  $N(y)/N_0$  would be (still assuming the airplane to be equally critical system-off and system-on):

System on: 
$$N(y)/N_0 = (.99)(1.0 \times 10^{-6}) = .99 \times 10^{-6}$$
  
System off:  $N(y)/N_0 = (.01)(5 \times 10^{-5}) = .50 \times 10^{-6}$   
Net:  $N(y)/N_0 = (.01)(5 \times 10^{-5}) = .50 \times 10^{-6}$ 

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An increase of strength of about 7% would be required in this case to achieve the desired net  $N(y)/N_0$  of 1.0 x 10<sup>-6</sup>. Conversely, the use of the simplified criterion could still lead to an airplane that would be understrength by 7% (of the gust increment) relative to the airplane without a stability augmentation system.

If the system-off  $N(y)/N_0$  were to be specified as 1/3p, instead of 1/p or 1/2p, times the basic value, the 7% unconservatism would decrease to about 5%.

The above percentages have been found not to be sensitive to the value of p assumed.

To eliminate the unconservatism associated with modification of only the system-off  $\sigma_w\eta_d$ , both system-off and system-on  $\sigma_w\eta_d$ 's must be altered. A fully rational approach would be to select arbitrarily values of  $N(y)/N_0$  system-off and system-on such as to satisfy the equation,

$$p\left(\frac{N(y)}{N_{O}}\right)_{\text{system-off}} + (1 - p)\left(\frac{N(y)}{N_{O}}\right)_{\text{system-on}} = \left(\frac{N(y)}{N_{O}}\right)_{\text{basic}}$$

This equation is satisfied, for example, by taking

$$\left(\frac{N(y)}{N_O}\right)$$
 system-off =  $\frac{1}{2p}\left(\frac{N(y)}{N_O}\right)$  basic

and

$$\left(\frac{N(y)}{N_{o}}\right)$$
 system-on =  $\frac{1}{2(1-p)}\left(\frac{N(y)}{N_{o}}\right)$  basic  $\approx \frac{1}{2}\left(\frac{N(y)}{N_{o}}\right)$  basic

leading to a system-on  $\sigma_w \eta_d$  10 to 12% greater than the basic value, depending upon altitude. This special case will provide a useful rule-of-thumb, but it is believed desirable to provide the flexibility offered by use of the above equation without individually specified values of  $N(y)/N_0$  system-off and system-on.

The comments made in Section 15.1.2 with respect to system nonlinearities are equally applicable in connection with a design envelope type of criterion.

15.2.5 Fail Safe Design Level. As in connection with the mission analysis form of criterion, it is considered appropriate to retain the ratios of fail safe gust intensity to limit design gust intensity currently in use on a  $U_{de}$  basis. Thus to determine fail safe values of  $\sigma_{W}\eta_{d}$ , the  $V_{C}$  limit design value at any given altitude should be multiplied by the following factors, based upon the tabulation in Section 15.1.3:

$$v_{C}$$
: = .66  
 $v_{D}$ : (.50)(.60) = .30

If preferred, these ratios can be applied instead at a single representative altitude and a constant  $N(y)/N_0$  line in Figure 5-8 followed.

15.2.6 Design Levels of  $\sigma_{\rm W}$  and P. For analyses in which the joint probability technique is employed, design values of  $\sigma_{\rm W}$  and of P, the allowable probability that limit strength is exceeded, rather than of  $\sigma_{\rm W}\eta_{\rm d}$ , are necessary.

Based upon the results given in Reference 1 and in Section 12.3 herein, a value of  $\eta_d$  of 3.5 is considered appropriate.

The design value of  $\sigma_w$  is then given by the design value of  $\sigma_w\,\eta_d$  divided by  $\eta_d$  .

The design value of P, the probability that limit strength is exceeded, is read from an appropriate curve in Figure 12-7, entering with  $\eta_{\rm d} = y/\sigma = 3.5$ .

In establishing limit-strength values of  $\sigma_W \eta_d$  for the reference airplanes, it was necessary to bring the Model 720B to a common basis with the Model 188 and Model 749, inasmuch as the analysis of the Model 720B had been on a joint probability basis and that of the Model 188 and Model 749, on a single parameter basis. For this purpose, the "2 x Normal" curve in Figure 12-7 was used. For use in new design, it is believed that a slightly more conservative value of P should be used, intermediate between the "Normal" and "2 x Normal" curves. At  $\eta_d = 3.5$ , the P values given by the three curves are:

"Normal"  $P = 2.3 \times 10^{-14}$ 

"2 x Normal"  $P = 4.7 \times 10^{-4}$ 

"Circular Normal"  $P = 2.1 \times 10^{-3}$ 

A value of  $3 \times 10^{-4}$  is suggested for design.

15.2.7 Suggested Formal Requirement. The following is suggested as a formal statement of a gust loads requirement based upon the design envelope concept:

- (a) The limit gust loads shall be determined utilizing the continuous turbulence concept, in accordance with the provisions of paragraphs (b) through (h) following.
- (b) The limit loads shall be determined for all critical altitudes, weights, and weight distributions, in accordance with FAR 25.321(b), and for all critical speeds within the ranges indicated in Paragraph (d) below.
- (c) In determining the limit loads, values of A (ratio of root-mean-square load to root-mean-square gust velocity) for various load and stress quantities selected in accordance with Paragraph (e) below shall be determined by dynamic analysis. The effects of all pertinent rigid and elastic degrees of freedom shall be included. The power-spectral density of the atmospheric turbulence shall be as given by the equation,

$$\Phi(\Omega) = \frac{\sigma^2 L}{\pi} \frac{1 + \frac{8}{3} (1.339 L\Omega)^2}{\left[1 + (1.339 L\Omega)^2\right]^{11/6}}$$

where

power-spectral density

**σ** = root-mean-square gust velocity

 $\Omega$  = reduced frequency, radians per foot

L = 2500 ft.

- (d) The limit loads shall be obtained by multiplying the  $\overline{A}$  values given by the dynamic analysis by the following values of  $\sigma_{v}\eta_{d}$ :
  - (1) At speed V<sub>C</sub>: as given by the line  $N(y)/N_0 = 1.2 \times 10^{-6}$  in Figure 5-8 herein.
  - (2) At a speed  $V_B$ , to be selected by the manufacturer but in no event to be below the lowest speed at which stall would not occur at the limit load levels resulting from the criteria: as given by 1.32 times the values obtained under subparagraph (1) above.
  - (3) At speed  $V_D$ : as given by 1/2 the values obtained under subparagraph (1) above.
  - (4) At speeds between  $V_B$  and  $V_C$ , and between  $V_C$  and  $V_D$ : as given by linear interpolation.
- (e) A sufficient number of load and stress quantities shall be included in the dynamic analysis to assure that stress distributions throughout the structure are realistically or conservatively defined.
- (f) If the joint probability technique, as described in Sections 10 and 12 herein and more particularly in Reference 1, is employed,  $\sigma_w$  shall be obtained by dividing the  $\sigma_w\eta_d$  values defined in paragraph (d) by 3.5. The allowable probability of exceedance of limit strength shall be taken as 0.0003.

(g) For structural components that are stressed significantly by both the vertical and lateral components of turbulence, the resultant stress shall be determined assuming the vertical and lateral components of turbulence to be uncorrelated. For example, in a structural element subjected to a single stress, the resultant stress shall be taken as given by

$$\sqrt{f_v^2 + f_L^2} ,$$

where  $f_{v}$  and  $f_{f_{v}}$  are the stresses due to the vertical and lateral components of turbulence respectively.

(h) If a stability augmentation system is utilized to reduce the gust loads, a conservative estimate shall be made of the fraction of flight time, p, that the system may be inoperative. Limit loads shall be determined separately for the system operative and system inoperative, using  $\sigma_w \eta_d$  values defined by a pair of  $N(y)/N_O$  values seeting the condition that:

$$p\left(\frac{N(y)}{N_O}\right)_{\text{system off}} + (1 - p)\left(\frac{N(y)}{N_O}\right)_{\text{system on}} = \left(\frac{N(y)}{N_O}\right)_{\text{Par. (d)}}$$

When a stability augmentation system is included in the analysis, the effect of system nonlinearities on loads at the limit load level shall be realistically or conservatively accounted for.

(i) The fail safe gust loads defined in FAR 25.571(c)(2) shall be replaced by loads defined as in Paragraphs (a) through (h) above at the following out values:

At Vc: .66 of the value given by Paragraph (d)(1) above.

At  $V_B$ : .74 of the value given by Paragraph (d)(2) above.

At  $V_D$ : .60 of the value given by Paragraph (d)(3) above.

At speeds between  $V_B$  and  $V_C$ , and between  $V_C$  and  $V_D$ ; as given by linear interpolation.

# 15.3 Combined Criterion

As indicated in Section 4, a combined mission analysis and design envelope criterion gives promise of providing the advantages of each basic form while minimizing the associated disadvantages.

The proposed combined criterion provides for a choice between the following in any given application:

- (1) A design envelope analysis in accordance with Section 15.2 but at a level considerably in excess of that defined therein. This level would be set such that no matter how severe the actual operation might be, as restricted only by the design envelope, a realistic mission analysis would be extremely unlikely to indicate higher loads.
- (2) A mission analysis in accordance with Section 15.1, in combination with a design envelope analysis at a level equal to or slightly below that defined in Section 15.2, the highest loads from either analysis to be used for design.

For an airplane that is not gust critical, the simple, conservative approach offered by Option (1) above would be selected. If for a given design the conservatism of Option (1) were unacceptable, Option (2) could be selected. A mission analysis would then be performed. But a floor below which the loads could not drop would be established by a design envelope analysis at a reduced severity. This floor would provide insurance against either a rapid increase in loads as the design envelope is approached or an unconservative definition of the design missions.

The purpose of this section is primarily to establish the two  $\sigma_{\rm w}\eta_{\rm d}$  levels required.

15.3.1 Design  $\sigma_{\mathbf{u}}\eta_{\mathbf{d}}$  Levels for Use in Lieu of a Mission Analysis. To establish the desired conservative value of  $\sigma_{\mathbf{u}}\eta_{\mathbf{d}}$ , two somewhat independent approaches will be followed to indicate an upper limit.

First, using the Model 188 as an example, it will be assumed that the airplane operates 100% of the time at its critical design envelope point. The  $\sigma_w \eta_i$  value corresponding to the mission analysis limit strength N(y) of 2 x 10<sup>-5</sup> cycles per hour will then be determined.

The critical case is No. 417, at 116000 lb. G.W. and altitude 12,000 ft. Considering wing bending moment at WS 83 to be a critical load quantity,  $N_0$  is 1.3 cps (Table B-2).  $N(y)/N_0$  corresponding to the limit design frequency of exceedance of 2 x 10-5 cycles per hour is then

$$\frac{N(y)}{N_0} = \frac{2 \times 10^{-5}}{(3600)(1.3)} = 4.3 \times 10^{-9}$$

From Figure 5-5, the corresponding y/A at h = 12000 ft. is seen to be 114 fps. This is the required  $\sigma_w \eta_d$ .

It is noted that Model 188 characteristics entered only to the extent of establishing N<sub>O</sub> and h. The Model 188 N<sub>O</sub> is considered quite typical, and the result would be about the same for all altitudes in the range 10000 - 30000 ft. As the altitude increases further, the required  $\sigma_{\rm W}\eta_{\rm d}$  would decrease.

Second, again using the Model 188 as an example, it will be assumed that the airplane is operated so as to duplicate the overall exceedance curves such as shown in Figure 9-9, but that the placerds are reduced so as to just envelope Case 202, which is the predominant contributor to the load exceedances.

The limit strength value of  $\sigma_w \eta_d$  is determined for this case by the same method described in Appendix E, Section E.1.3, in connection with the preparation of Table E-1. The value is found to be 111 fps. As the Model 188 just meets the suggested mission analysis limit strength criterion of  $N(y) = 2 \times 10^{-5}$  cycles per hour, this is the required value of  $\sigma_w \eta_d$ . Inasmuch as the airplane is not operated, in this example, 100% of the time at its critical design envelope point, the 111 value obtained here is slightly less than the 114 fps value obtained above.

By either approach, the "upper limit"  $\sigma_w\eta_d$  lies in the very narrow range of 111 to 114 fps (at 12000 ft.). In comparison, the actual limit strength value is 60 fps.

It seems highly unlikely that any actual operation could be as s were, relative to the operating placards, as assumed in the above two calculations. Consequently, some reduction from the lll - ll4 fps range of  $\sigma_{\rm W}\eta_{\rm d}$  is in order, and a value of ll0 fps (at 7000 ft.) would appear to be ample.

15.3.2 Design  $\sigma_w \eta_d$  Levels for Use in Conjunction with a Mission Analysis. To establish a  $\sigma_w \eta_d$  level to use as a floor in conjunction with a mission analysis, specific quantitative guides are difficult to come by. However, the Model 188 appears to represent a fairly extreme degree of difference between normal operating conditions and design placards. As a result, it would appear that any  $\sigma_w \eta_d$  selection appreciably below the Model 188 limit strength value would be unlikely to satisfy the need for a  $\sigma_w \eta_d$  floor. A value equal to the Model 188 limit strength value, of 62 fps at 7000 ft., is suggested.

Under Option (2), the design envelope floor should include  $V_{\rm B}$  and  $V_{\rm D}$  as well as  $V_{\rm C}$  conditions; it should also include the appropriate treatment of stability augmentation devices as discussed in Section 15.2.4 and the determination of fail safe conditions in accordance with Section 15.2.5.

15.3.3 <u>Suggested Formal Requirement</u>. The following is suggested as a formal statement of a gust loads requirement that would combine the mission analysis and design envelope concepts:

- (a) The limit gust loads shall be letermined utilizing the continuous turbulence concept, in accordance with the provisions of either Paragraph (b) or Paragraphs (c) and (d) below.
- (b) Design envelope analysis. The limit loads shall be determined in accordance with the following:
  - (1) All critical altitudes, weights, and weight distributions, as specified in FAR 25.321(b), and all critical speeds within the ranges indicated in Paragraph (b)(3) below, shall be considered.
  - (2) Values of A (ratio of root-mean-square load to root-mean-square gust velocity) for various load and stress quantities selected in accordance with Paragraph (b)(4) below shall be determined by dynamic analysis. The effects of all pertinent rigid and elastic degrees of freedom shall be included. The power spectral density of the atmospheric turbulence shall be as given by the equation,

$$\Phi(\Omega) = \frac{\sigma^2 L}{\pi} \frac{1 + \frac{8}{3} (1.339 L\Omega)^2}{\left[1 + (1.339 L\Omega)^2\right]^{11/6}}$$

where

- = power-spectral density
- σ = root-mean-square gust velocity
- $\Omega$  = reduced frequency, radians per foot

L = 2500 ft.

- (3) The limit loads shall be obtained by multiplying the  $\overline{A}$  values given by the dynamic analysis by the following values of  $\sigma_u \eta_d$ :
  - (i) At speed  $V_C$ : as given by the line  $N(y)/N_O = 6 \times 10^{-9}$  in Figure 5-8 herein.
  - (ii) At a speed V<sub>B</sub>, to be selected by the manufacturer but in no event to be below the lowest speed at which stall would not occur at the limit load levels resulting from these criteria: as given by 1.32 times the values obtained under subparagraph (i) above.

- (iii) At speed V<sub>D</sub>: as given by 1/2 the values obtained under subparagraph (i) above.
- (iv) At speeds between  $V_B$  and  $V_C$ , and between  $V_C$  and  $V_D$ : as given by linear interpolation.
- (4) A sufficient number of load and stress quantities shall be included in the dynamic analysis to assure that stress distributions throughout the structure are realistically or conservatively defined.
- (5) If the joint probability technique, as described in Sections 10 and 12 herein and more particularly in Reference 1, is employed,  $\sigma_{\rm W}$  shall be obtained by dividing the  $\sigma_{\rm W}\eta_{\rm d}$  values defined in paragraph (b)(3) by 3.5. The allowable probability of exceedance of limit strength shall be taken as 0.0003.
- (6) For structural components that are stressed significantly by both the vertical and lateral components of turbulence, the resultant stress shall be determined assuming the vertical and lateral components of turbulence to be uncorrelated. For example, in a structural element subjected to a single stress, the resultant stress shall be taken as given by

$$\sqrt{f_v^2 + f_L^2} \quad ,$$

where  $f_{V}$  and  $f_{L}$  are the stresses due to the vertical and lateral components of turbulence respectively.

(7) If a stability augmentation system is utilized to reduce the gust loads, a conservative estimate shall be made of the fraction of flight time, p, that the system may be inoperative. Limit loads shall be determined separately for the system operative and system inoperative, using  $\sigma_w \eta_d$  values defined by a pair of N(y)/No values meeting the condition that:

$$p\left(\frac{N(y)}{N_{O}}\right)_{\text{system-off}} + (1 - p)\left(\frac{N(y)}{N_{O}}\right)_{\text{system on}} = \left(\frac{N(y)}{N_{O}}\right)_{\text{Par.(b)(3)}}$$

When a stability augmentation system is included in the analysis, the effect of system nonlinearities on loads at the limit load level shall be realistically or conservatively accounted for.

(8) The fail safe gust loads defined in FAR 25.571(c)(2) shall be replaced by loads defined as in Paragraphs (b)(1) through (7) above at the following  $\sigma_{c}\eta_{1}$  values:

At  $V_0$ : .66 of the value given by Paragraph (b)(3)(i) above.

At  $V_B$ : .74 of the value given by Paragraph (b)(3)(ii) above.

At  $V_D$ : .60 of the value given by Paragraph (b)(3)(111) above.

At speeds between  $V_{\bar{D}}$  and  $V_{\bar{C}}$  and between  $V_{\bar{C}}$  and  $V_{\bar{D}}$ : as given by linear interpolation.

- (c) Flight profile analysis. Limit loads shall be determined in accordance with the following:
  - (1) The expected utilization of the airplant small be represented by one or more flight profiles in which the payload and the variation with time of speed, altitude, gross weight, and center of gravity position are defined. These profiles shall be divided into mission segments, or blocks, for analysis, and average or effective values of the pertinent parameters defined for each segment.
  - (2) For each of the mission segments defined under Paragraph (c)(1) and each of the load and stress quantit reselected in accordance with Paragraph (4) below, values or A and No shall be determined by dynamic analysis. A is defined as the ratio of root-mean-square load to root-mean-square gust velocity and No as the radius of gyration of the load power-spectral density function about zero frequency. The effects of all pertinent rigid and elastic degrees of freedom shall be included. The power-spectral density of the atmospheric turbulence shall be as given by the equation,

$$\Phi (\Omega) = \frac{\sigma^2 L}{\pi} \frac{1 + \frac{8}{3} (1.339 \text{ I}\Omega)^2}{\left[1 + (1.339 \text{ I}\Omega)^2\right]^{\frac{11}{6}}}$$

where

• = power spectral density

σ = root-mean-square velocity

 $\Omega$  = reduced frequency, radians per foot

L = 2500 ft.

(3) For each of the load and stress quantitie selected in accordance with Paragraph (4) below, the frequency of

exceedance shall be determined as a function of load level by means of the equation,

$$N(y) = \sum_{i} tN_0 \left[ P_1 \exp \left( -\frac{y - y_{one-g}}{b_1 \overline{A}} \right) + P_2 \exp \left( -\frac{y - y_{one-g}}{b_2 \overline{A}} \right) \right]$$

where

y = net value of the load or stress

y<sub>one-g</sub> = value of the load or stress in one-g level flight

N(y) = average number of exceedances of the indicated value of the load or stress in unit time

= Symbol denoting summation over all mission segments

t = fraction of total flight time in the given segment

 $N_0$ ,  $\overline{A}$  = parameters determined by dynamic analysis as defined in Paragraph (c)(2)

P<sub>1</sub>,P<sub>2</sub>,b<sub>1</sub>,b<sub>2</sub> = parameters defining the probability distributions of root-mean-square gust velocity, to be read from Figures 5-3 and 5-4 herein.

The limit gust loads shall be read from the frequency of exceedance curves at a frequency of exceedance of  $2 \times 10^{-5}$  exceedances per hour. Both positive and negative load directions shall be considered in determination of the limit loads.

- (4) A sufficient number of load and stress quantities shall be included in the dynamic analysis to assure that stress distributions throughout the structure are realistically or conservatively defined.
- (5) If the joint probability technique, as described in Sections 10 and 12 herein and more particularly in Reference 1, is employed, the frequency of exceedance of limit strength shall not be greater than 2 x 10<sup>-5</sup> exceedances per hour.

(6) For structural components that are stressed significantly by both the vertical and lateral components of turbulence, the resultant stress shall be determined assuming that, within any patch of turbulence, the vertical and lateral components are uncorrelated. For example, in a structural element subjected to a single stress, the resultant stress shall be taken as given by

$$\sqrt{f_v^2 + f_L^2} ,$$

where  $f_v$  and  $f_L$  are the stresses due to the vertical and lateral components of turbulence respectively.

- (7) If a stability augmentation system is utilized to reduce the gust loads, a conservative estimate shall be made of the fraction of flight time that the system may be inoperative. The flight profiles of Paragraph (c) (1) shall include flight with the system inoperative for this fraction of the flight time. When a stability augmentation system is included in the analysis, the effect of system nonlinearities on loads at the limit load level shall be realistically or conservatively accounted for.
- (d) Supplementary design envelope analysis. In addition to the limit and fail safe loads defined by Paragraph (c) above, limit and fail safe loads shall also be determined in accordance with Paragraph (b) above modified as follows:
  - (1) In Paragraph (b)(3)(1), the value  $N(y)/N_0 = 6 \times 10^{-9}$  is replaced by  $N(y)/N_0 = 1.2 \times 10^{-6}$ .
  - (2) In Paragraph (b)(7), the reference to Paragraph (b)(3) is to be understood as referring to the paragraph as modified by Paragraph (d)(1) above.
  - (3) In Paragraph (b)(8), the reference to Paragraph (b)(3)(i) through (b)(3)(iii) is to be understood as referring to the paragraph as modified by Paragraph (d)(1) above.

### 15.4 Evaluation of the Three Forms of Criterion

Structural design criteria to date have almost universally been of the design envelope type. However, in recent years, whenever there has been any real question of the adequacy of a given airplane to withstand the

gust loads to which it may be exposed, or of the adequacy of existing criteria for application to new vehicles operating on vastly different flight profiles, mission analyses have been performed. Only in this way can it be assured that the new airplanes do not become less safe than the old as a result of possibly more severe operational usage relative to the design envelope. For this reason, the mission analysis format for a gust loads criterion appears to be almost a necessity.

Furthermore, only if the original design is substantiated on a mission analysis basis can the effects of changes in operating practices during the life of a fleet be conveniently evaluated.

On the other hand, as discussed in Section 4.3, the mission analysis form of criterion suffers certain disadvantages. Judgement is required in setting up the design missions, and as a result, differences of opinion may arise and be difficult to reconcile in administration of the criterion. Also, considerable care may be required to assure that a sufficient variety of off-typical flight conditions are included; in fact this is an area that has been barely touched upon in the present study. Another possible disadvantage is the increased difficulty in matching statistically defined loads with conditions for stress analysis. This may be of rather small consequence, however, and may even be overshadowed by the possibility that under a design envelope criterion many more sets of statistically defined loads would have to be matched in order to establish the critical design point.

Should it be decided to retain the design envelope form of criterion, it is believed that a major gain over the existing discrete gust criteria would still be achieved, as a result of the more realistic evaluation of the airplane response to turbulence provided by the power-spectral approach.

The combined criterion developed in Section 15.3 is believed to largely overcome the disadvantages of using either of the two basic forms of criterion alone. While it will involve somewhat more analysis in some instances, this is offset by the simpler treatment possible for those airplanes that are not gust critical and by the more straight-forward treatment of non-typical operating conditions. The combined criterion is therefore believed to be most appropriate for use at this time.

## 15.5 Formal Requirements for Design Technique

It will be noted that the suggested formal requirements provided in Sections 15.1.5, 15.2.6, and 15.3.3 do not specify a particular technique for integration of the power spectral loads determination with the routines of detailed stress analysis. Both the matching condition and joint

probability techniques developed in the present program are considered adequate, and sufficient information is provided in the suggested formal requirements so that either can be used. Furthermore, it is to be expected that improvements in these techniques, or new techniques altogether, will be developed in the future. It is believed that the design technique must, necessarily, be left to the selection of the individual manufacturer in order that he may adequately integrate power spectral results with his overall philosophy of structural design and testing.

### 16 SUMMARY OF DESIGN PROCEDURES

The purpose of this section is to discuss how the criteria suggested in Section 15 would ordinarily be implemented in application to a new design. Other portions of this report, dealing specifically with the analyses of the three reference airplanes, will be drawn upon or referenced as appropriate. The procedure will, of course, differ to some extent depending upon whether the analysis is to a mission analysis or design envelope form of criterion. The choice between the two forms of criterion will presumably depend in part on policy action to be taken by the Federal Aviation Agency based on the results of this study. As noted in Section 15.4, the "combined" form of criterion, which makes provision for both mission analysis and design envelope approaches (Section 15.3), is recommended by the present authors.

## 16.1 Flight Conditions Required for Analysis

The first step in a gust design procedure is to establish the various flight conditions for which analysis will be required.

16.1.1 <u>Mission Analysis Criterion</u>. Where loads are to be determined according to a mission analysis type of criterion, it is first necessary to establish the design missions and lump into segments for analysis.

The missions developed for the three reference airplanes in Section 6 herein and in Reference 1 are considered appropriate guides to the type of mission profile suitable for a new design. Usually, however, no actual operational data will be available; and, as a result, realistic estimates of typical operating conditions will be required. Ratios of typical to placard values of speed, payload, etc., based upon the operation of existing aircraft can be used as a guide, but careful thought will have to be given as well to how the new airplane will probably be operated.

As in the analysis of the reference airplanes, values of the various parameters required in the analysis can usually be taken at the midpoint of each segment, or as average values over the segment. It should be noted, however, that where one or more parameters vary over a wide range within any one segment, use of average values tends to be unconservative. (For example, see the discussion of speed selection in Section 6.1.) Consequently, such segments should be lumped nearer to the critical end of the segment, or the profile should be broken into more segments.

As noted in Section 15.1, for airplanes which depend upon a stability augmentation system to limit the gust loads, the design missions must

include an appropriate fraction of flight time with the system inoperative. In addition, if a specific emergency procedure - for example, an emergency descent procedure - involves a substantial increase in gust exposure, this too should be included in the design missions.

For advanced designs the chief difference in the generation of the design missions is likely to be a need for a finer breakdown into mission segments. For a typical supersonic transport, for example, ranges of chivalent airspeed, Mach number, and altitude throughout the flight are all much greater than for current airplanes; and both the turbulence exposure and the response characteristics vary markedly as the flight proceeds. Variable configuration geometry, such as introduced by a variable sweep wing, would also lead to a need for a finer mission breakdown.

16.1.2 Design Envelope Criterion. Where loads are determined according to a design envelope criterion, the first step is to select a variety of potentially critical combinations of speed, altitude, payload, fuel weight, and c-g. location. VB, VC, and VD conditions should all be included. Some elimination of non-critical conditions can perhaps be accomplished at this stage by use of a simplified analysis as illustrated in Section 7. Probably the best approach to determination of critical conditions is to run a somewhat limited number of cases at first, then examine the results and add other cases as indicated.

### 16.2 Equations of Motion

The next step - which actually can be carried out simultaneously with the definition of flight conditions for analysis - is to write the necessary equations of motion and program these for automatic digital solution. This is ordinarily a major undertaking, which requires a high order of capability in the field of aeroelastic dynamic analysis. All pertinent elastic as well as rigid-airplanes modes must, of course, be included, as well as the effects of automatic control and stability augmentation systems if present. Examples of equations of motion appropriate for various specific applications, together with their derivations, are given in References 1, 21, 22, 26 and 27. Solution of these equations is such as to provide the steady-state response to a sinusoidal variation of gust velocity of unit amplitude at each of various frequencies. Response outputs are obtained for a variety of accelerations, loads, and stresses. Multiplication by the gust power-spectral density and integration with respect to frequency leads to values of A and No for each output quantity.

Because of the complexity of a modern dynamic gust analysis and the need for judgment in establishing values of the various input parameters,

various checks should be made in order to keep the studies in perspective and to provide confidence in the results. Of particular importance is a maneuver loads check such as illustrated for two of the reference airplanes in Section 8.1.3. A flutter check also is desirable, as this will tend to bring to light any inconsistencies between the dynamic gust analysis and the formal flutter analysis with respect to representation of the elastic mode dynamics and aerodynamics. Over-all reasonableness checks of A values should also be made by comparing with A values obtained from a simple static analysis using curves such as those in Figure 5-2.

For some airplanes, a much simpler dynamic analysis than implied by the above discussion may suffice. For example, published NACA data (Reference 26) indicate that, for an airplane comparable to the DC-3, the dynamic factor for wing bending is on the order of only 1.05; and there is no reason to expect that dynamic increments to the shears and torsions would be significantly greater. For other airplanes that are generally comparable in size, mass distribution, first wing elastic mode natural frequency (above 4 cps), etc., the dynamic effects could be expected to be no greater and therefore could be adequately accounted for by means of a simple factor of 1.05 to 1.10 applied to the static loads.

For such an airplane, the equations of motion would, of course, be much simpler, as the elastic-mode degrees of freedom would not be included. Further, it appears that, for past airplanes, the effects of pitch have generally been small and tend to reduce the loads slightly. (For example, for the Model 749 Constellation the inclusion of pitch reduces the load factor by about 7%.) Thus it appears that - for an airplane having conventional stability characteristics - the pitch freedom can also be eliminated. With the representation thus simplified, the airplane remains free only to plunge. For this representation, solutions of the equations of motion are already available in the form of curves such as provided in Figure 5-2. These provide the A value for airplane load factor; air loads are then assumed to be distributed on a static basis and are placed in equilibrium with inertia loads in the usual way. The estimated dynamic factor must, of course, be applied to the gust incremental loads thus obtained.

It may be remarked that the particular curves shown in Figure 5-2 are known to be slightly unconservative because of approximations made to the left growth functions in their derivation. It would be desirable, therefore, to recompute these curves, following the procedure used in Reference 15. Pending such revision, an approximate correction factor, on the order of 1.08, can be applied to  $K_{\sigma}$  values read from Figure 5-2.

Values of  $N_0$ , which are needed if the mission analysis form of criterion is used, can be estimated. A value of 1.0 cps is generally realistic.

For advanced configurations, the equations of motion will be derived following the same general principles as for current aircraft. Differences in treatment may be required, however, and the analysis may become more complex. For a low aspect ratio delta wing, for example, the concept of an elastic axis loses its meaning, and a lifting-line treatment of the aerodynamics will no longer suffice.

As analysis methods are modified to suit new configurations, or as advances are made in analysis techniques, the intent should be to secure as realistic a representation as is practical. In particular, no attempt should be made to purposely retain the specific conservatisms that might be present in the reference-airplane analyses. The factors affecting gust response are complex, and various airplanes differ reatly in the detailed characteristics of their dynamic response. As a result, it is believed that the only practical approach is to judge the adequacy of the representation of each airplane on an individual, absolute basis.

On the other hand, one must not completely lose sight of the fact that the design levels are set based upon the strength of the reference airplanes. Whenever a significantly different method of analysis is introduced, therefore, the probable effect on the reference airplanes should be reviewed. Examples of changes that would clearly require review of the reference airplane analyses would include the introduction of the spanwise variation of the vertical gust velocity, and the inclusior of the transfer function of the human pilot.

### 16.3 Dynamic Analysis and Design-Level Loads

Under either the mission analysis or design envelope form of criterion, the next step is to determine the necessary input data for the various flight conditions and perform the dynamic analysis. This will result in  $\bar{A}$  and  $N_O$  values for as many load quantities - loads, stresses, and ficticious stresses - as may be needed to define loads, stresses, or margins of safety throughout the structure. If the joint probability technique is to be used, this step will include also the computation of the pertinent correlation coefficients,  $\rho$ . (The quantities  $\sigma_{\alpha}$  and  $\sigma_{\beta}$ , used when the joint probability technique is applied on a mission analysis basis, are given by  $2\pi$   $N_O$   $\bar{A}_X$  and  $2\pi$   $\bar{N}$   $\bar{A}_X$  respectively.)

16.3.1 Mission Analysis Criterion. Under the mission analysis form of criterion, the  $\overline{A}$  and  $N_0$  values obtained from the dynamic analysis are next used to obtain exceedance curves for each load quantity, at described in the last paragraph of Section 4.1 and illustrated, for example, by Figure 9-9. The design level value for each load quantity is then read at the design frequency of exceedance of 2 x  $10^{-5}$  cycles per hour defined in Section 15.

Advanced configurations where acrodynamic heating must be considered will require some modification to this procedure. One major effect of aerodynamic heating is the reduction of material allowables in the supersonic portion of the flight, in general resulting in different allowables for each flight segment. For representative supersonic transport designs, the highest gust loads have been found to occur during subsonic climb, where the structure is cold. Supersonic speeds, resulting in hot structure and reduced allowables, are reached only at high altitudes, where the gust loads are very much reduced. An obvious simple, but conservative approach would be to define design-level loads in the usual way and to apply these loads in conjunction with the lowest (high temperature) allowables. This conservatism is likely to be unacceptable, however. It can be eliminated by arbitrarily allocating the design frequency of exceedance amongst several portions of the flight. For example, the permissible 2 x 10<sup>-)</sup> exceedances per hour might be divided equally,  $1 \times 10^{-5}$  to a low-temperature portion of the flight and  $1 \times 10^{-5}$  to a high-temperature portion. If, under this arbitrary allocation, the lowtemperature portion is found to be critical, the allocation could be changed, say, to  $1.8 \times 10^{-5}$  exceedances per hour for the low-temperature portion and  $0.2 \times 10^{-5}$  for the high-temperature portion. Under any arbitrary allocation, as long as each set of loads is within the limit strength corresponding to its allowables, the total exceedances of limit strength will not exceed the design value of 2 x 10-5 per hour defined in Section 15. (It will be noted that the allocation principle used here is quite similar to that described in Section 15.2.3 for treatment of stability augmentation system malfunction under a design envelope form of criterion.)

The same objective might also be achieved by obtaining exceedance curves for y/ylimit instead of for y. The value of ylimit would, in general, be different for each mission segment. This approach would make unnecessary the arbitrary allocation of exceedances amongst mission segments. It would, however, appear to lead to a variety of difficulties in practical application, especially where the "matching condition" technique is to be used.

Transient stresses due to non-uniform thermal expansion will also require special treatment. In principle, these stresses can simply be added to the one-g level flight stresses for each mission segment.

16.3.2 Design Envelope Criterion. Under the design envelope form of criterion, the A value for each load quantity for each flight condition is multiplied by the appropriate  $\sigma_W$   $\eta_d$  value as specified in Section 15 to obtain a design load value.

The problems mentioned above as likely to occur in application or the mission analyses form of criterion to advanced configurations do not appear with the design envelope form of criterion.

## 16.4 Generation of Matching Conditions; Joint Probability Analysis

At this stage, the procedures become quite different, depending upon whether the matching condition or joint probability technique is to be used.

If the matching condition technique is to be used, some consideration should be given to the degree of conservatism that will be acceptable in matching the statistically defined loads. If gust loads are critical, a refired technique comparable to that described and illustrated in detail in Appendices C and D would ordinarily be appropriate. On the other hand, if considerable conservatism can be allowed, conservative assumptions should be made as appropriate to minimize the work. For example, maximum bending moments and maximum torsions (about the elastic axis) can be assumed to occur simultaneously, with each of the four combinations of sign.

The technique to be followed in matching the statistically defined loads will be essentially the same for a mission analysis as for a design envelope form of criterion. Some minor differences are pointed out in Section 11.1 and others will be evident from a study of Appendix C. In addition, it might be noted that, in utilizing the design envelope form of criterion, a major effort should be made to eliminate non-critical conditions based on values of  $(\overline{A})$   $(\sigma_{\overline{W}} \eta_{\overline{M}})$  prior to generation of the matching conditions, so that the number of design envelope points for which matching conditions are generated can be held to a minimum.

If the joint probability technique is to be used, it will be generally in accordance with the procedures described in Reference 1. The amount of computation indicated therein in conjunction with the design envelope form of criterion, however, will be greatly reduced, inasmuch as the calculations need be carried out for only a single  $\sigma_{\rm W}$  value for each flight condition.

For advanced configurations, particularly those characterized by low-aspect-ratio wings, some increased difficulty in applying either the matching condition or joint probability technique is likely to be encountered.

In the matching condition technique, more matching conditions may be required, and it will probably be necessary to examine a greater number of internal stresses, both actual and ficticious. As a result, however, of limited experience in matching statistically defined taxi loads for a delta wing airplane, it appears that the matching condition concept will still be quite practical to apply.

Considerably increased difficulty would be expected, in either the matching condition or joint probability technique, if it became necessary

to include wing rib bending stresses. The stress condition at a point on the surface would then be defined by tension-compression stresses in two directions and a shear stress, rather than only one tension-compression stress and a shear stress. A three dimensional instead of a two dimensional treatment would then be required. Hopefully, simple conservative assumptions regarding rib bending stresses will usually be acceptable, so that the complexities of treating rationally the additional stress component can be avoided.

### 17 THE PLACE OF THE DISCRETE GUST CONCEPT

The present study has been directed explicitly toward the development of a power-spectral gust design procedure, with the future role of the present discrete gust requirement not intended to be a part of the study. At the same time, the selection and development of a power spectral gust criterion is bound to be influenced at least indirectly by the role which the discrete gust concept will continue to play. In addition, in the course of developing the power-spectral criteria, various thoughts have crystalyzed regarding the relation between the power-spectral and discrete-gust approaches. As a result, some discussion of the future role of the discrete gust criterion is considered appropriate.

Historically, as the continuous turbulence concept gradually gained acceptance, good engineering judgment dictated the use of both the old and the new concepts in combination until sufficient experience could be gained to assure that the newer approach would be adequate by itself. Now, however, it appears that the need for a discrete gust criterion is diminishing. Some of the factors leading to such a conclusion are indicated by the following comments.

- 1, First, while reasonably discrete gusts undoubtedly occur in the atmosphere, there is accumulating evidence that the preponderence of gusts are better described in terms of continuous turbulence. It has long been accepted that clear air turbulence at moderate intensity levels is generally continuous in nature. Thunderstorm gust velocity profiles are now available in considerable quantity, for example in References 14 and 28; these almost invariably display the characteristics of continuous turbulence. Also, the extremely severe low level turbulence of which measurements are reported in references 29 and 30 is also understood to have consisted largely of continuous turbulence, although a number of severe discrete gusts were also encountered.
- 2. Second, it has become more and more evident that elastic mode dynamic efforts must be treated on a power-spectral basis. The elastic mode effects, in a discrete gust analysis, are highly sensitive to the gust gradient distance. Yet the problems of selecting a gust gradient distance and of relating the gust velocity to this gradient distance appear as insurmountable now as when the continuous turbulence concept was first introduced, offering for the first time a practical way of bypassing this knotty problem. In order for a discrete-gust dynamic analysis to be realistic for design loads determination, data on the joint probability of gradient distance and gust velocity for discrete gusts would be required. Such data simply are not available, nor are they likely to become available. One cannot help feeling, however, that the relation of gust intensity to

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gust wavelength inherent in the power-spectral description of atmospheric turbulence is probably quite representative of discrete gusts as well as continuous turbulence. Consequently, as long as the various elastic modes are all fairly well damped, the power spectral analysis should duplicate reasonably well the results that a discrete gust analysis would yield if the necessary statistical data were available and incorporated. For a system with poorly damped modes, of course, the continuous turbulence analysis would be required regardless of whether a discrete gust analysis were performed, in order to account for resonant build-up of load at the natural frequencies.

3. From a static loads standpoint, the impression has prevailed that gust loads are not sensitive to the gradient distance and that the discrete-gust and power-spectral approaches should lead to nearly identical results. Instances have been found, however, where discrete-gust and power-spectral approaches give results differing by rather sizable amounts.

In order to study these differences, values of  $\sigma_W \, \eta_{\rm d}$  necessary to give the same airplane load factor as a 50 fps discrete gust (U<sub>de</sub>) have been obtained for a number of representative airplanes. The discrete gust is defined as in FAR 25, and the gust velocity is considered to decrease with altitude above 20000 ft. as indicated therein. For the purpose of this comparison, the airplanes are considered to be rigid and restrained to plunge only. Under these assumptions, the desired  $\sigma_W \, \eta_{\rm d}$  values are given by

$$\sigma_{\rm w} \, \eta_{\rm d} = U_{\rm de} \, \frac{K_{\rm g}}{K_{\rm \sigma}} \, \frac{1}{\sqrt{\sigma}}$$

where  $K_g$  is the discrete gust alleviation factor, evaluated in accordance with FAR 25, and  $\sigma$  is the atmospheric density ratio. Values of  $K_{\sigma}$  are read from Figure 5-2. (These  $K_{\sigma}$  values are slightly low due to the approximations to the lift growth functions used in obtaining the curves; use of "precise" values would have decreased the  $\sigma_W$   $\eta_d$  values obtained by about 8%).

If, at each altitude, the value of  $\sigma_W$   $\eta_d$  necessary to give the same load factor as a 50 fps discrete gust were found to be the same for all airplanes, it would make no difference whether a discrete gust or power-spectral criterion were used. But suppose that different values are found. If the various airplanes had all been designed to the same  $U_{de}$ , their capabilities to withstand continuous turbulence, as measured by the  $\sigma_W \eta_d$  value made good, would then differ. If the airplane making good the highest  $\sigma_W \eta_d$  were considered just adequate from

a gust loads standpoint, its  $\sigma_W \eta_d$  would define the appropriate design level of  $\sigma_W \eta_d$ , and the other airplanes would be deficient.

Results for the various airplanes are shown by the dash lines in Figure 17-1. The background grid of lines of constant  $N(y)/N_0$  is the same as in Figure 5-8. Curve A shows the  $\sigma_W \eta_d$  values corresponding to the prescribed  $U_{de}$  for the Table la airplane of NACA TN 4332. This is a typical 4-engine piston-powered transport. Curve B reflects a 50% increase in wing loading and is roughly representative of the Model 188. Curve C reflects a further increase of 33% in wing loading. Curve D represents a large delta wing airplane representative of proposed supersonic transport configurations;  $W/C_{L,\alpha}S$  is the same as for curve C, but the wing chord is increased by a factor of five. Curve E reflects the result of a 50% decrease in wing loading relative to curve A and is representative of the DC-3 generation of transports.

The knuckle in each curve at 20000 ft. reflects the variation of  $U_{\rm de}$  with altitude. The slight unfairness that may be noted in some of the curves apparently is the result of difficulty in reading the curves of Figure 5-2 accurately at the low values of  $\mu$ .

The fairly substantial differences between these curves indicate that the discrete gust and power-spectral approaches can give significantly different results, even where resonant build-up in poorly damped modes cannot be a contributing factor. For example, suppose that airplanes A and D were each designed to a 50 fps discrete gust. For flight through continuous turbulence at sea level, airplane A would be good for a turbulence intensity of  $\sigma_W \eta_d = 93$  fps. Airplane D, on the other hand, would be good for a turbulence intensity of only  $\sigma_W \eta_d = 65$  fps. Its actual loads in a given patch of turbulence, relative to those of airplane A, would be greater than predicted by discrete gust theory, therefore, in the ratio 93/65 = 1.43.

The reasons for this difference are not hard to understand.

First, in the discrete gust methods now in use, the length of gust is assumed to be proportional to the wing mean chord. This assumption simplifies the calculations, and for past airplanes it may have been fairly realistic. However, the extremely long chord of airplane D results in a gust so long that the airplane tends to rise with the gust and develop relatively little load. Further, this alleviating effect of gust length is not offset by any increase in gust velocity.

CURVE A: TABLE 10 AIRPLANE OF TN 4332

CURVE B: SAME AS A EXCEPT W/CL S INCREASED IN RATIO 1.5

CURVE C: SAME AS A EXCEPT W/CL S INCREASED IN RATIO 2.0

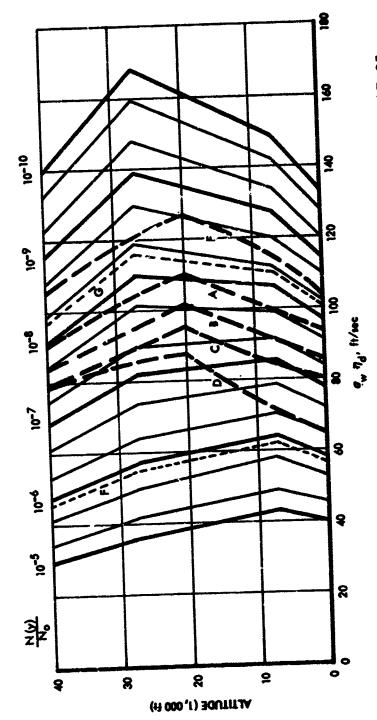
CURVE C: SAME AS A EXCEPT W/CL S INCREASED IN RATIO 2.0 AND C IN RATIO 5.0

CURVE E: SAME AS A EXCEPT W/CL C DECREASED IN RATIO .5

CURVE E: SAME AS A EXCEPT W/CL D DECREASED IN RATIO .5

CURVE F: DESIGN LEVEL\* SECTIONS 15.2.7 AND 15.3.3(a)

Battle cases of



17-1. " W" d VALUES GIVING SAME LOAD FACTOR AS FAR 25 Vc DISCRETE GUST (Ude = 50 FPS BELOW 20000 FT) FIGURE 17-1.

On the other hand, the power-spectral treatment of atmospheric turbulence reflects the fact that the longer-gradient gusts tend to have significantly higher gust velocities. This effect of wing chord explains the difference between curves C and D in Figure 17-1.

Second, because of its higher value of  $W/C_{L,Q}$  S, airplane D acquires vertical velocity less rapidly as it enters any given gust. This phenomenon is reflected in higher alleviation factors on both discrete gust and power spectral bases. On encountering gusts of various wavelengths, however, airplane D - and likewise airplane C - will tend to feel the longer wavelength gusts that airplane A rides over. In contrast to the discrete gust formula, the power spectral treatment reflects the mixture of gusts of all wavelengths and the righer gust velocities associated with the longer wavelengths. This effect of a higher value of  $W/C_{L,Q}S$  explains the difference between curves A and C in Figure 17-1.

Thus it is evident that the relation of gust intensity to gradient distance is important from the standpoint of static as well as dynamic loads determination.

- 4. As indicated by the above discussion, it appears that the power spectral approach accounts much more realistically for the actual mix of gust gradient distances in the atmosphere and for the variation of gust intensity with gradient distance than does the present discrete gust formula, on a static as well as on a dynamic loads basis. As a result, the power spectral approach probably does a better job of accounting for loads due to actual discrete gusts than does the present discrete gust requirement. With a comprehensive power spectral gust loads criterion in use which will be necessary in any event to provide for the situation of a possible resonant build-up of response in poorly damped modes it would appear that the discrete gust situation is inherently provided for and that a specific dynamic or static discrete gust criterion is not necessary in addition.
- 5. A power-spectral method of analysis is not necessarily more difficult to apply than a discrete gust method. The present static-load plunge-only discrete-gust method can, in fact, be converted to a power-spectral basis by making just two changes:
  - (a) Replace the discrete-gust alleviation factor by an alleviation factor read from curves such as those of Figure 5-2 herein.

(b) Replace the specified value of  $U_{de}$  with a specified value of  $\sigma_v$   $\eta_d$  (varying appropriately with altitude).

The discrete gust and power spectral procedures in this case are essentially identical. In using the power spectral rather than the discrete gust data, one needn't even be aware that it is no longer discrete gusts that are described.

To be sure, this simple rigid-airplane analysis does not exploit the full potentiality of the power-spectral approach. But it does account more realistically for the actual mix of gust gradient distances in the atmosphere and the variation of gust intensity with gradient distance. Furthermore, as additional rigid and elastic degrees of freedom are introduced, the added complexity is due to the additional degrees of freedom rather than to the power-spectral treatment. And if the added degrees of freedom are important to the result, they are likely to be important on a discrete-gust as well as a power-spectral basis.

To further emphasize the parallelism of the discrete gust and power-spectral forms of criterion, it is of interest to compare the dash-line curves in Figure 17-1, representing the levels produced by the 50 fps discrete gust criterion, with the design levels selected in Section 15. The latter are  $N(y)/N_0 = 1.2 x$  $10^{-6}$  for the design envelope criterion and  $N(y)/N_0 = 1.2 \times 10^{-6}$ as a lower bound and 6 x 10-9 as an upper bound for the combined criterion (Curves F and G respectively in Figure 17-1). In making this comparison, it should be borne in mind that the 50 fps discrete gust velocity has generally been employed on a static basis and has provided sufficient strength to cover whatever dynamic effects are present - on the order of 40% of the static loads in the case of the Model 188, for example, as indicated by the A values for cases 202 and 202 Rigid in Tables B-9(b) and (c). Consequently, when the elastic-mode dynamic effects are to be included explicitly in the analysis, the  $\sigma_{\rm W}\eta_{\rm d}$  values indicated by the dash lines would be divided by the dynamic factor of 1.40 as well as by the factor of about 1.08 which accounts for the unconservatism in Figure 5-2. Dividing the Curve B (Model 188) value at 12,000 ft. by (1.08) (1.40) gives  $\sigma_W \eta_d = 63$ , which is very close to the value of 60 actually obtained in Section 13.

As a result of the above considerations, it appears that the discrete gust concept has largely served its purpose and that airworthiness requirements based thereon can be dropped at such time as suitable power-spectral criteria are adopted.

## CONCLUSIONS

- 1. Three forms of power-spectral gust loads criteria have been developed. All of these properly account for the continuous nature of atmospheric turbulence. They differ, however, in the degree to which they take account of how closely normal operational flight conditions approach the design envelope.
- 2. A combined form of criterion, embodying both the mission analysis and design envelope concepts, is considered to be the most desirable. In this criterion, two alternatives are offered. Under the first, appropriate for an airplane that is not gust critical, loads are obtained on a design envelope basis at a sufficiently severe  $\sigma_W \eta_d$  level to assure an adequate structure no matter how severe the actual airplane operation may be relative to the design envelope, subject only to the design envelope not being exceeded. In the second, loads are obtained on a mission analysis basis, reflecting the actual operation expected; in addition, loads are obtained on a design envelope basis, at a considerably lower  $\sigma_W \eta_d$  level, in order to provide a "floor" below which the loads will not be allowed to fall.
- 3. The "combined" form of dynamic gust loads criterion is sufficient to assure adequacy of a new design from a gust loads standpoint. A static or dynamic discrete gust criterion would not be necessary in addition to the power-spectral criterion.
- 14. Limit-strength frequency of exceedance values for the reference airplanes, based upon mission analysis calculations, are:

# Vertical gust

Model 188					exceedances		
Model 749					exceedances		
Model 720	$\mathbf{B}  \mathbf{N}(\mathbf{y})$	=	1.1 x	10-5	exceedances	per	hour

#### Lateral gust

```
Model 188 N(y) = 6.0 \times 10^{-5} exceedances per hour Model 749 N(y) = 2.5 \times 10^{-4} exceedances per hour Model 720B N(y) = 4.0 \times 10^{-6} exceedances per hour
```

For these airplanes, vertical gust values are governed by wing strength and lateral gust values by tail strength. The Model 720B lateral gust value is for yaw damper off.

5. Limit strength values of  $\sigma_W \eta_d$  for the reference airplanes at speed  $V_C$ , based upon critical design envelope points are:

### Vertical gust

```
Model 188 \sigma_W \eta_d = 60 \text{ fps at 12,000 ft.} (N(y)/N_0 = 1.2 \times 10^{-6})

Model 749 \sigma_W \eta_d = 88 \text{ fps at } 7,000 \text{ ft.} (N(y)/N_0 = 7 \times 10^{-8})

Model 720B \sigma_W \eta_d = 111 \text{ fps at 22,000 ft.} (N(y)/N_0 = 8 \times 10^{-9})
```

### Lateral guat

```
Model 188 \sigma_{\rm W} \eta_{\rm d} = 61 fps at 7,000 ft.(N(y)/N<sub>0</sub> = 1.4 x 10<sup>-6</sup>)
Model 749 \sigma_{\rm W} \eta_{\rm d} = 65 fps at 7,000 ft.(N(y)/N<sub>0</sub> = 8 x 10<sup>-7</sup>)
Model 720B \sigma_{\rm W} \eta_{\rm d} = 99 fps at 23,000 ft.(N(y)/N<sub>0</sub> = 2.4 x 10<sup>-8</sup>)
```

Again, the vertical gust values are governed by wing strength. The lateral gust values are governed by tail and aftbody strength. The Model 720B lateral gust value is for yaw damper off.

- 6. Although both the Model 188 and Model 749 limit-strength frequency of exceedance due to lateral gust is higher than due to vertical gust that is, the vertical tail is critical the design frequency of exceedance should be taken at the more conservative level based on wing strength. It is believed that actual lateral gust loads may be somewhat lower than indicated by the analysis because of the ability of the pilot to provide additional Dutch roll damping by use of the controls.
- 7. Appropriate design levels for use on new airplanes are concluded to be:

For a mission analysis:  $N(y) = 2 \times 10^{-5}$  exceedances per hour.

For a design envelope criterion if used alone or for the design envelope "floor" in the combined criterion:  $\sigma_{\rm W} \eta_{\rm d}$  to be as defined by N(y)/N<sub>0</sub> = 1.2 x 10<sup>-6</sup> in Figure 5-8 (corresponding to  $\sigma_{\rm W} \eta_{\rm d}$  = 62 fps at 7000 ft.)

For the conservative design envelope loads obtained in lieu of a mission analysis under the combined criterion:  $\sigma_{\rm W} \eta_{\rm d}$  to be as defined by  $N(y)/N_0 = 6 \times 10^{-9}$  in Figure 5-8 (corresponding to  $\sigma_{\rm W} \eta_{\rm d} = 110$  fps at 7000 ft.)

The above  $\sigma_W \eta_d$  values are for speed  $V_C$ . At speed  $V_B$ , design should be to 66/50 of the  $V_C$  values, and at speed  $V_D$ , to 25/50 of the  $V_C$  values.

8. The description of the atmosphere to be used in conjunction with the stated design levels of N(y) and  $\sigma_{\rm W} \, \eta_{\rm d}$  utilizes a shape of power spectral density function given by the isotropic turbulence equation,

$$\phi(\Omega) = \frac{\sigma^2 L}{\pi} \frac{1 + \frac{8}{3} (1.339 L\Omega)^2}{\left[1 + (1.339 L\Omega)^2\right]^{11/6}}$$

with L = 2500 ft. The  $\sigma_w$  distributions for use in the mission analysis are defined by b and P values in equation 5-2 herein as given by Figures 5-3 and 5-4. This description, were it to be used on an absolute basis (that is, independently of the limit design levels established herein) would be slightly conservative.

- 9. Either a "matching condition" or a "joint probability" technique can be used to integrate the statistical loads determination with the stress analysis operation. The application of each is illustrated. Use of the joint probability technique is likely to be limited to the final stage of design. The matching condition, or single parameter, technique can be applied in various degrees of refinement and is appropriate for use at all stages of design.
- 10. Exact consistency of the joint probability and the matching condition or single parameter techniques is not to be expected, because of the subtle difference in the design philosophy reflected. However, the numerical differences are very small.
- 11. There is some indication that aerodynamic induction effects and transient lift growth may have a much greater influence on the gust response of a rigid airplane free to pitch than has previously been realized. Inasmuch as rather crude assumptions in this area have generally been regarded as entirely acceptable, further research is considered urgent.

### APPENDIX A

# COMPARISON OF ASD TR 61-235 AND TN 4332 $\sigma_{ m w}$ DISTRIBUTIONS

Comparisons of the ASD TR 61-235 and TN 4332 P and b values are shown in Figures A-1 through A-4. The over-all effect on the  $\sigma_{\rm W}$  distributions, as reflected in plots of N(y)/N<sub>O</sub> vs y/A, is then shown in Figures A-5 and A-6.

In these comparisons, the "As Published" P and b values are taken directly from the respective sources. They are for use with a Liepmann spectral shape with L = 1000 ft., except that the ASD TR 61-235 values below an altitude of 5000 ft. are associated with reduced values of L. Although not applicable in the present work, TN 4332 "Missile"  $P_2$ 's (no storm avoidance) are included as a matter of interest.

The ASD TR 61-235 "Modified" P and b values are as defined by Figures 5-3 and 5-4.

The TN 4332 "Modified" values are obtained so as to be generally consistent with the ASD TR 61-235 "Modified" values. The same factors are applied to  $P_1$  and  $P_2$  as in obtaining the ASD TR 61-235 "Modified" values. The computation of  $b_1$  and  $b_2$  values is shown in Tables A=1 and A=2. These tables follow the format of Tables Ia and Ib of TN 4332, but the computations differ as follows:

- (1) The quantity labeled  $\sqrt{I(K,S)/\pi}$  in TN 4332 and designated  $K_{\sigma}$  herein is read from curves based upon the "isotropic turbulence" spectrum (Figure 5-2), at a value of L=2500 ft., instead of from Fig. 7 of NASA TR 1272 (based upon the Liepmann spectrum) at L=1000 ft.
- (2) The lift curve slope is taken as

1.15 
$$\frac{6A}{A+2}$$

where A is the aspect ratio, the quantity 6A/(A+2) is an excellent approximation of the lift curve slope for wing alone, and the factor 1.15 accounts for the average ratio of airplane to wing lift curve slope. The value thus obtained is used both where the lift curve slope appears explicitly in Equation (17) of TN 4332 (Equation 5-5 herein) and in evaluation of the mass parameter. The inclusion of the 1.15 factor in the equation itself results in its appearance in the heading of Column 9 of Tables A-1 and A-2.

Its inclusion in the mass parameter accounts for its appearance in the heading of Column 4.

Column 4, designated  $\overline{\mu}$ , corresponds to "K" in Tables 1a and Ib of TN 4332. However, a factor of 4 has been omitted for consistency with the Pratt mass parameter (NASATR 1206, Reference 31); and, as noted above, the theoretical lift curve slope of  $2\pi$  is replaced by an estimated actual lift curve slope.

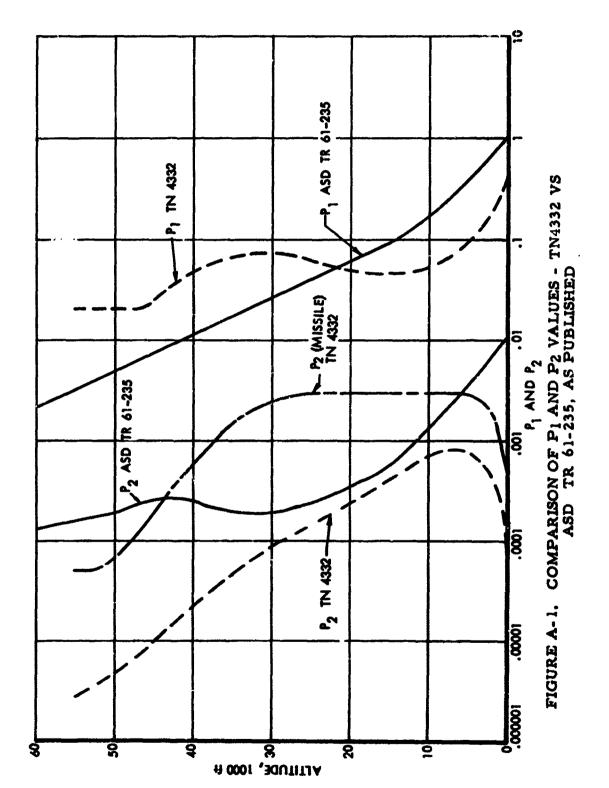
(3) A revised estimate of dynamic factor is included in the final evaluation of b<sub>1</sub> and b<sub>2</sub> in Column 10. The dynamic factor calculated for the Lockheed Model 749A Constellation (ratio of rms values, flexible to rigid, based on the Liepmann spectrum with L = 1000 ft.) is 1.07. Values quoted for the DC-6 and DC-7 in ASD TR 61-235 range from 1.02 to 1.07. A value of 1.06 is considered representative, and the ratio of the value 1.20 used in TN 4332 to this value is is 1.13. This factor provides what is in effect an adjustment to the Ude levels and could properly have been applied as a factor to either the 2.2 coefficient in Column 2 or to C in Column 9.

No correction for ritch is included. As indicated in connection with the modification of the ASD TR 61-235  $b_1$  and  $b_2$  values, analysis based on the Model 749 has shown the effect of pitch to be small. Further, whereas inclusion of pitch would reduce  $\overline{A}$  by about 7%, use of more exact lift growth functions in the plunge-only analysis would increase  $\overline{A}$  by almost exactly the same amount.

It will be noted that the "ASD TR 61-235 Modified" and the "TN 4332 Modified" b's are inconsistent to the extent of about 7%, because of the differences in the lift growth functions assumed in the original determinations. To remove this inconsistency it would be necessary to increase the ASD TR 61-235 b values.

It may be remarked that no inconsistency results from not modifying the lift curve slope in evaluating the Pratt mass parameters (Column 3) or in the equation for  $\overline{C}$  (Column 9). A modification to  $\overline{C}$  will result in an equal and opposite modification to the coefficient 2.2 in Column 2 and hence will have no effect on the results.

It is interesting to note that although the differences between TN 4332 and ASD TR 61-235 b and P values appear rather great (Figures A-1 through A-4), the resulting generalized exceedance curves (Figures A-5 and A-6) show much closer agreement.



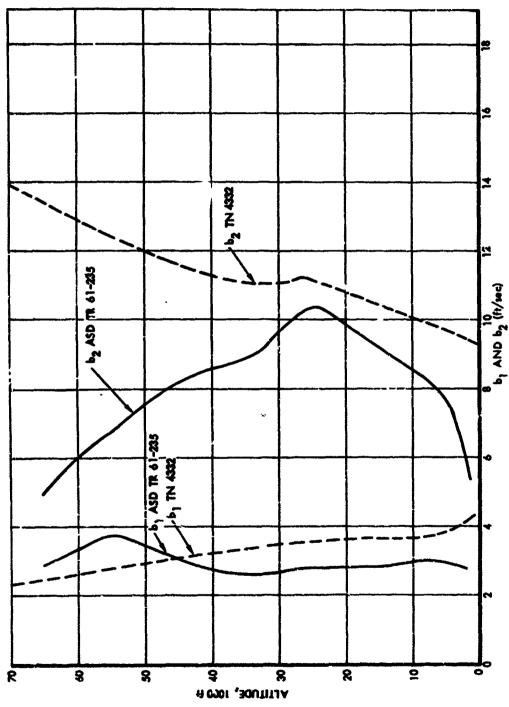


FIGURE A-2. COMPARISON OF b1 AND b2 VALUES -TN 4332 VS ASD TR 61-235, AS PUBLISHED

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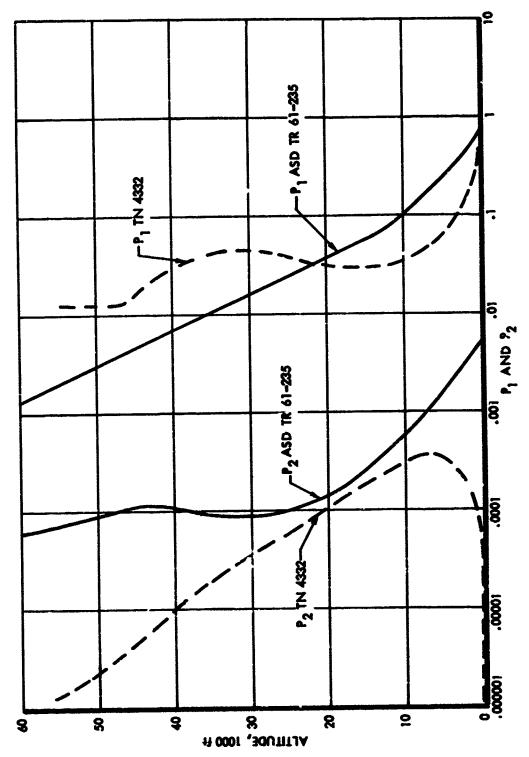


FIGURE A-3. COMPARISON OF P1 AND P2 VALUES -TN 4332 VS ASD-TR-61-235, MODIFIED

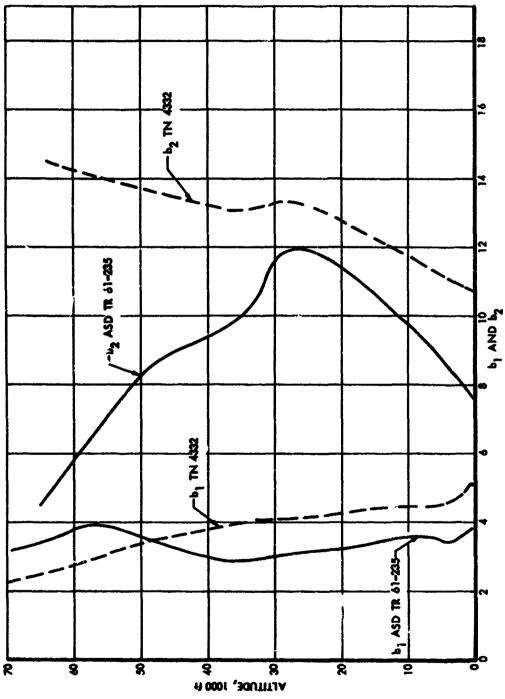
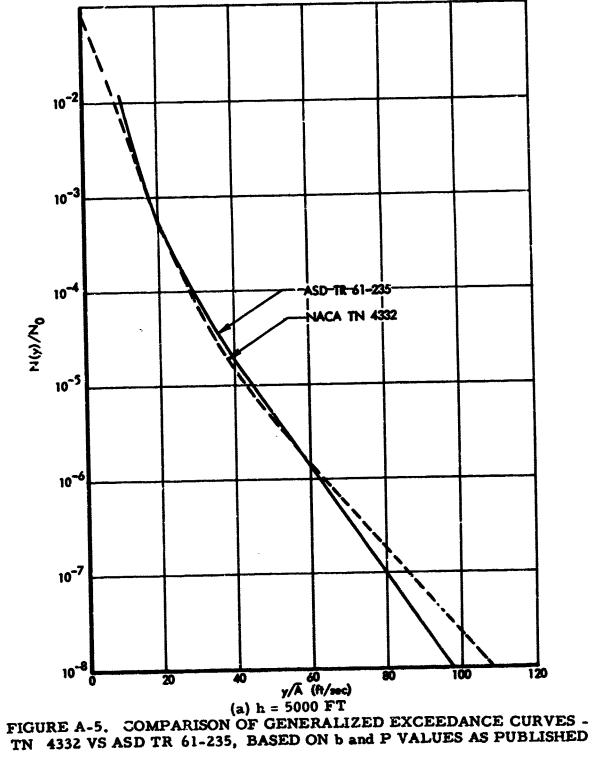
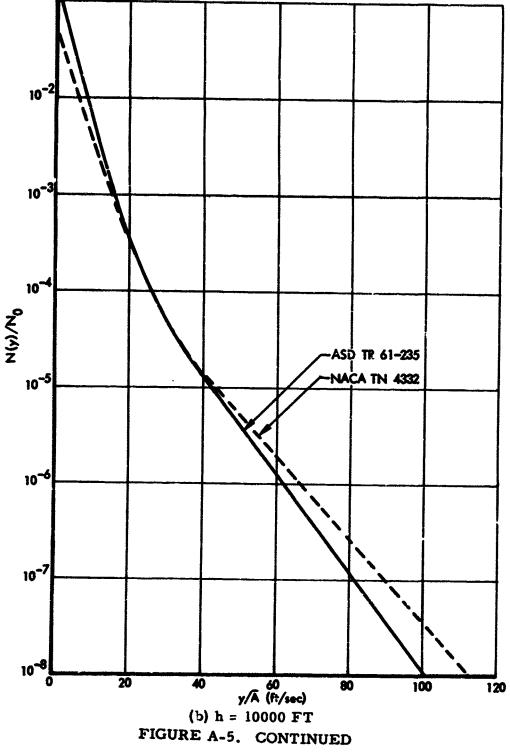
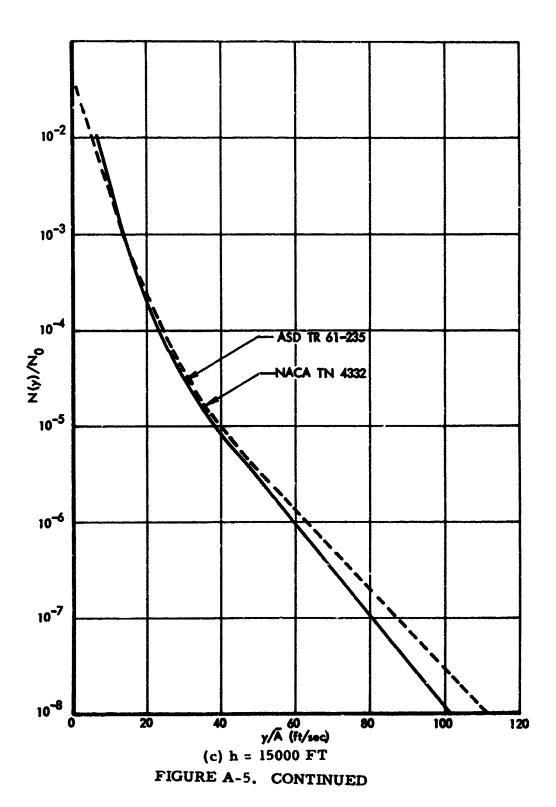


FIGURE A-4. COMPARISON OF b1 AND b2 VALUES -TN 4332 VS ASD TR 61-235, MODIFIED

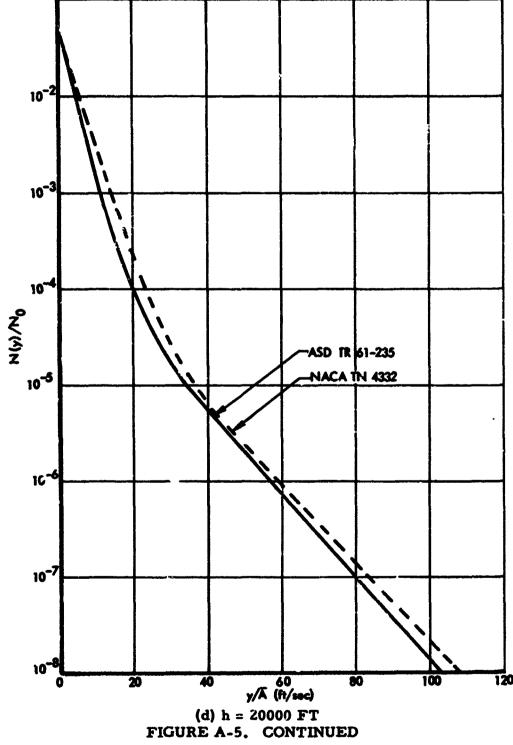
The second secon

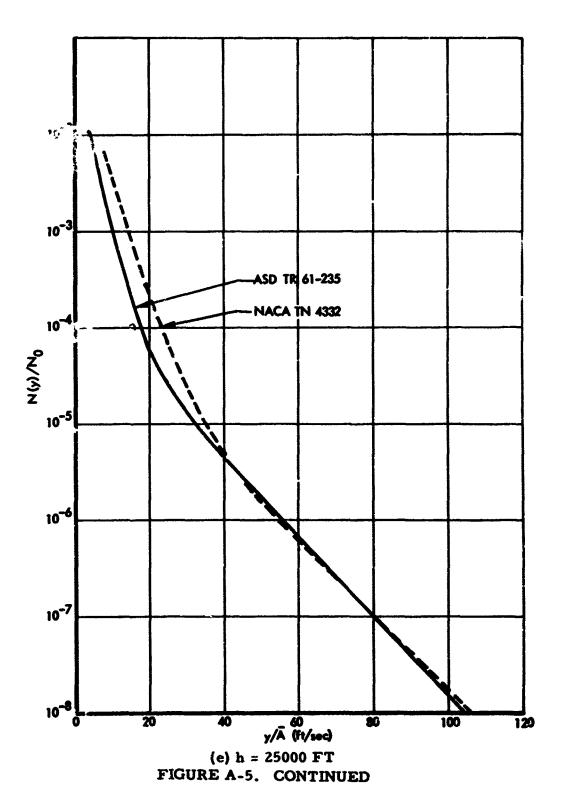




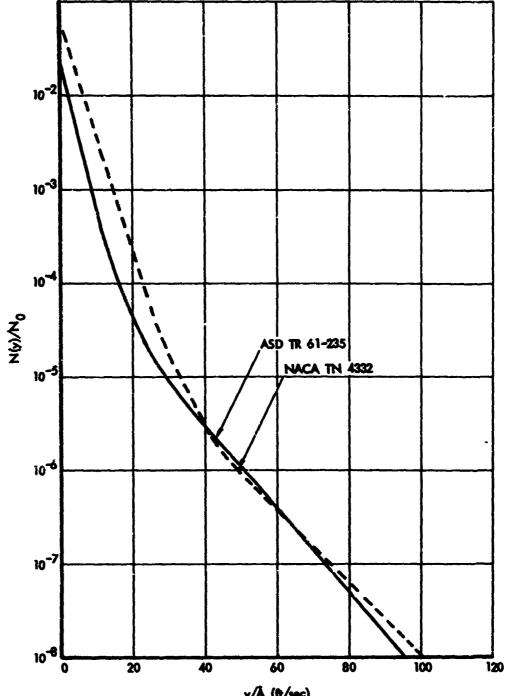


**A-9** 

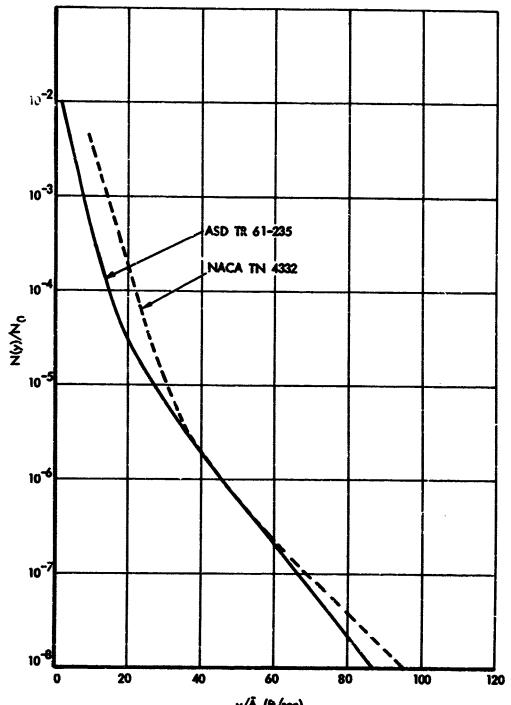




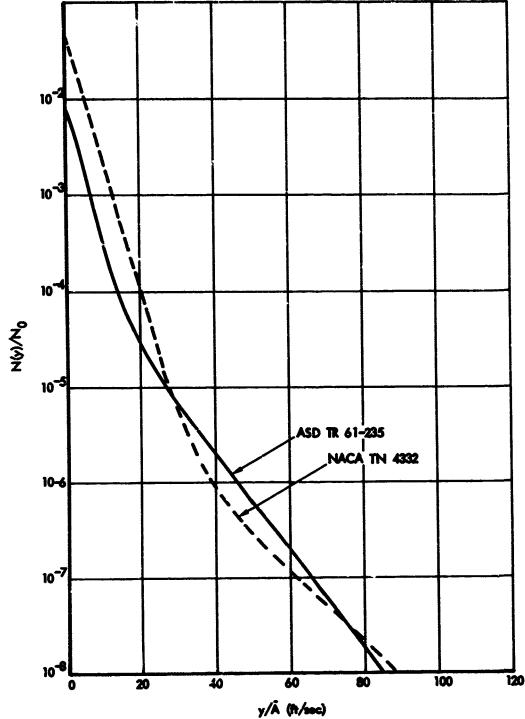
A-11



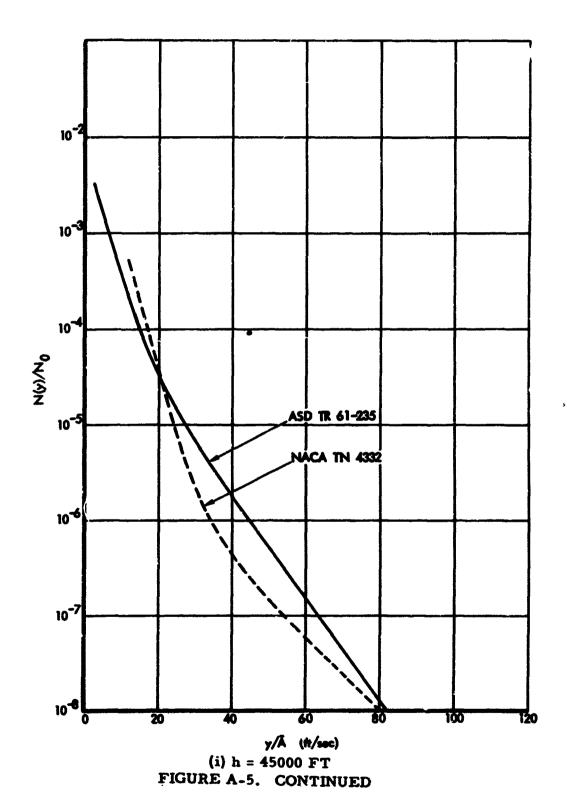
y/Å (ft/sec)
(f) h = 30000 FT
FIGURE A-5. CONTINUED



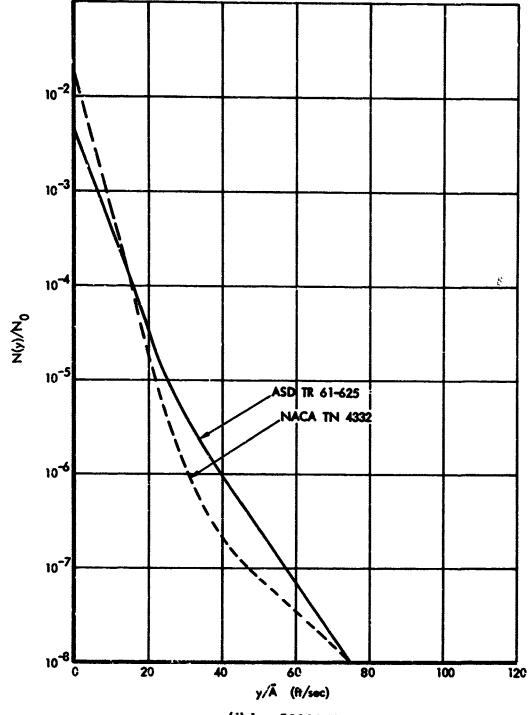
y/Å (ft/sec)
(g) h = 35000 FT
FIGURE A-5. CONTINUED



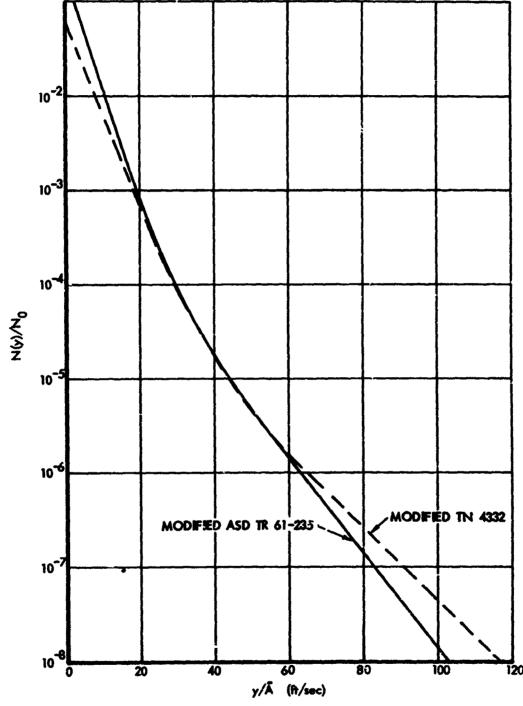
y/Å (ħ/sec)
(h) h = 40000 FT
FIGURE A-5. CONTINUED



A-15

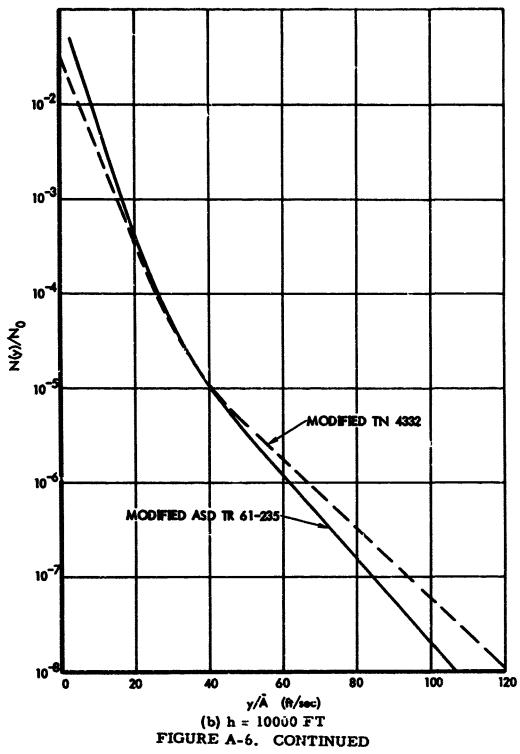


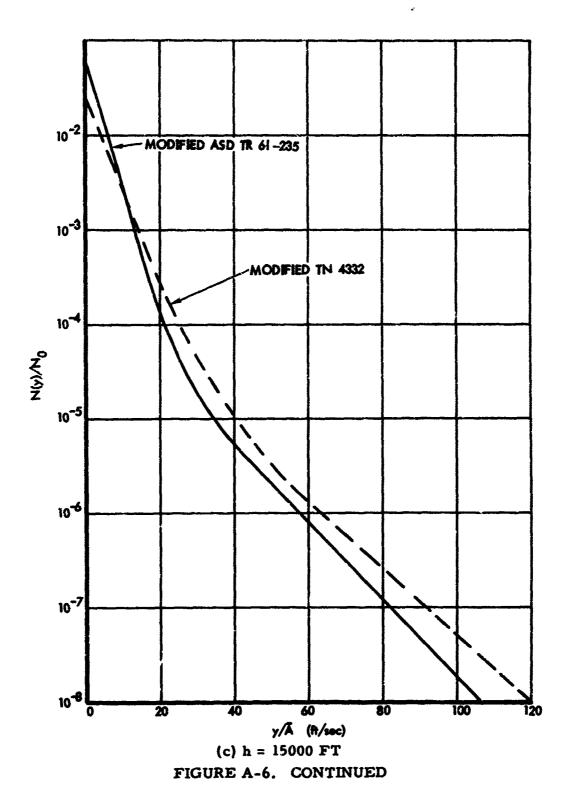
(j) h = 50000 FT FIGURE A-5. CONCLUDED



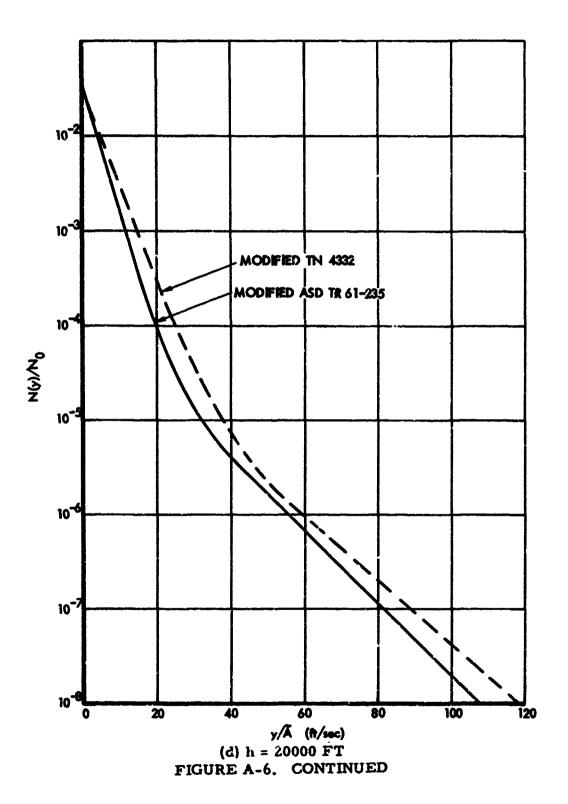
(a) h = 5000 FT

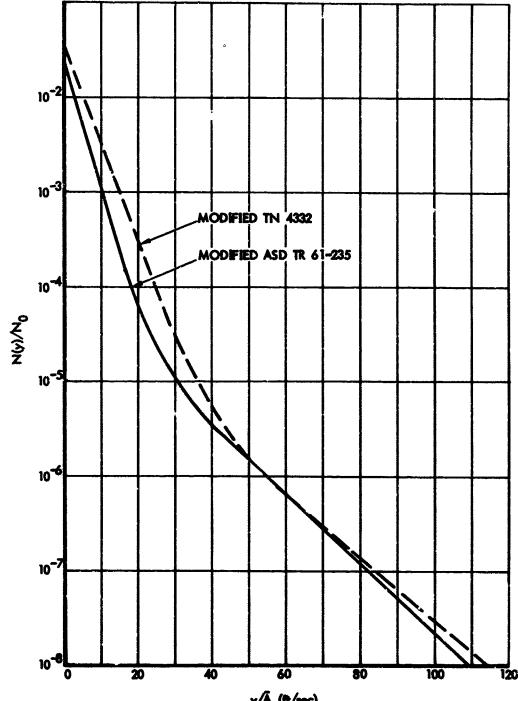
FIGURE A-6. COMPARISON OF GENERALIZED EXCEEDANCE
CURVES - TN 4332 VS ASD TR 61-235, BASED ON MODIFIED
b AND P VALUES





A-19





y/A (R/sec)
(e) h = 25000 FT
FIGURE A-6. CONTINUED

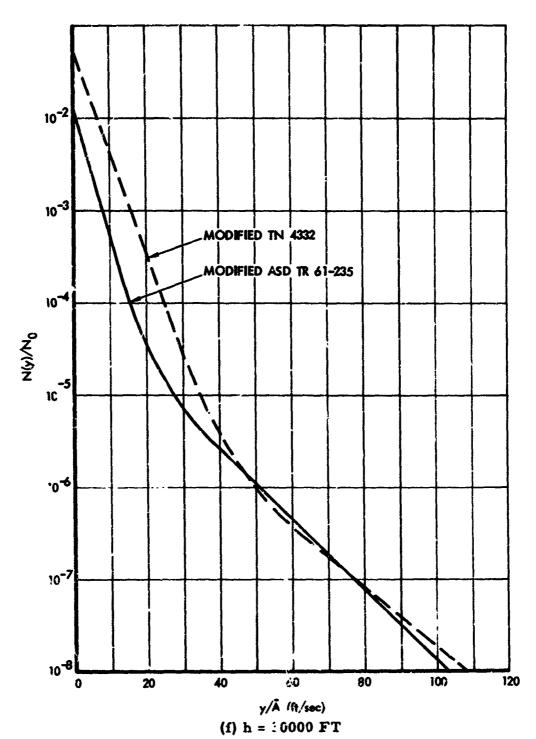
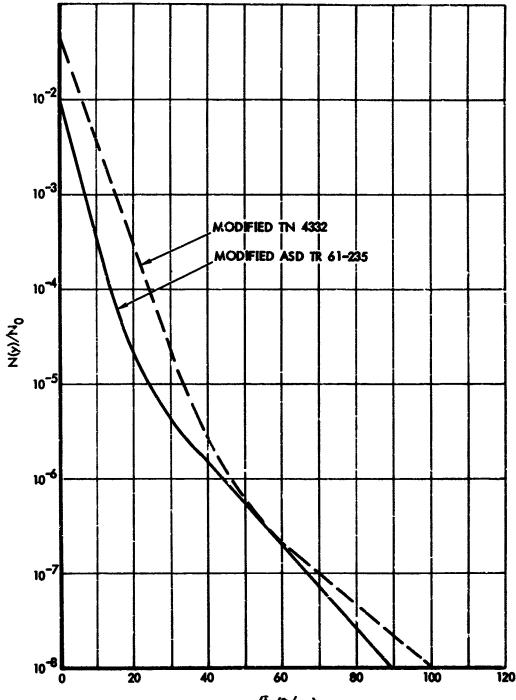
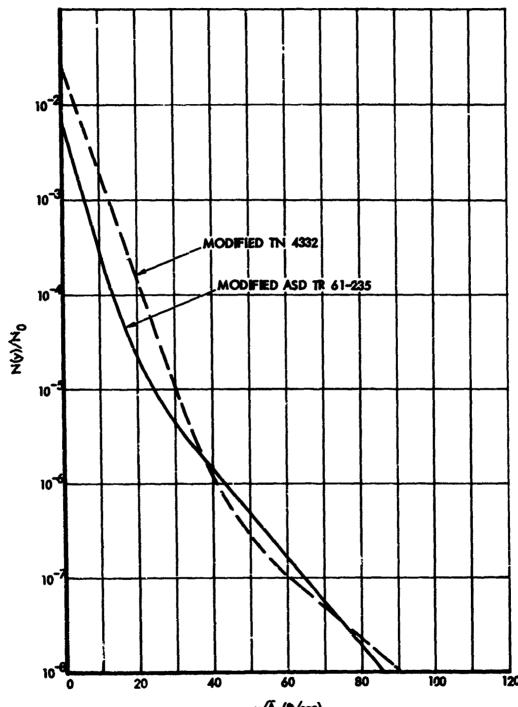


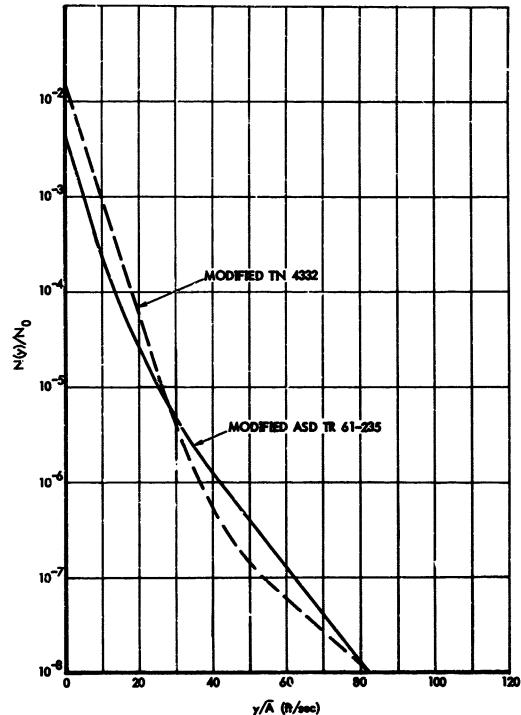
FIGURE A-6. CONTINUED



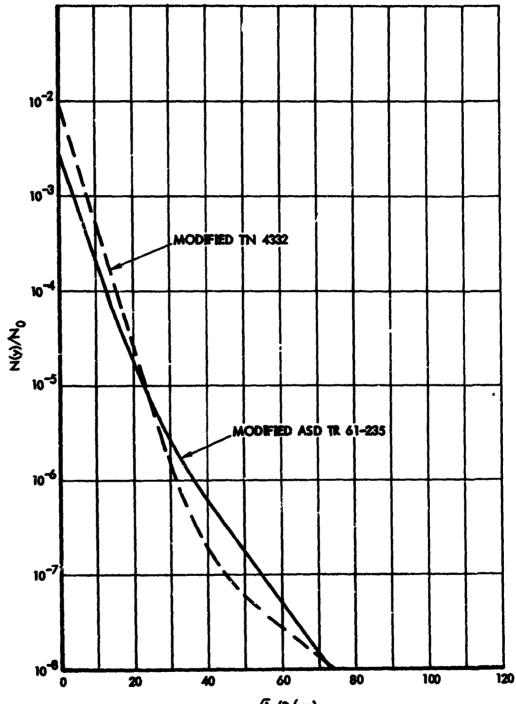
y/A (ft/sec)
(g) h = 35000 FT
FIGURE A-o. CONTINUED



y/Ā (ħ/sec)
(h) h = 40000 FT
FIGURE A-6. CONTINUED



y/A (R/sec)
(i) h = 45000 FT
FIGURE A-6. CONTINUED



y/A (A/sec)
(j) h = 50000.FT
FIGURE A-6. CONCLUDED

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TABLE A-1. RE-EVALUATION OF PARAMETER b<sub>1</sub> BASED ON TN 4332 DATA

ලු	, P	E 1.13	50.5	ंच-च	O1.4	4.12	%.°	3.58	3.06
0	2	<del>ŠĽ</del>	<b>u</b> ·τ	1.79	1.95	2.14	2.36	5°64	3.08
@	1 P		1.015	1.094	1.261	1.464	1.797	2.278	2.893
Θ	× <sub>a</sub> r <sub>o</sub>	ම	1.94	1.88	1.78	1.65	1.51	1.33	1.20
9	Къ	Function or (1) Figure 5-2	.363	.385	, 427	<b>28</b> 1.	445.	.63	.708
<b>©</b>	K 8	Function or (3) TWW 332 Table Is	.703	.722	.758	. 798	.823	048.	.850
<b>②</b>	12	<u>©</u>	18.3	21.1	28.1	39.9	57.0	91.8	148.0
0	Pratt µ	TN4332 Table is	21.0	24.3	32.3	45.4	65.5	105.5	170.0
@	2,2 K <sub>1</sub>	TR4332 Fable In	5.6	2.2	2.0	1.7	1.5	1.2	6.
0	n Ft.		0- 2000	2000-10000	10000-20000	20000-30000	30000-1-0000	40000-50000	20000-60000

1463 Ft<sup>2</sup>;  $\overline{c}$  = 13.7 Ft;  $C_{Lor}$  = 4.95 per radian (wing alone) = 5.70 per radian (airplane); isotropic turbulence Data Assumed:

TABLE A-2. RE-EVALUATION OF PARAMETER b2 BASED ON TN 4332 DATA

@	g Q	<b>©</b>	10.79	11.27	12.17	13.22	13.13	13.50	14.02
0	R	ÓЪ	1.80	1.88	2.03	2.21	2,42	2.72	3.10
0	<b>√</b> ₽.		1.015	1.094	1.261	154.1	1.797	2.278	2.893
Θ	* <b>4</b> %	9	५० ट	1.97	1.85	1.70	1.55	1.37	1.23
9	К	Function or or Fig. 5-2	.352	.373	.415	691.	.533	,614	<del>1</del> 69.
<u> </u>	K 8	Function of 3 TWH332 Table Ib	.718	.736	.768	. 798	488.	048.	.856
<b>④</b>	ja.	() ()	20.8	24.3	32.3	45.2	65.6	105.2	170.0
0	Pratt µg	TW4332 Table Ib	0°48	27.9	37.1	52.0	15.4	121.0	195.4
@	5.3 Kz	TH4332 Table Id	5.3	5.3	5.3	5.3	8.4	7.7	0.4
Θ	n Te		0- 2000	2000-10000	10000-20000	20000-30000	30000-10000	40000-50000	50000-60000

W = 30000 Lb.; S = 662.4 Ft<sup>2</sup>;  $\overline{c} = 10.5$  Ft.;  $C_{LR} = 4.83$  per radian (wing alone) and (1.15) (4.83) = 5.55 per radian (airplane); isotropic turbulence spectrum, I = 2500 Ft. Data Assumed:

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## APPENDIX B

## NUMERICAL RESULTS

 $\overline{A}$  and  $N_0$  values obtained from the vertical gust dynamic analysis of the Model 188 and Model 749, together with the associated one-g level flight loads, are listed in Table B-1 through B-4. Results for both the mission analysis and design envelope cases are shown.

Units in the tables are as follows:

Acceleration

g's

Shears, tail loads

pounds

Bending and torsion moments

inch pounds

Shear flows

pounds per inch

No

cycles per second

All  $\overline{A}$  values are in the units indicated above, per fps true gust velocity.

Sign conventions are as follows:

Wing shear and bending moment, positive up

Wing torsion, positive leading edge up

Wing shear flows, positive clockwise

Fuselage shear, positive up (relative to a fixed midbody)

Fuselage bending moment, forebody positive up and aftbody positive down (relative to a fixed midbody)

Tail load, positive up

Torsions and bending moments are with respect to the elastic axis in all cases.

It should be remarked that the A and especially the No values listed in Tables B-1 through B-4 for tail and aftbody loads are somewhat higher than would actually be realistic, as a result of the way in which the elevator float was treated. This motion was introduced, as noted in Section 8.1.1, in such a way as to permit an elevator flapping dynamic

mode. Inasmuch as the damping that would actually be provided by the control system was not included in the analysis, large elevator motions at about 6 cps resulted. By examination of the various load power-spectral densities for the Model 188 tail and aftbody, it was seen that, for example, a more realistic value of No would be about 1.5 cps in all cases and that A should be reduced from the value shown by about 4% for tail load, by 7% for shear and bending moment at F.S. 1000, and, for bending moment at F.S. 695 where the A value is already relatively very small because of the offsetting effect of inertia and air loads, by 25%.

 $\overline{A}$  and  $N_O$  values obtained from the lateral gust dynamic analysis are summarized in Tables B- $\bar{9}$  through B-8.

Units are identical to those of Figures B-1 through B-4.

As only  $\overline{\mathbf{A}}$  and  $\mathbf{N}_{\mathbf{O}}$  values are listed, all signs are inherently positive.

 $\overline{A}$  and  $N_O$  values obtained in connection with the Model 188 vertical gust parameter variation study (Section 14) are presented in Table B-9. Units, sign conventions, and other particulars are the same as in Tables B-1 through B-4.

TABLE B-1. RESULTS OF VERTICAL GUST DYNAMIC ANALYSIS, MODEL 188 MISSION ANALYSIS SEGMENTS (a) C.G. ACCELERATIONS AND WING SHEARS, CASES 201-209

\*

		F	8	3	4	5		1 1	သ	6	or
Case		0.0				Wing	g Shears	, S			1
		Accel	WB 83	WS 119	19t sm	WB 209	NS 275	%E 34€	WS 380	MS 148	WS 516
rc2	l≪'8	.01599	187.1	188.1	172. k	207.7	182.5	142.1 R13	126.7	74.79	31.15
	ğ	1.0		14241	1097	13663	10598	6787	9257	5385	2087
202	A No 1g Load	.02192 1.124 1.0	268.4 1.567 19055	263.4 1.681 16386	236.3 1.902 11862	289.8 1.606 13979	252.9 1.644 9889	194.6 1.837 5300	171.3 1.214 7679	100.8 1.365 4161	42.24 1.688 1531
203	A No 1g Load	.01913 1.100 1.0	229.8 1.597 17770	228.9 1.711 15597	208.3 1.920 11623	252.7 1.658 13973	222.2 1.672 10334	172.4 1.829 6057	151.2 1.204 8461	89.14 1.361 4756	37.35 1.711 1798
20t	A No 1g Lond	.01897 1.113 1.0	228.8 1.648 18607	233.6 1.746 16338	218.0 1.918 12156	259.1 1.715 14050	229.7 1.692 10117	180.3 1.794 5826	156.1 1.254 8222	92.60 1.420 45TT	38.22 1.809 1700
205	No 18 Lose.	.01836 1.100 1.0	217.3 1.6/1 17279	224.2 1.753 15498	211.0 1.912 11853	250.4 1.730 14020	222.1 7.696 10493	174.7 2.776 6518	152.9 1.260 8966	91.14 1.417 5157	38.17 1.815 1963
236	A No 1g Load	.02047 1.102 1.0	248.3 1.529 18277	241,2 1,649 15819	213.9 1.884 11586	264.2 1.581 13997	229,1 1,639 10160	175.5 1.852 5672	155.6 1.175 8064	91.23 1.324 4466	38.15 1.643 1675
207	A No 18 Lond	.02299 1.145 1.0	282.5 1.572 19541	276.2 1.684 16653	247,2 1,906 11906	303. B 1.596 13927	265.0 1.6 <sup>42</sup> 96 <sup>47</sup>	203.8 1.648 1907	178.0 1.228 7275	104.7 1.367 3880	43.97 1.668 1406
80%	No 1g Load	.01980 1.092 1.0	236.1 1.597 17853	238.3 1.700 15784	219.3 1.836 11873	264.2 1.669 14060	232.7 1.657 10411	181.2 1.778 6226	160.6 1.230 8615	95.04 1.396 4870	39.74 1.776 4263
503	Ko 1g Load	.02205 1.138 1.0	265.1 1.655 18961	268.8 1.750 16481	248.8 1.926 12079	299.3 1.6.8 13897	264.4 1.663 9830	206.0 1.769 5416	181.6 1.271 7795	107.8 1.430 1839	45.22 1.786 1562

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	or		8 NB 51.6	10% 1.6% 06 .078-106	2,436 21.688 06 .05384106	1270 1.711 30 1.711	1320 1.809 06 .05984106	1298 1.815 56 .0707×106	1297 1.643 36 .0994136	1165 3.668 3.04841.06	1331 05 1.776 06564306	1538 6 1756 6 .05441106
201-209	SZ.		844 SA	1,444 1,444 303x10	83.13. 83.13.	5366 1.515 255410	2783 1.59	2.5% 1.5% 1.5% 1.5%	2 1 4 5 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	58.1. 19.1.50 1.1.50	3889 1. 564 259×10	6734 1.586 .215210
	7.7		NS 380	1.285 1.285 7914106	. 35.00 82.1.35 80.00 90.00 90.00	1.358 1.358 6012069	14230 1.422 .6982106	13980 1.423 .T462106	14070 1.317 6462106	16150 1.360 1.360 59610	1.395 1.395 70410	16570 1. 127 6112106
TUED CASES	97	ents, K	94E 8K	15660 1.233 1.074x106	22.50 1.299 1.299 1.200	18760 1.299 937×106	19450 1. 447 . E932106	19070 1.349 1.013x106	19220 1.267 1972106	22110 1.305 1.757.	19950 1.321 .957×10 <sup>6</sup>	22640 1.352 .828x106
CONTINUED KENTS, CAS		Ving Bending Howent	NS 275	26290 1.899 1.671210 <sup>6</sup>	36140 1.339 1.3188106	11.342 1.4912106	32940 1.344 1.4242106	32100 1.332 1.5882106	38640 1.334 1.4092106	37760 1.352 1.234219	33610 1.315 1.517×10 <sup>6</sup>	36260 1.333 1.334x106
Ş.	47	Wing Der	6C# SR	38860 1.364 2.4582106	53720 1.388 2.080210 <sup>6</sup>	17.30 1.396 2.2712106	1.390 2.195x106	17.370 2.374×206	1.386 1.386 2.154x106	56200 1, 400 1, 986x106	1, 356 2, 301×106	\$6450 1.373 2.089x106
TABLE B-1	13		19T SM	2,976×106	64,990 1.417 2.609110 <sup>6</sup>	36650 1.4.11 2.8002106	2.733×106	\$6780 1.417 2.912×106	58500 1.415 2.711.106	67600 1. 426 2. 512×10 <sup>6</sup>	39600 1.395 2.8332106	67730 1.406 2.621×106
TA. WING BE	ส		VB 119	551.70 1,44.7 3.60km106	76390 1.414 3.2984106	66970 1.464 3.537×10	69160 1.465 3.435210 <sup>6</sup>	67040 1.456 3.589×106	69250 1.442 3.3812106	75960 1.450 3.208210	70390 1.432 3.519×10	79950 1.439 3.3212106
(b) WI	ជ		W8 B3	61890 1,455 4,1442176	85910 1.447 3.9234106	75170 1.469 4.1292106	77440 1. 475 4. 0534106	74940 1.468 4.173×106	78010 1.443 3.984x106	89960 1.452 3.845x10	78880 1. 140 4. 1162106	99500 1.449 3.822x106
				14 °0. 24	14 °5 °5 ≥1 Anot a	14 0 M	N No. 3	K 57 3	K <sup>6</sup> 2 202 203	14 °5 ≥1	14 °5 ₹	14 0 % A
		Case		<b>108</b>	333	8	2	8	8	504	808	209

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TABLE B-1. CONTINUED
(c) WING TORSIONS AND WING SHEAR FLOWS, CASES 201-209

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-		WB 83	7 143 No 2.5 18 Load 498	7 18930 No 2.624 1g Iosd -1.519x1	7 17110 % 2.617 1g Loed -1.175x	18010 No 0.1495 1g foed -1.40tx	7 17240 No 2.497 1g Lond -1.041x	7 17290 No 2.626 1g Load -1.394x	7 15710 Fo 2,548 1g Load -1.5/772	7 178 1, 2,4 1, 1044 -1,18	7 19630 % 2.627 1g Load -1.5%Cx*
20 22		83 WB 119	60 13590 115 2.595 1206537120	.06 -1.480zu	16240 7.692 106 -1.155x1	10 2774.0 95 5.53 12106 -1.365210	16290 2.564 106 -1.028cc	16370 2.708 106 -1.26341	18650 2.727 06 -1.499x1	2,438 2,953 1,130x10 <sup>5</sup> -1,159x10	18520 2.660 71.197x1
25		WB 167	127%; 2.630 587×106	16850 2.797 of -1.429×106	15320 2.780 -1.1252106	15950 2.657 6 -1.318x15	15230 2.660 -1.011×10	15460 C. 199 5-11-239210 <sup>6</sup>	17540 2.822 -1.473x10 <sup>¢</sup>	ر مو -1.1، مح	1712.) 2.787 36 -1.441x106
23	Ming	WB 209	12500 2,129 -,233x10 <sup>6</sup>	16730 2.092 908x106	14980 2.127 669x10 <sup>6</sup>	15630 2.067 845x106	15010 2.060 600x106	15270 2,131 7482106	17%60 2.097 938x100	13580 2.053 691x106	17012 2.094 933x106
24	Wing Torstons, H.	WS 275	11340 2, 318 271×106	15180 2.291 Refailof	13620 2.311 624x106	14160 2.257 769×10 <sup>6</sup>	13560 2.257 564106	13890 2.3.3 690:406	15450 2.269 884:10 <sup>6</sup>	2,255 2,255 2,639×10 <sup>6</sup>	15380 2,300 7634106
25	ATA	WB 346	10550 2,467 293x10 <sup>5</sup>	14070 2.456 732×10 <sup>6</sup>	12660 2.463 5674305	17,080 2,422 .683x10 <sup>6</sup>	12500 2.489 517x10 <sup>6</sup>	12950 2.477 608x106	2.455 794x10 <sup>6</sup>	2.432 2.432 578x10 <sup>6</sup>	14180 2.485 844x105
88		WB 380	2393 1.075 052×106	317? 1,354 .,2702106	25.8 1.250 20.x106	2330 3.230 260106	2965 1.201 186×106	290E 1.288 204x106	3293 1.417 286x106	2998 1.205 214x106	3368 1.352 284
27		भड़ स्पर्	1171 1.092 05321.06	1560 1.390 1.390	1384 1.308 1.14×106	1,26 1,247 -,180±106	1404 1.208 136x106	1424 1.324 0902x10 <sup>6</sup>	1620 1.456 206x106	1,221 1,221 1,52x10 <sup>6</sup>	1653 1.369 195x106
9₹		915 SK	4,9,8 1,276 -,337±10	546.5 1.591 101×106	485.2 1.510 0315x10 <sup>6</sup>	498.9 1.44.3 0996x1.06	1,400.8 1,400 -,078x106	1,521 1,521 0915x10 <sup>6</sup>	567.7 1.660 -,114×106	513.3 1.408 0769210 <sup>6</sup>	5787 1.561 105×106
82		WZ 83 Front Beam	4.590 1.820 152.39	<b>6.376</b> 1.915 61.79	5.551 1.913 85.52	5.66T 1.843 68.06	5.367 1.828 95.23	5.880 1.902 80.25	6.691 1.945 76.33	5.745 1.802 86.33	6.349 3.424 1
30	Wing She	ng 83 Rear Beam	1.438 4.063 -305.1	3.117 3.716 -537.51	1.836 3.952 -452.93	1.681 4.559 -507.44	1,299 4,122 4,122	2.023 3.453 -485.0	2.272 3.646 -546.15	1.733 4.367 -456.03	2.015 4.426 -538.72
31	Wing Shear Flows	WS 346 Front Beam	7.508 2.252 20.08	10.10 2.205 -177.1-	9.033 2.246 -97.98	9.430	9.058 2.197 -59.43	9.209 2.281 -121.75	10.56 2.249 -209.46	9.374 2.:15 ->6.41	10.38 2.230 -218.36
ĸ		VS 346 Rear Beam	1.917 3.066 -246.80	2.542 3.127 -388.67	2,322 3,135 -338,62	2.235 3.220 -379.76	2.137 3.252 -327.86	2.392 3.053 -347.18	2.632 3.176 -405.13	2.247 3.129 -346.47	2.593 3.149 -434.67

				TA	TABLE B-1.	1-1.	CONCTADED	UDED				
=	(d) FU	SELA	FUSELAGE LOADS AND HORIZONTAL	ADS A	CH QN	RIZON	TAL T	AIL L	OVO.	CASE	TAIL LOAD, CASES 201-209	2
		33	A	ž	Ж	37	æ	2.	<b>2</b>	7	1,2	6.3
9						- Puselag	e Londs -					Maria
		•	ž	•	ۍر د	Ęg.	Ż.	8	Ý	u e	ý	73
		P. 8. 350	F.S. 350	7.8. 500	7.8. 500	F.S. 571	7.8. 572	7.4. 695	F.S. 693	7.8, 30.06	7.8. 1006	
ğ	14.03 at	1,000 1,000	23,00 1,483 -1,4732106	1.88.5 2.86.5 2.89.4	47190 1 399 -3.2378106	868.7 1,811 -1781	64990 1.350 1.10001.4	135.8	15140 4,607 5.108410 <sup>6</sup>	93.33 87.68 4.769	2.0T7 2.0T7 1.0T84106	19.50 06.70 06.70
ğ	K 3 2	167.3 1.67.3 20.65	29610 1.787 -1.6012106	2.1.28 2.1.19 2.19.19 2.19.19 2.19.19	A.T.S. J. Susano	7.4.5 7.4.5	3.993 -1.7764106	6 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	2. 3. 378 7. 3080.06	2 4 4 2 4 4	2.737 2.737 1.9672306	S. S
8	K 2 2	1.60.6 9.60.6	25067 1.733 -1.5492106	20 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	99630 3.617 -3.4082106	9 9 1 1 1 1 1 1	7525. 1.519 -4.6174106	171.6 1.938 -80819	17360 2,136 6. kykalo <sup>6</sup>	27.55 107.65	25690 2.337 3.635436	2.30 8.30 6636
\$	No Est	118	24800 1.698 -1.5714106	861.1 1.336 1988	52230 2.568 -3.4542106	1, 150 1,	15570 1,583 -4,6864106	.643 2.643 -21093	17900 1,963 7,0692106	2.6.00 2.6.00 2.6.00	2,250 2,229 1,8874106	2.00.4 9.00.9
Š	K 2 3		24090 1.688 -1.499x106	32.1 1.83 1.13	3.20 miles	1.05.7	71180 1.507 -1. herrios	1,686 1,985	17400 4, 837 6, 1842106	66.13 2.800 1001	#6060 2.156 1. beauco	160.00 1.970 9970
ğ	K 23	17. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	27700 1.706 -1.9604106	28.9 1.411 1999	60330 1.293 -3.4692106	135	32.327 3.327 -4.7108106	1. 423 1. 423 2. 423	18800 5.878 6.6934106	25.5 25.5 25.5 25.5 25.5 25.5 25.5 25.5	2, 3cr 2, 3cr 1,680x106	263.54 2.30 -7272
ğ	K 2 3	193.0 1.744 -9704	300% 1.872 -1.597×106	1,917 1,917 1,504	66mo 1.737 -3.354a106	363.6 1.424 1.9413	91600 1.657 -4.5372106	228.7 1.407 19865	2.056 5.054 6.396a106	53. tr 1090	27310 2.948 1.6852106	160.0 8.1 -5724
8	K 0 34	1.9% 1.9% 1.0% 1.0%	26380 1.633 -1.6372106	15.35.0 1655.0	3. 3964106	1.4.5. 1.4.5.	80050 1, 470 -4, 879×106	11.1.1 1.96k 225.39	18040 7.885 7.8864106	68.00 3.834 3.348 5.348	27060 2.30e 2.1712106	165.cc 8.117 -9779
\$	No 16 Load	185.2 1.728 -10080	28850 1.896 -1.'.89x106	303.5 1.900 -16411	64080 3.783 -3.483m?	367. h 1. kor 19061.	67840 1.641 -4.7784136	208.1 1.965 -27877	2.473 7.509110 <sup>6</sup>	58.60 -1,935	2.606 2.606 2.006 2.006	174.06 2.189 -9204

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TABLE B-2. RESULTS OF VERTICAL GUST DYNAMIC ANALYSIS, MODEL 198 DESIGN ENVELOPE CASES

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ن ن	ACCELERATIONS	LER	ATK	SZC	AND		WING	SHEARS	ARS,	S	CASES	401-4]
		7	8	3	4	3	9	7	8	6	01	
Cane		6.0				Man	Wing Shears, S.	, C.			1	
		Acce1	W883	M8119	WRIGH	WIGGOS	VIS275	ng.	MB380	8448%	<b>9158</b> M	
1 5	L	A Bridge	188			2. W. 7	8.05	14.0	167.8	8		
	12 No.		2.03 5.03 5.03	2,140	<b>3</b> 9	1.65 8.65 8.65 8.65 8.65 8.65 8.65 8.65 8	1.836	2,405	1,10	88	1.738	
<u> </u>	<u> </u>		221.9		157.6 2.603	264.2 1.603	216.5 1.829	154.9	167.6	84 84		
52	7		15505		7559 166.1	95.05 25.05	*337 23.6	191.6	27.79	1041	202 54.18	
-	. 23 22 2	100.1	2.017 14477		2.054	1.806 9128	1.023	3.868 3.73	3531	1.358 1672	25. 25.	
₫.	14 153 1	.02526 1.056 1.0	163.8 2.088 12720	171.0 2.021 10643	5.15.9 6.00 6.00	242.1 1.746 7885	216.9 1.80.9	1.52 1.82 1.82 1.83 1.83 1.83 1.83 1.83 1.83 1.83 1.83	178.9 1.483 2957	118.6 1.843 1333	52.89 2.243 405	
<b>6</b>	¥ 29	.0000 1.109	323.9 1.450 81310	346.5 1.502 18533	1.60°E	366.1 1.496.1 13956	344.6 1.534 8284	268.1 1.601 3314	2.36.3 1.399 5757	150.8 1.725 2987	68.25 2.109 1079	
, <del>,</del>	K 200	.08362 1.030	11.62 19706	17038 17038	184 212	374.7 2.441 12816	330.4 1.506 1783	266.5 2665 2665	1.25. 1.25. 1.25.	1.69.5 2676 2676	67.41 1.997 95.1	
104	14 80 16 84	.08663 1.212 1.0	177.4 1.425 86322	465.6 1.300 21760	1.664 1.664 15273	11.381 16594	377.0 1.519 10380	288.0 1.842 1191	226.4 1.194 6308	133.7 11.258 31.26	26.53 1.462 1052	
90,	16 100 M		139.6 1.346	1.1.34 20107	13.65.8 13.65.8 13.65.8	433.8 1.328 15338	360.7 1.485 9386	270.4 1.862 3477	228.6 1.107 5728	134.9 1.17 271	3.3 2.3 2.3 3.3 3.3	
§	1< 2	.06572	474.6	1,56.6	11.5	11.5 461.8 390.4 302.2 237.3 140.0 59.14	39C. 4	302.2	237.3	1,273	39.14	

250.0 1.167 7218

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	(C) C.G. ACCELERATIONS AND WING SHEARS, CASES 413-	
	SES	30
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e E	ONS	·
TABLE B-2. CONTINUED	LATI	Ŀ
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3		9				ž	Seers,	22			
		Accel	¥1803	6TIDA	<b>WEL67</b>	¥8209	MARTS	946 94	08 <b>€ 2</b> 80	APPRA	<b>31684</b>
E C	~ 2 <sup>2</sup>	.08431 1.153 1.0	425.9 1.473 24941	433.7 1.538 21649	1.09.7 1.643 16133	149.9 1.948 16793	397.3 1.588 11399	312.5 1.58° 6116	249.8 1.295 8206	1.430	62.69 1.743 1369
* * * * * * * * * * * * * * * * * * *	7 20 7 20 7 20 7 20 7 20 7 20 7 20 7 20	.08489 1.067	11.10T 23.051	11.185 20102	8.12 5.35 5.45	1,15 1,55 1,55 1,55 1,55 1,55 1,55 1,55	38.1 1.50 10460	239.1 1.564 5486	256.0 1.206 7643	158.8 1.336 1.056	6. 1 1.650 14.92
\$7.7	. 50 20 20 20 20 20	.02361 1.141 1.0	210.0 2.485 2445	428.6 1. ° 31 21573	115.3 1.600 16420	1575 1.575 16857	399.9 1.535 11,535	1.36. 68 H	253.3 1.355 0.655	132.4 1.491 4726	6. 3 17. 1
416	7 30 10 4	.06424 1.055	397.4 1.463 29912	413.2 20072	396.7 1.565 151ch	11.548 11.548 15706	388.1 1.513 10422	324.7 1.349 3582	259.8 1.265 7937	157.1 1.391 4414	2.5.5. 1.6.5.5.
F2.4	7. 20. 20. 20. 20. 20. 20. 20. 20. 20. 20	1.00387	207.8 24.073	1.98.4 1.917 21296	1,366 1,366 16367	1.575 1.575 16717	103.4 11.531	320.3 1.555 6016	255.0 1.374 800	154.1 1.509 1765	65.06 1.684 1888
418	4 20 A	00.11	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	19861	1,527 1,527 15090	1.5.7 1.5.6 155.79	391.9 1.510 1ct27	306.6 1.340 5367	261.1 11.245 777	159.0 1.404 1.54	67.24 1.570 1701
<b>61</b> %	, 29 29 7	.08061 1.134 1.0	2.4.8 2.4.8 2.4.8 2.4.8 2.4.8 3.6.8 3.6.8	337.4 1.499 20735	296.2 1.688 15288	336.8 1.40 1735	27.6 1.561 11960	215.1 1.912 6157	170.9 1.158 8252	100.5 1.840 1.824	12.50 1.475 1605
8	E 25 24	1.06 1.06 1.0	113.5 1.409 25353	365.8 1.497 21239	1535.8 15350	1.386.1 1.388	1.535 1.535 1.744	246.7 1.877	195.8 1.172 7380	112.5 11.246 3895	1.660 1.660 1399
421	1. 23. 2. 20. 24. 24. 24. 24. 24. 24. 24. 24. 24. 24	1.08539 1.024	2.1.1.2 26.1.2 26.36 26.06	1.511 2.738	35.5 1.697 15333	105.3 16648 16648	336.0 1.636 10426	253.6 2.045 4216	212.4 1.208 6381	125.4 1.272 3133	52.90 1.442 1055
8	, 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20	.02550 1.284	1. 1.09	1.1.66	2003 2003 2003	1.446 1.446 16797	33.3 1.630 10585	242.1 2.048 4363	210.5 1.196 6453	124.1 1.266 3221	52.23 1.442 1093
ş	7 2 2 3	1.0	4.659 4.659	25.5 1.71 12160	2.127 3555	¥:52 7.32 7.32	373.5 1.629 -3745	45.00	238.2 1.168 -5964	1.5%.9	6.38 1.720 -242
ţ	1s road	1,400	1.531 17070	265.0 1.741 10648	233.8 2.230 2225	1.500 1.500 2299	1.07 663.0	241.1 2.159 -9915	1,108	1.6.9 1.481 -5334	61.71 1.685 -2577

(c) C.G. ACCELERATIONS AND WING SHEARS, CASES 425-427

		1	લ	٣	7	5	9	.,	8	6	oτ
Case		0.0				Wing -	Shears,	2,0			1
		Accel	V:583	6118W	1.9T8M	48209	WS275	วาธิสก	WE380	श्चिमध्य	9153H
\$37	14 301 103 104	.03849 1.257 1.0	754.0 1.065 29011	715.2 1.312 20612	640.3 1.426 11264	761.3 1.288 20302	659.8 1.357 1733	506.7 1.560 -5244	390.0 1.219 -271'	230.7 1.252 -3075	97.36 1.353 -1654
924	2. 50. 50. 50. 50.	.04007 1.280 1.0	736.5 1.303 26312	695.5 1.367 19213	C17.6 1.510 24.5	720.7 1.285 9051	613.7 1.393 732	466.8 1.688 -5970	381.2	226.0 1.227 -3426	95.48 1.357 -1798
1.5.1	24 26 24 24 26 24 24 26 24 24 26 24 24 24 24 24 24 24 24 24 24 24 24 24	.01284 1.052 1.0	213.6 1.351 21120	195.8 1.180 18292	167.3 1.722 130.4	193.6 1.415 16903	160.3 1.607 12517	122.9 1.982 7344	97.27 1.037 9555	56.82 1.146 5547	23.79 1.428 2163
3	¥ % % % % % % % % % % % % % % % % % % %	1.028	215.9 1. Kil	137.9 1.436 18270	168.7 1.663 17017	192.0 1.397 16899	161.1 1.587 12519	123.0 1.962 10075	26.2 2.033 9555	57.47 2.142 5549	2.4.1. 2.4.1. 2.4.5.3
8	7 % % % % % % % % % % % % % % % % % % %		176.9 1.487 18618	183.8 1.559 17560	177.9	192.4 1.668 1.668 16619	168.1 1.682 1.744	13.9 1.726 11.53	106.5 11.265 11234	64.23 11.23 6995	27.03 1.147 2869
Q.	₹ 32 38ad	.0339 1.085	13.490 19890	229.7 1.552 16037	222.3 1.633 18059	1.645 1.645 16677	210.4 1.627 12588	166.6 1.68 1.242	134.7 1.295 10917	81.65 1.398 6745	34.40 1.593 2747
TF.	N No Load	.0317 1.043	215.6 1.570 19905	223.1 1.582 18396	219.4 1.660 1.660 18745	236.8 1.659 17100	208.1 1.642 12917	165.4 1.691 11472	12.5 2.3 2.3 2.3 3.3 3.3 3.3 3.3 3.3 3.3 3.3	79.87 2.406 6851	33.71 1.597 2790

		(A)	WING B	BENDIN	BENDING MOMENTS	MENTS, CAS	CASES	40 i-412	12	
		1 1	क्र	13	77	2.5	16	17	18	88
3					Ving senil	ring Moments,	- ×			
		V803	6718A	16167	W\$209	V8275	<b>WRJ</b> <sup>4</sup> 46	<b>9838</b> 0	1184 kB	915BA
<b>19</b> 7	7. 7. 7. 7. 7. 7. 7. 7. 7. 7. 7. 7. 7. 7	76570 1.616 2.175#106	68540 1.623 1.653#106	59470 1.621 1.1612106	50210 1.624 .819#136	33720 1,59% 350#10 <sup>6</sup>	20530 1.471 20091	15260 1.501 1702106	6198 7.608 .ue66a106	1.738
8	76 55 50 74 50 84	72160 1.590 1.640m1\5	64740 1,599 1,3814306	\$6370 1.388 .9434106	1.131 1.131 .6.9x10	32400 1.545 .2414106	2.414 2.414 3.5994106	1523i 1.439 .1282106	6177 1,552 09738106	1410 1.709 1.005 1.005
ÇQ.	20 20 20 20 20 20 20 20 20 20 20 20 20 2	77720 1,504 2.1564106	71690 1.500 1.690a106	62310 1.1.42 1.1.58106	53610 1.490 .8351106	37950 1.521 .425#106	23790 1.739 .286#106	17810 1.691 .234106	7580 8.153 .06188106	2.375 2.375 .00394106
ಕ್ತ	N No.	73260 1.186 1.758x106	6/720 1.16 3.752116	9134106.	51070 1.495 62941.26	36300 1.480 392106	23220 1.650 .:14x106	1.7500 1.780 1.884106	7519 2.029 .0414x106	1798 2.243 .01862100
<b>20</b>	, 5, 4, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,	119800 1.328 3.7012106	107900 1.334 3.000x106	91600 1.335 2.207x106	76500 1.348 1.6358105	92778 1.361 1.340 .9421106	31220 1.548 .5778106	22860 1.466 4 128109	9757 1 900 1.1 100	2320 2.105 .0444x106
<b>9</b> 8	N No Lond	11,294 1,294 3,335x106	104200 1,300 2,090x136	88700 1,304 1,965#106	74210 1.312 1.4464156	51380 1.342 .8191106	30835 1.469 .5084106	1.517 365210¢	9689 1.800 122×106	298 1.997 .0395x106
*0.7	다 20년 10년 10년	132000 1.361 4.294x106	119900 1,371 3,456x106	95700 1.378 2.567#106	78260 1.384 1.9171106	51380 11.962 11.0602106	28673 1.252 .596x106	20610 1.259 .402106	8333 1.335 1352106	1982 1.442 .03382106
80	F 200 PM	127100 1.306 3.892x156	1.1400 1.319 3.0314106	92600 1, 323 2, 300#106	75960 1.325 1.7091106	30080 1.297 .905x10 <sup>6</sup>	28640 1.170 .5214106	1,176 384106	8447 1.255 1152106	1933 1, 367 .0885x106
<u>6</u>	اد دران دران م	137000 1.345 4.503#106	1.350 1.350 3.667106	99560 1.345 2.761x106	81450 1.345 2.100x106	53700 1,312 1,822106	30070 1.240 .698106	21590 1.270 5.14106	6776 1.357 .1638106	2011 1.472 .0411#106
1,10	7 1 € £ 53 2 7	132500 1.289 4.102x106	116900 1.295 3.3274106	96860 1.291 2.496a106	79430 1.283 1.9124106	38640 1.241 1.0878106	30820 1.153 .6234106	21900 1.189 1.6601.06	8892 1.872 1.84108	2333 1.391 .03582306
117	76 E	139600 1,350 1,650100	119930 1. 14.3 3. 8314.106	99880 1.330 2.914x106	2.2" M106	34820 1.283 1.350x106	30990 1.310 .790#106	25.11.300 301.77.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.	9068 1.510 1902106	2076 1.668 .048106
412	14 1.00 M	131800 1.298 1.266x105	1167/10 1.234 3.496#106	97620 1.272 1.633#106	8061: 1.246 2.039#10 <sup>2</sup>	54130 1.208 1.219#10 <sup>©</sup>	11.223 1.223 .TITELOG	22770 1.393 .527x106	9294 1.482 1.50 1.6	2115 1.583 . '12821'x

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		* (•)	T WING B	TABLE Bandin	B-2. G MON	TABLE B-2. CONTINUED BINDING MOMENTS, CAS	NUED CASES	8 413-424	<b>1</b> 24	
		ជ	118	13	2.6	15	16	17	18	ន
į					Ving Sending	ing Homente,	, ,			
		S <b>ga</b> 4	6TTM	19tes	WEOD	WRRTS	VB 346	ME 380	844 84	916 84
514	~ 2°	136.00	1.335 2.335 3.994106	10000 1.314 3.0094106	11.898 11.898 8. 38 82.06	55780 1.871 1.6302106	1 1 100 mg.	054.0 1.150 .647x10	931. 1.568 .218106	# 1.1. E. 1.1. O. 1.1.0.
\$	7 12 13	13900	11.200 11.200 2.396.106	2. 1. 20 2. 20 20 20 20 20 20 20 20 20 20 20 20 20 2	8.1.880 1.8870 1.8870	53850 1.197 1.898106	30040 1, 257 . 7801106	SASSING.	2.18. 2.18.	26.1.65 50.1.65 50.1.65 50.1.65
33	~ 23	1371.00 1.386 5.0578106	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	1.2000	8.537426 8.537426	5640 1.872 1.698106	3690 1.388 1.00k106	2330 101.10 101.00	9549 1.60e .2671.06	1.741 Organo
¥	, es	134100 1.879 4.698106	1,870 1,870 3,9136106	100000 1.244 3.0471106	8.34 M.106	\$6150 1.800 1. 1872106	930 1.536 93416.	States.	44.14. 64.14.	1.634 Grando
117	~ 25 2	13600 1:319 4.798106	24.18. 24.18. 26.18.	1030K 1.890 3.034176	2 Te 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	9690 1.869 1.4692106	32990 1.399 .913106	2356 1.186 6.1876	28.19. 10.19. 10.19.	1.666 1.666 0.054106
418	~ #3	153400 1.871. 4.3934106	1.863 3.650×106	101kon 1. fyr 2. 796-106	8.01.10 8.01.106	96740 1.199 1.3474106	33860 1.303 .0434106	1.365 1.365 .638106	9978 1.479 .8252106	11.570 1.570 1.970 1.970 1.970
614	~ 23 7	26960 1.398 1.7808106	3.967#1.06 3.967#1.06	71470 1.413 S.14411.6	26370 1.517 2.5362106	30830 1.394 1.4052108	21460 1.249 .89432106	15510 1.844 .654106	69a 1. ¥1 235206	24.1. 25.00 25.00
ş	- 25 27	113600 11.378 1.36810	9.1:35 7:35 7:45 8:35 8:35 8:35	Serio 1. 391 8. STERIOS	ente 1.396 8.398106	1.374 1.894106	1.247 1.247 .T396a106	1700 1.849 536106	7841 1.337 19021061	1560 11.460 11.460
ដ្ឋ	~ 23 2	1.500 1.500 5.000	2000 2000 2000 2000 2000 2000 2000 200	86370 1.148 2.376106	70940 1.437 1.9892106	1. 399 1. 0642106	26570 1.297 59632106	19360 1.272 Mario	15.3. 1.36.196	1796 11.44-3 19960
3	,, es	118300 11.188 1.360106	109600 1.534 3. See 106	9.4.1.4.6. 6.6.0.1.06.	69600 1.1486 1.9632106	1.95790 1.967 1.0978106	afero 1.246 .61572106	301.00 201.10 301.10 301.10	7768 10.11 20.11141.	F 35
ş	- 25 27	11.34 1.34 - 13.40	109600 1.539 -1.744106	9300 1,533 1,981,06	30730 1.496 -1.690:106	\$42.0 1.484 -1.6312106	32090 1.177 -1.101e106	1.350 1.350	. 3575 - 354106	1.70 1.70 1.00
\$	, g	1.584	1: 983 1: 983 1: 983	11.15T	13150 1.146 -1.87106	1, 141 1, 141 -1, 762106	30430 1.484 -1.178106	2. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	. 1. 28 2. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	1.665 1.665

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TABLE B-2. CONTINUED (f) WING BENDING MOMENTS, CASES 425-427

		-			4	ž	3,5	٤	٤	9,
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į					And Mark	ing Housen's,				
		WEBS	6TUM	19TEM	singer:	SLE SK	946 SM	98 SM	944 BN	975 VA
125	7 29 7 3	22300 1.263 1.4794106	199100 1.890, 1.890,	oolge:	137800 1.879 5364106	90600 1,867 36210	268-1 1.838 67866	25570 1.252 474410	11.898 1.898 988106	11.35 1.35 - 0678-10
Ž	× 200	213900 1.842 1.07/2106	1.949. 1.949.	1,2700	1.858 1.858 786810	89630 1, 887 -2, 017210	1,164 1,164 75/4106	1: 282 1: 282 - 35810	11.100 1.100 300106	1.35% 073810
, 27	2 2 2 3	36380 1424 4.8982106	1.439 1.439 1.198106	2.435 3.4034306	2930 1. ter 2. 7534106	21480 1.393 1.7942106	1.176 1.176 1.1162106	9778 1.151 1.151	3546	508.7 1.126 .0814126
<b>§</b>	~ %  	8.18. 883	Solution .	S. P. P. C.	S. Sept. 1	2000 2000 2000 2000 2000 2000 2000 200	1.173	. 1476 1.147 . 1470 . 1470	38.1.85. 7.85.28	88.5 80.5 80.5 80.5 80.5 80.5 80.5 80.5
3	H NA	5.85.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0	000000.4 000000.4	5. 00 10 10 10 10 10 10 10 10 10 10 10 10	3.11.24 2.11.24 3.11.24	2.17.300 2.17.300	13470 1. 1273 1. 1273	9804 1.300 1.0950206	2 3 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	116.00 20.00 20.00 20.00
8	2 2 2 2 3	2	1.335 1.375	82.15 83.35	3. cristos	20490 1.893 2.118106	17090 1.330 1.573420	1.390 1.390 1.0090106	H. J.	Series.
ti d	,	3. 17. 12. 18. 18. 18. 18. 18. 18. 18. 18. 18. 18	63370 2. 709820 60. 709820	8.3.5 8.3.5	1.336 2.348 3.3482.06	2.13%106	1.386106	1.09 delo	201-93 101-93	34.1. 28.1. 20.21.

	ONS AND WING SHEAR FLOWS, CASES 401-412
TABLE B-2. CONTINUED	SHEAR FLOWS,
BLE B-2.	AND WING
TA	(g) WING TORSIONS AND WING SHEAR FLOWS, CASES 401-412
	(8)

A COLUMN

b commercial

_	50	Case	K683W	1,31 7 A 15240 1,0 3,864 1,2 Lond -2.535x106	13940 No 13940 No 13940 No 18	14 Load -1.9613106	1.04 A 2.0830 1.0 2.663 1.0 1.094 -f. 0.14106	105 A 29190 Ro 2,134 16 Lond -1,615#106	14 14 14 11 7011106	107 X 28490 10 2,460 10 1084 -2.053130	14 1084 -2.1468106	16 100 -1.9578106	120 X 27300 2.000 12 1000 -2.000106	111 N 27130 N 27175 14 Load -1.85 M10 <sup>6</sup>	112 X 27930
NIM (8)	เล		W8119	14/P0 3,912 5,47)#106	13830 h. 025 -2.506#105	2128c. 2.66k -1.885x106	19000 2.779 -1.969106	2.197 2.197 -1.557x106	25080 7.250 -1.630#106	2.546 2.946 -1.993#106	24120 2.728 -2.07/1106	2.339 -1.596x106	25700 2.493 -1.973x106	29050 2.168 -1.792x1(%	2,38
ING TORSIONS	32		W8167	14600 3.868 -2.138x106	14270 3.821 -2.374x106	19970 2.844 -1.785#106	16.70 2.033 -1.863x106	24,360 2,428 -1,485x106	28320 2.412 -1.5608106	25230 2.658 -1.903x106	22630 2.344 -1.980x106	26680 2.439 -1.8108106	23960 2.504 -1.880106	2.255 2.255 -1. 712x106	2, 104 2, 104 2, 104
	23		6028#	14570 2.564 -1.584x106	13070 2.556 -1.622x106	18370 2.094 -1.254x106	16960 2.116 -1.303x105	22470 1.845 -1.069x106	21300 1.352 -1.319x106	2.016 2.016 -1.3234106	2.07% 2.07% -1.372x106	25380 1.909 -1.262x106	23450 1.758 -1.311#104	25390 1.806 -1.201x106	1.849
AND W	76	Wing Torsions, MygA	SLC:3N	13240 2.833 -1.476x106	11980 2.918 -1.437#106	15560 2.420 -1.118106	14140 2:195 -1,160x106	19350 2,097 -,962x106	18100 2.143* -1.017x106	22180 2.194 -1.184x106	20320 2.277 -1.225x105	23070 2.078 -1,130x106	21220 8.154 -1.172x106	23120 1.972 -1.377106	2.045
WING SHEAR	92	- VAYN 'cuc	WE346	12520 3,003 1,214124	11570 3.059 -1.2394106	13190 2,797 -,96/x106	11850 2.931 -1.001x106	16630 2.384 833x106	15370 2.475 870x106	20510 2.357 -1.028106	18840 2,453 -1,064x10 <sup>6</sup>	21180 2.239 981x106	19490 2.333 -1.016x106	21030 2.142 935x106	2,239
	9/2		Wr.380	3316 1,881 -,481x106	5339 1.836 -,5384136	4523 3.57h 375x106	1,47) 1,47) -,384x106	4907 1.451 3654106	5100 1.356 349x106	1,588 1,588 -,394x1c6	4141 1.515 403x106	1,493 1,493 -,382x106	4319 1.419 391x106	4321 1.371 371x106	11.2%
FLOWS,	2.6		MB448	163" 1,960 -,286x10	1647 1.912 289x199	2318 1.632 250x106	7386 1.5%0 254x136	2500 1.516 2334106	2612 1,421 237x106	1997 1,655 -,8684106	2047 1.579 259x106	2073 1.547 2564106	2135 1,464 2601106	2111 1,415 250x106	1.3%
CASES	8.2		NC516	579.0 2.238 145x10.5	586.7 2.185 146x106	847.0 1.678 132x106	874.5 1.590 133x106	909.0 1.588 136410£	952.1 1.494 128#106	698.2 1.909 137x100	119.2 1.825 138x106	722.1 1.763 13.4106	787.40 1.671 1361106	740.0	169.9
5 401-412	39		WSB3 Front Deam	5.124 3.096 -104.7	3.211	2.585 2.585	2.715 2.715 -106.5	8,492 1,758 100,7	6.011 1.763 61.3	11.24 1.840 121.8	10.41 1.832 78.8	11.40	10.59 1.707 81.3	10,80 1.616 125.4	10.06
12	30	Wing She	habs Reor Beam	2.640 3.014 -695	2.857 2.851 -684.2	2.973 3.004 -556.7	2.769 3.059 -543.4	2.611 3.554 -599.8	2.537 3.533 -590.1	3.561 2.367 -755.7	3.864 2.208 -7h4.1	3.129 2.849 -727.1	3.4.7 2.65) -715	2.521 4.080 -698.7	3.839
	æ	Sheur Flows	WE346 Front Bean	8.715 2.796 2.744.2	7.903 2.900 -1.97.1	6.826 2.144 -379.3	7.919 2.66% -409.5	12,55 1,999 -261,9	11.64 2.053 -292	14.36 2.151 -312	13.75 2.730 -343.2	15.58 2.044 -272.7	14.38 2.113 -303.2	15.66 1.957 -240.6	24.54
	æ		WS346 Henr Bea	2.753 3.795 -475.8	2.862 3.584 -1.72.9	3.03 3.03 3.73	3.7.8 3.043 • 577.3	3.050	3.928 3.070 -386. (	3.235	3.308	3.163 3.298 -48, -6	3.2%	2.925 3.183 480.9	3.005

	CASES 413-424
CONTINUED	SHEAR FLOWS
TABLE B-2. C	(b) WING TORSIONS AND WING SHEAR FLOWS. CASES 413-424
	3

		8	21	83	23	5¢	25	%	27	28	&	Se Se	ĸ	æ
8					Win	Ving Toretons, M	14 X					Wing Sheer	Ş	
		WBB3	6TEM	MELLET	W8209	VB275	94684	*8380	87752	MESIG	WS 83 Front Bean	NS 83	MS 346 t	2 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -
614	% 50 4	31210 2.013 -1.711106	29470 2.051 -1.712x136	27250 8.129 -1.696106	25800 1.743 -1.154x106	23210 1.919 -1.036106	2.0980 2.096 8994x106	1,319 1,319 2,3612106	2181 1,321 2462106	755.8 1.481 132106	10,61	2.198 4.856 -665.4	15.81	89.25
454	. × × × × × × × × × × × × × × × × × × ×	20560 2.120 -1.867106	2.169 2.169 -1.8982106	2.650 2.23 -1.721214	24130 1.782 -1.209106	7	<u> </u>	1.234 3.234 3.370x106	2268 1.230 250£106	789.7 1.380	9.4.40 4.694.4.	2.375 1.586 -665.8	14. 1.X.	3.292
£3	# 25 25 26 26 27	31180 1.944 -1.6702106	29360 1.966 -1.6128106	2.035 2.035 -1.5372106	25570 1.680 -1.103106	22900 1.862 992x106	20520 2,068 8634106	1,569 1.257 354x306	2244 1.248 2408106	1.365	10.29 1.47 40.7	3.860 5.856 5.68.7	15.78	2.259 3.821
914	1 1 1 1 1 1 1	20170 2.043 -1.75/1106	26930 2.074 -1.694x106	24570 2.162 -1.613x106	24080 1.716 -1.1418106	21400 1.532 -1.004x105	19090 2.172 889x106	4753 1.173 359x106	2345 1.158 244x106	912.1 1.264 1314106	9.666 1.424 -4.0	1.994 5.607 -555.3	14.81 1.931 -273.2	2. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4.
717	¥ ₹ ₹ ₹ 201	31310 1.967 -1.5782106	29440 1,942 -1,560106	2.036 2.036 -1.4872106	25530 1.648 -1.071x106	22730 1.347 9652106	2.057 2.057 840106	4635 1.239 345#106	2278 1.225 2374106	. 783.7 1.318 1238106	10.23	1.796 6.216 -627	15.79 1.858 -203.9	2.067
¥18	16 55 24 202 203	29037 2.021 -1.703x106	2.046 2.046 -1.6428106	24650 2.129 -1.5622136	24120 1.680 -1.117x106	21300 1.917 -1.00\$x10*	18920 2.161 87hx106	1.155 1.155 353x106	2385 1.136 245x106	824.2 1.217 130x106	9.647 1.397 93.3	1.878 6.005 -623.6	11,912	2.128
674		2.614 2.614 -1.310*106	21000 2.702 -1.289x106	19720 2.8c3 -1.25;#106	18610 2.157 802210	17130 2.384 7314106	16080 2.459 659x106	3103 1.500 244x106	1529 1.571 170#106	538.4 1.834 09392106		3.06; -76.5	2.230	2.864 3.437 -437.6
8	. × × γ γ γ γ γ γ γ γ γ γ γ γ γ γ γ γ γ	24.770 2.550 -1.659æ106	23500 2.640 -1.619x106	2216n 2.749 -1.755x106	2.094 2.094 -1.043x106	19270 2.269 946x106	17960 2.418 7861106	3536 1.541 313x106	1749 1.608 213*106	611.6 1.870 1141x106		3.339 2.341 -854.7	12.95 2.195 -273.0	3.471
য়	× 20 3	2.770 2.700 -2.0592106	21240 8.823 -1.9964106	19670 2.970 -1.905x106	17610 2.214 -1.3192106	15660 2.500 -1.257x106	14420 2.744 978*106	3619 1.512 391x106	1882 1.755 260x106	657.6 1.751 2368106	9.948 1.858 - 79.82	3.623 2.029 -957.0	11.76 2.493 -359.5	3.24.3
2	الا الاراكا الاراكا الاراكا	224.50 2.659 -2.0612106	20870 2.784 -1.990x106	1986c 2.934 -1.903x106	17370 2.201 -1.3192106	15410 2.496 -1.180m106	14.180 2.748 -1.023x10 <sup>6</sup>	380. 1.472 . 391x106	1871 1.514 26010	653.1 1.701 136#106	9.868 1.829 -73.78	3.597 1.985 -957.9	11.55 2.508 -357.6	2.355 3.133 -586.
S T	15 50 10 10 10 10 10 10 10 10 10 10 10 10 10	19110 2.855 -1.0468106	2.934 -3.8857: 25	17310 3.022 5.5782106	22610 1.979 -2.655x106	20230 2.137 -2.383x16	18230 2.309 -2.031x106	1899 2.107 677x106	2.162 2.162 422106	842.9 2.413 204106	7.025 1.818 -246.50	3.135 3.258 -1021.43	13.41 2.145	3.417 4.133 -598.31
154	× 20	16:30 3.836 -4.112:106	15580 3.279 -3.967x106	15710 3.206 -3.756136	19480 2.124 -2.7372106	17230 2,320 -2,4194106	15730 2.540 -2.7602106	4798 2.096 68ia106	2367 2.147	836.0 2.394	5.195 1.091	3.13	2.323	042.5 499.5 499.5 499.5

(1) WING TORSIONS AND WING SHEAR FLOWS. CASES 425-427

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H	*		eg eg	j Ž	r F	3	3	2	# #
ľ	بو		~ 20 N	12 PE	~ 25 P		14 mg	L. P.	in all
8		11963	1.833 1.833 3.992106	2.3740 2.327 3.689£106	13970 2.547 3764106	0 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	25.45. 25.45. 25.45.	341.84 361.84 301.84	2600 2.244 30000
и		матъ	3. 1. 342.06	39365 2. 361 -3. 5061106	13370 8.632 4362106	19870 8.670 6460.06	27.3 17.3 17.3 17.3 17.3 17.3 17.3 17.3 1	300 P	19610 8.197 . Monto
83		29TBM	3,999 1,997 -3,861106	36410 8.465 -3.389610 <sup>6</sup>	12800 2.718 9042106	2.73. 2.73. 53.00.06	2. 286 2. 286 3. 286 3. 286 3. 286 3. 286	21690 8.859 186006	13400 8.896 4908106
83	Win	608 <b>8</b> N	\$65.1 268.1 368.1	37280 1.823 -2.4762306	111420 8.860 ::ideloé	2,86.9 1,86.9 1,86.106	2.05 2.05 2.05 2.05 2.05 3.05	13730 1.976 1.976 1.976	25.1. 25.1. 20.1.
£	Wing Tersions, M	NB275	37380 1.696 -2.1614106	33600 2.022 -2.1961.06	10690 8.404 2005#106	1060 8.103 3614106	10960 2.867 180406	148.90 8.108 336.106	2000 2000 2000 2000 2000 2000 2000 200
85		94684	33720 1.613 -1.8442106	30680 2.059 -1.8734106	10800 2.498 86534106	10060 2. 599 8011.06	2.183 2.183 3.192-106	orni Serios	ofcir.
8		08884	6689, 1.686 4342106	6632 1.566 63734106	1830 1.102 1183x106	1.097 1.097 18321.06	2054 2016 161.106	eres Soldes.	65.8 20.17 20.18 20.18
21		Strien	3890 1.735 1.735 394106	3296 1.612 40222106	89%.9 1.164 031%106	30.1. 1.16e 	1006 .9396 .12741.06	1861. - 36706. - 1674106	1,000 1,000 -,169006
82		916 SN	9013961 926.11 9013961	1166 1.807 197621.06	315.9 1.409 02611106	319.1 1.416 05544106	348.T 1.083 06062106	1.110 1.110 oresido	1,153 1,153 orsalo6
&		NG 83 Pront Been	16.94 1.372 -12.90	16.92 1.680 -92.90	5.167 1.886 466.8	2.157 1.811	44 44	2.306 2.318	1. % 1. 1. % 1.
S.	Wing Shear Flows	VS 83 Near Deam	3.933 2.327 -1002.63	1, 908 2, 1,20 -1070, 02	1.895 2.199 -372.83	1.960 2.148	1.865 4.465	1.1k7 5.603	1.1. 5.55
¤	rions .	NS 346 Front Beam	75.40 1.664 -835.0	2.036 -963.6	8.38 25.32 25.13	6.960 8.897	201.9 8.108	8. 040 8. 040	8. 506 8. 083
X,		115 346 Red 7 Bee	1.150 3.693 -611.18	6.06 6.09 6.09	1.939 3.131 -239.05	1.972 1.154 1.154	1.697 0.775	38	44 44

CASES 125.2 3.235 -16193 CONTINUED 1,086 1,000 26.93 2.639 -16030 135.5 5.53 1.76 2.53 3.76 3.76 (1) FUSELAGE LOADS AND HORIZONTAL 606.6 1.641 -7554 TABLE 3-2. 359.0 1.615 -25305 96.1. 18.80.4 18.90.90 175.2 1.58e -22855 1.655 1.637 2.0.9 2.071 2.071 4.00 m 3 Ę £0.4 ē 8 ş

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a. 100.00 93.0 1.9% in a series 2.3. 2.7. 2.7. 19.55 1.956 1040 CONTINUED FUSELAGE LOADS AND HORIZONTAL TABLE B-2. 35 1,555 1.50.1 118 3 2 2 Ş £12 974 7 3 \$ 3 ź

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TABLE B-2, CONCLUDED
(1) FUSELAGE LOADS, CASES 425-427

		E	*	×	×	37	88	33	04	3	, <del>,</del> ,
3					4	Fuselage 1	Loads				
		.,	,		×	8	2,	82	Α,	22 22	s'
		3550	75350	78500	18900	17857	78571	75695	78695	751006	782/206
\$84	1. 80. 100. 100.	1.356.6 1.356 1.360	6602v 1. 198 -2. 297106	834.3 1.288 -26786	16900 1.333 -5.687106	963.1 1.268 -304?y	233500 1,314 -7,722x105	689.8 1.313 -39143	96120 1.650 15.7792106	82.16 3.418 -29537	31.347 3.347 5.150.106
<b>8</b>	1g 75 34	625.1 1.166 -15272	78000 1.550 -2.064x106	935.8 1.370 -25721	196000 1.462 -4.929x106	1066 1.336 -2666	267000 1.429 -6.696106	\$12.0 1.360 -39918	39900 4.994 14.720x106	111.9 4.521 -25943	3.640 3.640 4.473.206
124	18 TOBQ	174.4 1.868 -15505	21260 1.332 -1.912kire	268.3 1.207 -23084	54670 1.269 -4.841x106	309.3 1.186 -26193	74140 1.248 -6.591x106	193.4 1.501 -23105	18940 2.251 6.098x106	30.78 7.675 -0125	14710 1.638 1.2254106
<b>8</b>	26 M 74	178.6 1.871	20760 1.340	263.7 1.200	53520 1.871	304.6	73660 1.847	137.8	19900	27.10 2.81.7	1.600
ş	¥ 30 20 20 20 20 20 20 20 20 20 20 20 20 20	1.357	16870 1.452	2.00.2	1.350	1.159	3.239	4% 4%	38800 1.914	81.38 1.727	20410 1.749
Š	k Ko	133.6	20570 1.457	247.7 1.227	50170 1.359	287.6 1.182	69240 1.322	8.276 8.276	1.870	83.88 1.73	1.695
<b>5</b> ,	7 8 1004	1.55.7 1.660	1,968	2,296 1,296	1. kgt	275.1 1.245	65740 1.398	550.8 2.009	1.697	88.19 1.589	1.516

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TABLE B-3. RESULTS OF VERTICAL GUST DYNAMIC ANALYSIS,

		1	2	3	-2	3	6	7	8	9	ដ
88		6.			Juja -	Sheers,	z				
		Accel	WETOS	WBIAS	1618M	18263	WB337	1018A	M8480	WB\$8R	MBERG
gor	¥ 8 3 2 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	.01228 1.091 1.0	154.0 1.530 16022	12.5 11.78 14.069	194.1 1.467 18421	166.2 1.601 19680	124.9 1.770 11396	127.9 1.076 13418	87.44 1.200 9184	39.15 1.161 4184	5.13 1285 1278
106	보 원 원 명 명 명	.00.727 1.832 1.0	246.0 1.530 19000	211.4 1.856 16542	297.6 1.423 20710	242.4 1.648 16517	188.4 1.930 12092	179.2 1.142 13812	120.6 1.218 9453	3.06 1.350 1120	15.60 1.063 1243
6	18 503 84 1004	.a.877 1.251 1.0	273.8 1.505 19391	231.1 1.842 16920	1.37.5 2037.5 4.45	262.7 1.616 16679	200.8 1.932 12201	194.7 1.110 13783	130.3 1.182 9433	57.18 1.307 1095	16.82 1.970 1232
<b>1</b> 01	16 18 1 18 18 1	. alshe 1.267 1.0	238.8 1.674 18863	210.4 2.012 1/669	292.8 1.539 20721	1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00	12.85	18'.3 1.129 14439	122.4 1.237 9875	1.389 1.389	15.98 11.14 12.98
8	7 20 31 20 20 31	.01834 1.293 1.0	266.4 1.668 19887	2.030 17068	323.4 1.500 2000	265.3 1.672 17082	206.1 1.887 12819	198.9 1.088 1412	133.2 1.185 9851	58.48 1.400 4276	17.21 1.157 1286
201	16 10ed	.01622 1.239 1.0	227.3 1.590 1.721	199.6 1.911 16350	278.7 1.491 20542	25.30 16.68 26.88	1.950 1.950 12180	169.7 1.182 13938	11.266 1.266 9545	50.52 1.474 4169	11.82 11.122 12.60
101	× 23 24 24	. a849 1.256 1.0	269.4 1.520 19391	2.8.1 1.356 16920	20.75.8 20.75.8	259.8 1.635 16679	139.5 1.947	191.6 1.135 13786	1.21.2 2.22.2	26.38 1.341 1095	16.56 12.090 12.090
<b>8</b> 8	¥ 53 24 24	.0396 1.834 1.0	1.693	166.7 1.960 15167	229.3 1.596 19322	198.4 1.733 15558	165.0 1.869 11627	147.3 1.279 13708	101.3	34.98 2.833 4462	13.39
109	보 보 보 보	. 8436 1.30 3.0	198.5 1.25 117999	1.5.5.5	243.2 1.689 20007	205.8 1.815 16202	1593	150.6 1.207 13959	108.4 1.350 9586	15.45 1.634 1212	13.32
ដ	보 보 보 4	.c1823 1.363 1.0	265.2 1.537 19391	25.4 1.672 16980	318.6 1.116 20941	257.2 1.655 16679	1.961 1.961 1.961 1.201	186.7 1.160 13788	1.840 1.840 9433	55.65 1.376 1095	8.91 1.112 1.123
307	ĸĸ	. a.686 1. 165	2.907	5.50 100 100 100 100 100 100 100 100 100 1	2; d	1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5	1,935	179.8 1.197	1.20.1	2.1 24	52.4
No.	KZ	2.8 2.8	1,126	1,110	1.00.1 0.01	1.058	1.009 1.009	17. t	45. 58.	<b>89.06</b>	zigi g
AS A	×21-		1. To		209.7 1.556 108.6	1.25 × 2.	35.9 2.9 2.9 2.9	1897	11. 3. 11. 3.	34 x	
Med	- 1			\$	8	1.883	11.1	308	1.16	1,160	7.7

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(b) WING BENDING MOMENTS, CASES 101-110

an n		SALON COLON	A 62220 96130 No 1.308 1.296 Load 6.3692106 5.7002106	1 90080 80630 1.377 1.372 1004 6.845x106 6.075x106	1 98030 87600 1 350 1.346 1004 6. 5752106 6.1072106	7 90960 81100 1.390 1.376 1.396 6.2992106	N 98780 88520 1.361 1.345 Load 7.079x106 6.895x106	A 85230 7610 1041 1.417 1.410 1044 6.850106 6.092106	M 96700 86430 1.370 1.366 Load 6.895x105 6.107x106	No. 11,462 1,453 1,453 1.645 5.99x106	7 7550 67850 1.1.180 1.1463 1.8.180 1.1463	N	69850 1,403	77410 69580 1.048 1.054	69000 63220 1.539 1.576	0063
13		16134	1.275 1.275 1.935x106	69060 1.368 5.1992106	74900 1.338 5.2171206	69680 1, 357 5, 360e106	7990 1.384 5.400r106	65540 1.396 5.221106	7900 1.358 5.21713-06	57060 1.442 5.070x106	98340 1.439 5.190210	72990 1.379 5.2172106	0696 1-348	60070 1.086	2.1 5.8	19630
7.	Wing De	ME263	35610 1.226 3.7492106	1,331 3,3811106	53600 1,310 3.869x106	30400 1.319 4.0404106	54750 1.863 4.0512106	47220 1.363 3.9114106	\$2880 1.332 3.65521.6	1,489 3,840x106	1.396 3.906a106	\$2220 1.355 3.885x106	1.352	813 1.08	8.1 8.8 8.8	39060
15	Dending House	N8337	25350 . 1.132 2.7532106	35030 1.218 2.797x105	37890 1.189 2.792x106	35630 1.216 2.925x106	38770 1.176 2.9192106	33280 1.258 2.8252106	37330 1.214 2.7922106	2,3090 1,350 2,807x106	29750 1.317 2.834106	3680 1.840 2.7382106	3500	86. 88. 88.	200 1,000 1,000	27350
91	sente, K	MEROF	16980 1,129 1,8402106	2.400 1.206 1.806 1.861x106	25310 1.173 1.856x106	23770 1.225 1.9452106	25870 1.188 1.938106	22220 1.257 1.860x106	24930 1.801 1.85610	19480 1,346 1.862x106	19860 1,349 1,8902106	24580 1.230 1.85610~	13900	966:	19730 1-784	1870
ኔኒ		<b>118</b> 680	8885 1.1.1 3012989.	12160 1.253 .9782106	13100 1,216 1974x106	12340 1.288 1.022x106	13390 1.261 1.017106	1.307. 9892106	2910 2421. 974476	10160 1.327 1.0202106	10350 1.452 .997x106	12730 1.877 .9742106	1.36	96. 78.	1,767	of the
36		99584	2253 1.079 .2524106	3037 1.254 20137 20137	3274 1.229 1.24 1.25 1.25	30% 1. Xe 2001.06	3349 1.314 2568106	2689 1.311 2502106	226 1.246 .245x106	2504 1.159 2604106	25.99 1.5.14 .25.11.06	3183 1.279 .2454106	306 1.376	% ę	25.70g	1
â		999 <b>8</b> 11	22.3 198. 30142460.	296.4 1.063 .335#106	319.6 1.070 033106	302. h 1.141. 20149420	27.0 7.1.1 30.13460.	261.5 1.122 .0339210 <sup>6</sup>	314.7 1.090 0331.06	234.4 1.036 03642106	233.1 127.1 2012/20	Maria State	1,157	\$ 8.	# 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	946.0

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101-110	29 30 31 K	Wing Steer Flows	Willog Willog Wilging Wilging Wilding West Dear	2.128 2.031 h.106 2.43h 3.463 2.828 2.767 2.223 -43 -296 -45 -337	3.549 2.789 6.152 3.016 3.270 2.946 2.727 2.143 -107 -135 -127 -145	3.895 2.534 6.449 3.091 3.182 2.834 2.698 2.755 -125 -163 -146 -168	3.567 2.596 6.180 2.943 3.215 3.410 2.679 2.727 -301 -418 -443 -448	3.961 2.746 6.529 3.09 3.156 3.434 2.661 2.775 -120 -447 -132 -471	3.396 2.659 6.074 2.963 3.305 3.124 2.745 2.799 -99 -416 -115 -435	3.866 2.909 6.493 3.094 3.187 2.896 2.706 2.800 -125 -463 -146 -468	2.602 1.946 5.116 2.397 3.116 3.13e 2.595 2.494 -66 -359 -92 -367	3.359 2.436 3.552 2.756 3.359 3.655 2.750 3.340 -30 -376 -08	3.841 2.941 8.713 2.944 3.193 2.941 8.713 2.949 -123 -163 -166 -168	1,227 3,236 6,228 3,328 1,031 2,107 2,031	1,482 8,187 7216 8,447 8,850 1,306 3,002	1,977 1,137 5,999 1,126 1,034 2,178 3,130 2,172	1,977 2,330 1,176 2,978 1,895 1,376 1,376
VUED FLOWS, CASES	27 28		W5588 W5668	393.0 153.6 2.217 1.487 1.28105745x106	2.567 209.5 2.567 1.725 1.99x106077x106	600.6 225.2 2.499 1.672 .21420608392106	962.8 212.7 2.556 1.802 200x1060781x106	609.2 2.585 2.585 2.582 2.582106 084x106	8.653 1.805 192106 07452106	2,554 1.714 2,554 1.714 214210608392106	2.046 1.479 2.046 1.479 173x1060665x106	2.965 2.132 2.965 2.132 1.Toklob 065fk106	2.61 1.759 2.61 1.759 2.61 0.0398106	2,786 2,984	1.0.1. 1.0.1.	3.437 2.407	190.3 137.0 1.230 1.135
CONTINUED SHEAR FLO	98		NS OB YSM	508.3 3.461 178x1.07	3.9% 3.9% -29%106	3.956 3.956 321x106	794.1 3.752 2978106	973.1 3.866 - X23106	330.8 3.960 283x106	892.7 2.971 371x136	2.996.0 2.996.0 25%106	7.7.7 3.938 8474106	899.8 1.007 301x106	3.995	203.8	1000 1.1869	1,700
B-3. WING	25 25	Torstons, Hyka	18337 NS404	853 657.8 2.934 3.574 .623106164xi.5	12390 1034 2.987 4.100 931#106312#106	12620 2,959 4,141 -1,001x106	2.960 2.960 3.920 913x106	2,951 4,039 985x106 -,345x106	3.015 3.015 896a106 296a106	12940 1157 2.971 4.165 -1.00121069452105	9732 668.9 2.872 3.302 .78221062542106	1134c 966.0 3.113 3.976 .80221062512106	13070 2.983 4.190 -1.0012106	3,006	7.77.7 1.876. 998.	3,169	1245 1.034 1.035
TABLE TORSIONS AND	23	Wing Tor	W8263 NE	8373 3.064 521x106	3.049 3.049 8514106	12860 3.005 928106	12300 3.014 831x106	2.989 2.989 907x106	12330 3.079 8134106	13010 3.016 9264106	9731 2.946 683#106	2,147 30,1417 	3.030 3.030 98623.06	983.4 641.4 1.0	6.06 5.06 1.	3,396	1.38 1.38 1.39 1.3
Š	88		16.2W	9467 3.091 356x106	12890 2.993 735x106	13520 2.921 819x1.06	2.946 2.946 706106	13740 2.893 790x136	12760 3.037 6936106	2,360 2,940 81:130	10130 2.903 9464106	3.120 3.120 593106	13730 2.958 819#106	13920 3.15	2 ° 5 8	25.4 88.	8.1 4.2
(c) WID	178		<b>WEL</b> 45	94.09 3.453 9452106	3.769 3.769 -1.438#106	13360 3.610 -1.594x106	12860 3.788 -1.3931106	13320 3.846 -1.5072106	12850 3.747 -1.379×106	13400 3.796 -1.5541106	9602 3.518 -1.1612106	12180 3.756 -1.227x106	19440 3.786 -1.5941306	268 268 268	**************************************	3,100	1,335
	&		WELOS	5929 3.672 1972105	12880 3.846 -1.299x106	13440 3.847 -1.4832106	12990 3.808 -1.2451106	13870 3.816 -1.3462106	12730 3.827 -1.237x106	13460 3.837 -1.4202106	9533 3.599 -1.003£106	12120 3.615 -1.0612106	13490 3.889 -1.1802106	17720 5.260	4. 4.	85. 85. 85.	1.35
				% %3 1667 ≯1	25 50 2007 2007	¥ %2 20 20 20 20 20	16 50 M	¥ 501 501 501	1. 503 24 ×1	동양기 10년	¥ 287 287	¥ 50 20 20 20 20 20 20 20 20 20 20 20 20 20	26 85 H	K#°	× n°	××°	××°
		* v &		101	8	103	ğ	203	8	304	901	85	97	106s	Meta	1067	No.

(d) FUSELAGE LOADS, CASES 101-110 11.628 1.628 -6075 104.6 1.539 -5216 2.815 -8500 457.7 2.918 -9129 100 103 106g 106g 19 19 106x 3 ಕ್ಷ ð ş 28 101 8 â Ned A

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B-22

TABLE B-4. RESULTS OF VERTICAL GUST DYNAMIC ANALYSIS, MODEL 749 MISSION ANALYSIS SEGMENTS
(a) C.G. ACCELERATIONS AND WING SHEARS, CASES 301-312

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S	G. AC	ACCELERATIONS	KY.	NOT	DAR D		WINGS	SHEARS,		CASES	<b>ES</b> 30
		1	æ	۳,	17	2	9	7	В	ب	01
Cane		C. G.				Susk —	Sheare	2 S			
		Accel	4S 103	\$1,T SM	161 SM	VS 263	WB 337	WS 14 Off	WS 480	48 988 ₩	WS 668
301	A No 16 Lud	.0232 1.541 1.0	131.0 1.955 11215	89, 31 2,954 9619	221.3 1.546 13888	165.6 1.927 10882	119.5 2.568 7650	153.8 1.508 97600	103.8 1.595 6755	1,6,12 1,706 2895	13.53 1.325 870
38	16 Ford	. œ48£ 1.389 1.0	130.1 1.768 90'	81.10 2.977 8552	231.8 1.430 12878	168.7 1.84£ 10109	2.573 2.573 7098	166.4 1.460 9292	112.3 1.438 6448	49.81 1.532 2761	1.152 331
<u>ئې</u>	Xo 16 Lond	.01698 1.465 1.0	76.79 2.504 10419	63.60 3.515 8808	1,3,1 1,727 12376	2.003 9524	98.31 2.136 6927	130.4 1.229 10629	92.88 1.448 6935	1,827 3,67	15.7" 1.223 1326
ź.	No Lond	.01862 1.154 1.3	75 .5 1.324 8409	61.6. 2.727 7108	147.8 1.462 1074.7	120.1 1.794 8696	105.3 2.065 6069	145.4 1,126 9885	102.3 1.295 6453	50.66 1.431 3359	16.31 1.917 1267
305	No.	.01577 1.288 1.0	181.8 1.5% 1705'i	15%.7 1.978 1%22	226.0 1.426 17755	193.0 1.610 13671	166.2 1.755 9918	172.3 1,25.5 1314	123.9 1.400 8592	59.05 1.660 1289	17.04 1.136 1541
% %	No.	.01695 1.086 1.0	188.7 1.339 15394	154.4 1.742 13010	238.9 1.267 16353	197.6 1.509 12571	165.8 1.746 913°	183.9 :.124 12479	130.4 1.263 8148	61.29 1.418 1.094	19.28 .9653 1483
307	N No. No. Lond	.0177 1.368 1.0	337.9 1.520 24627	281.9 1.770 21176	367.2 1.41.7 21.76\$	295.2 1.690 19273	2.039 2.039 13707	193.3 1.320 14851	129.7 1.401 10111	56.80 1.518 4356	16.31 1.214 1301
308	No. No.	.01916 1.175 1.3	349.6 1.321 ?2642	282.1 1.593 19499	385.8 1.276 23156	300.7 1.544 18061	225.0 1.961 12862	213.7 1.143 14115	142.6 1.218 9634	62.63 1.323 4151	19.33 1.021 1240
<u>§</u>	16 12nd	.01719 1. 965 1.0	23.7 1.574 243ya	268.0 1.863 20583	349.7 1.450 24053	288.1 1.671 18717	232.5 1.503 1,415	195.3 1.338 14478	134.6 1.6\$2 9379	\$6.75 1.481 4619	16.50 1.297 1382
one -	ig iond	.01853 1.191 1.0	334.5 1.394 12232	267.7 1.713 18815	365.5 1.325 22348	291.8 1.555 17448	227.1 1.852 12560	210.7 1.179 13709	142.5 1.500 8897	62.66 1.262 1413	18.63 1.089 1322
ā	۲. <sup>24</sup> ع المرابع	1.0 m. 1.	318.6 1.529 ?*912	260.3 1.789 19745	337.4 1.396 23143	268.3 1.599 17756	220.6 1.711 12691	1,291 1,291 1,3931	142.6 1.607 8506	20.52 20.52 20.52	16.73 1.258 1462
318	X Ko 1g Lond	.01711 1.196 1.0	330.2 1.363 21926	261.3 1,655 18069	352.5 1.248 21532	270.7 1.495 16544	214.9 1.674 11847	207.6 1.163 13195	145.6 1.509 8029	65.46 1.809 4230	18.95 1.066 1100

ບໍ່	ACCELERATIONS 10NO						-			-	
		٦	2		1;	2	9	7	9	٥	o;
Case		0.0				Ming	Shears,	:2 <sup>N</sup>			
		Accel	N: 103	W: 145	W: 192	£9≅ ‰	W: 337	401 13H	WC 1480	886 CM	999 CM
311.5	^ No 1g Ioud	.01587 1.339 1.0	288.5 1.611 23536	238,4 1,912 1962	310.3 1.444 22856	257.0 1.549 17567	212,4 1,623 12709	198.2 1.210 11230	1.529 1.529 8592	68.39 2.077 1289	17,19 1,195 1541
31.5	N. N.	.01705 1.173 1.0	299.2 1.1033 21775	2.39.5 1.758 1811	324.2 1.283 21454	260.6 1.438 16467	208.8 1.585 11889	208,4 1,129 13564	147.5 1.440 3148	69.85 1.888 1094	19.40 1.018 1483
315	⊼ No 1g Load	.01777 1.060 1.0	311.5 1.215 22866	757.0 1.468 19780	345.6 1.211 23849	269.3 1.467 18837	200.3 1.867 136 34	196.6 1.131 12178	132.2	\$8.27 3.300 1.711	17.14 .953 1456
, orc	A No 18 Lond	.02033 1.105 1.0	363.5 1.230 22642	288.4 1.512 19499	403.8 1.173 23156	309.5 1.429 18061	225.2 1.853 12862	229.8 1.057 14115	153.1 1.127 9634	66.94 1.229 1.151	19.48 .9514 1240
31.7	Mo.	.02304 1.091	376.3 1.202 22642	28 <b>6.5</b> 1.522 19499	406.3 1.150 23156	308.4 1.411 18361	221.0 1.854 12862	231.5 1.024 14115	154.0 1.090 9634	67.19 1.186 1.151	19.98 .9302 1210
318	18 K <sup>R</sup> A	,01916 1,175 1,0	349.6 1.321 22642	282.1 1.593 19199	395.8 1.276 23156	330.7 1.544 18061	225.0 1.461 12862	213.7 1.143 1415	142.6 1,218 9634	82.63 1.323 4151	18,33 1,021 12%
319	7 No 1g Lond	.03636 1.955 1.0	204.3 2.506 12483	132.6 4.015 13610	348.0 1.718 14529	249.9 2.207 14028	182.9 3.058 12753	224.1 1.505 11789	145.8 2.585 9122	63.69 1.709	18.50 1.529 1330
Si.	K. Ko Lesa	.03%61 1,822 1.0	195.9 2.384 10049	115.8 h, 290 12341	354.1 1.557 13181	242.1 2.121 13109	168.6 3.155 12214	239.1 1.329 11207	155.2 1.405 8771	67.72 1.316 4103	20.10 1.322 1288
ផ្ល	No No Ise toed	.œ861 1.599 1.3	547.9 1.737 27550	2.082 2.082 25964	603.5 2.580 26902	1.866 1.866 23018	355.8 272.4 18676	307.8 1.353 17391	198.7 1.416 12668	86.14 1.526 5766	24.36 1.109 1773
84	No No Load	.03064 1.376 1.0	553.9 1.540 25416	425.2 1.957 24223	620.3 1.372 25146	1.707 21752	350.8 2.296 17852	333.7 1,132 16601	215.0 1.194 12171	92.98 1.298 5554	27.00 1.174 1712
323	K 20.	.01.650	269.6	2.600	292.3	236.5	183.8 2.002	162.5	1.046	1.102	8105

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TABLE B-4. CONTINUED
WING BENDING MOMENTS, CASES 301-312

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		TM (D)	WING BE	BENDING MOMENTS,	MOM.	ENTS,	CASES	5 301-312	312	
		11	टा	13	134	15	16	17	18	61
Cage					- Wing De	Bending Momenty,	, X,			
		WB 103	VS 145	161 BA	E92 SM	VIS 337	707 SM	084 SM	¥E 588	WB 668
301	A No 1g Lond	63360 1.666 4.553×106	59070 1.670 1.075x10	1.680 3.541×106	38270 1.706 2.664x106	29130 1,596 1,961×106	20160 1.576 1.332106	10490 1.612 .693x106	2635 1.566 .1732x10 <sup>6</sup>	257.1 1.325 1.325 1.325
ğ	7. 10 Load	65980 1.550 4.246x106	61790 1.549 3.839×106	\$4810 1.553 3.332×106	1.570 2.519×106	31300 1.444 1.865x106	21830 1.418 1.2622106	11360 1.446 .6672100	2859 1.392 1652100	281.7 1.152 .0823x10
<b>8</b>	No.	47990 1.496 4.472x106	45550 1.430 4.059×106	41440 1.411 3.551×10 <sup>6</sup>	32840 1,410 2.732x106	25980 1.349 2.152×10 <sup>6</sup>	18340 1,393 1,4982106	9,75 1,589 .81410	2690 1.504 237×106	299.0 1.223 .0356x10
<u>క</u>	K of all	\$2650 1.385 3.983×106	3.651×106	45510 1.353 3.220x10 <sup>6</sup>	35960 1,345 2,553×10 <sup>6</sup>	28660 1.229 2.001x106	20270 1.216 1.403x105	10980 1.269 .765×106	225x136	342.3 1.017 .034×136
ጀ	ig fond	78000 1.357 6.121x10 <sup>6</sup>	71200 1.355 5.439×10	62620 1.357 4.673×106	47640 1,372 3,565×106	35020 1, 326 2,668×10 <sup>6</sup>	23910 1.350 1.826×106	12790 1.443 985×106	3229 1.405	323.8 1.136 1.0413840
ğ	K° X 1g Load	81170 1.276 5.684x106	74170 1.279 5.073x106	65260 1.284 4.375×106	1.296 3.336×106	36920 1,220 2,530x106	25330 1.216 1.738×106	13530 1.268 1.939×106	3479 1.170 .268x106	366.2 56.2 039841
39	No 18 Load	107400 1.490 7.890x10	94610 1.496 6.889x135	7980 1.502 5.812x106	35920 1,509 4,249x10 <sup>6</sup>	38100 1.404 3.007x106	25090 2.387 3.987×106	12970 1.127 1.339x106	3226 1.407 2602106	379.9 1.214 0349x10
308	K°o X	11.7600 1.318 7.407×106	99480 1.386 6.4862106	84230 1.332 5.455×10°	\$9390 1.337 4.232x106	41600 1.224 2.857×106	27720 1.203 1.893×10 <sup>6</sup>	14340 1.239 .9901106	3579 1,212 .248x106	348.2 1.021 33275
<u>&amp;</u>	1 ost toed	106300 1.474 7.722×10 <sup>6</sup>	94070 1.479 6.736x106	80020 1.487 5.686x10 <sup>6</sup>	\$7030 1.511 4.176×10 <sup>6</sup>	38860 1,449 2,960x10 <sup>6</sup>	25440 1.453 1.958x10 <sup>6</sup>	13090 1.477 1.053×106	3233 1.407 .276×106	313.6 1.297 37076
310	Is load	11,335 1,335 7,215x106	97600 1, 342 6, 315x136	83170 1,353 5,348x106	59410 1.372 3.9452106	41400 1.290 2.807x106	27410 1.284 1.863x106	14190 1.290 1.004x106	3596 1.190 .264x106	353.9 1.089 35466
TE.	Ho Tond	134600 .387 7.370x106	92770 1.392 6.407x106	79:00 1,1:05 5,398:106	57610 1.453 3.964x106	1.452 1.452 2.809x106	26670 1.517 1.844x106	13980 1.665 .993x106	3383 1.744 .280x176	317.9 1.258 39227
द्य	A Sold	107200 1,275 6,887±106	95090 1.284 6.004x106	81220 1.301 5.072x106	58830 1.353 3.738106	1,334 2,560x106	27750 1.387 1.749×106	14550 1.515 944x106	3635 1.523 .268x106	360.0 1.066 37605

370.2 .95%1 33275 370.6 .9302 33875 3375 357.4 1.529 .036x106 WS 668 CASES 313-323 15560 1.430 .9502100 084 SN 29740 1.114 1.893x10<sup>6</sup> CONTINUED 407 GA Wing Bending Moments, M. 41600 1.224 2.857x136 40910 1.411 2.829x106 1,129 2,857×106 1.096 2.857x106 WING BENDING MOMENTS, 58850 42130 1.304 1.307 3.769x106 2.691x106 38340 1.196 3.125×196 WS 337 62650 1.203 .232×106 55610 1.661 3.451×106 62620 1,229 237x106 59390 1.337 .232x106 3.618x106 TABLE B-4. WS 263 79760 1.257 5.094x106 38480 1.224 5.485x106 84230 1.332 5.485x106 161 BM 92450 1.247 6.027x106 104300 1.219 6.486x106 99480 1.326 6.486x106 PHS .45 7 103400 No 1,246 16 L ad 6,9033400 11.7800 1.214 7.407×106 112600 1.318 7.401×106 92950 1.725 5.472×106 1.189 1.189 7.107×106 101900 1.250 7.823x106 100800 1.344 7.34x106 WB 103 E Case 33 316 328 å 8 ŧ 325 317 ã ផ្ត 8

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TABLE B-4. CONTINUED WING TORSIONS AND WING SHEAR FLOWS. CASES 301-312

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		3	WIN	G TORSIONS		AND WING SHEAR	NG SHI		FLOWS,	CASES	301-	312		
		20	21	22	23	7,8	25	92	27	28	33	34	35	36
Č					y gu ix	Wing Torsions, MyEA	5					41 ng Che	ding Chear Floars	
		WB 103	WS 145	WS 191	WB 263	WS 337	HC TOT	084 SN	90 <b>5</b> SM	AT 668	AS 103 Front Beam	JE 103 Rear Beam	MS 337 Front Beam	WE 337 Rear Boom
301	A No 1g Lond	14170 3.926 -1.946x10 <sup>6</sup>	15670 3.520 -2.118x10 <sup>6</sup>	10000 3.553 -1.131x10 <sup>6</sup>	10247 3,390 -1,180x106	10870 3.120 -1.214x106	1281 4, 395 -, 398klo <sup>6</sup>	901.0 1.586 351×10 <sup>6</sup>	517.5 3.288 227x106	183.1 8.169 0907×10 <sup>5</sup>	2.810 4.451 -297.3	2.928 3.014 -470	4,538 3,031 -279	2.935 3.224 -465.9
302	A No 1g lond	15790 3, 522 -1,991x106	17950 3.093 -2.0913106	13150 3.608 -1.155x135	10870 3.299 -1.198x.06	11890 2.947 -1.2214106	130e 4,364 -,398x106	917.5 4.532 350x106	548.2 3.089 226x106	230.2 1.947 0903x106	2.905 4.153 -317.6	3.400 2.716 -163	4.719 2.975 -289.6	3.298 2.954 -1.59.8
303	الا تواديم الأواديم	8114 1, 496 -1, 469x105	63& 4,123 -1,621×106	6447 2,190 -,886x106	1,109 2,880 -1,005x106	3385 3.123 -1.0%0x106	\$516 2.418 :04x106	295.6 2.365 369x106	408.1 1.427 239×106	194.6 1.300 0950210	1.860 3.718 -215.8	1.340 3.292 -366 4	2,148 2,626 -20,1	1.30) 3.251 -402.5
ర్లే	76 Fond	6439 4.133 -1.539×106	595, 4,188 -1.679×10°	5034 2.190 923#106	2991 3.011 -1.033×10 <sup>6</sup>	3534 2,340 -2,0994206	495.7 2.450 404x10 <sup>6</sup>	388.8 1.830 3571106	483.5 1.134 237×106	227.0 1.043 094x106	1.457 4.149 -248	.9967 4.163 -354.5	2.330 2.23 194.1	1.366 2.554 -395.3
<u>\$</u>	7, 7, 7, 16 2.0md	10510 2.626 -1.242x106	7743 3.281 -1.4272106	9501 1.733 764x106	5942 2.145 915x1.06	1,642 2,516 -1,013x106	533.4 2.424 404x106	1,900 1,900 -,376x106	1.331 1.246x106	214.7 1.200 097x106	3.139 2.346 -110.2	3.857 -405.2	3.682 2.054 -194.1	2.790 2.790 -127.5
%	16 Logs	%in 3.04 -:.3004106	60.0 3.962 -1.477×106	7257 1.622 794x106	4640 2.176 939×106	3874 2.461 -1.030x106	505.0 2.410 404x106	1,614 1,614 374×106	\$62.6 1.123 244x106	245.8 .9959 096x106	2.779 2.396 -137.4	1.040 3.664 -395.1	3.402 2.094 -211.8	1.670 2.274 420.3
ळू	K on si	16350 3.332 -1.488x106	15550 3.449 -1.687x106	17080 2.762 884×106	16190 2.868 998¤106	15800 2.890 -1.072x106	1307 4.390 397×106	1030 4,151 -,365x106	634.1 2.845 242x106	223.5 1.929 0947x106	5.334 2.605 -84.1	3.021 2.689 -548.4	8.178 2.582 -1 <sup>1</sup> 3.2	3.040
308	7. 16 load	14240 3.700 -1.564x106	14030 3.707 -1.692×106	15500 2.927 923110 <sup>5</sup>	14820 3.021 -1.029x10	14740 2.992 -1.096x10 <sup>6</sup>	1320 4,378 3972106	10th 1.111 367.256	679.8 2.634 240x3.06	249.3 1.692 0942x13 <sup>2</sup>	2.725 2.746 -117.4	3.625 2.317 -538.1	7.433 2.693 -163.2	3.389 2.951 -508.8
806	18 10 H	3.380 3.380 -1.392x106	12200 3.301 -1.547x106	1,930 2,378 -1,014x106	12690 2.516 963×106	2.558 2.558 -1.047x106	830.0 3.339 401-106	630.3 2.879 372×106	563.5 2.141 244x106	216.0 1.698 -95513	2.3070 2.3070 -66.4	2.391 2.820 -529.7	7.124 2.294 -140.1	2:25 2:77 500
93	14 °5 ≥4 100 to	11270 3.455 -1.481x106	10440 3.602 -1.623x106	12970 2.536 8831106	2.680 2.680 999x106	11370 2.664 -1.074x106	839.5 3.347 401×136	678.3 2.707 370×106	618.8 1.876 242x105	244.3 1.427 -94936	4,333 2,432 -103.9	2.957 2.233 -519.4	6.539 2.399 160.8	2.6% 2.3% 1.98.0
a	16 50 ™ 1085	10180 2.67 -1.3072106	7902 3,192 -1,475×106	9779 1.890 7902106	81.9 2.138 931×106	7325 2.240 -1.023x106	627.3 2.867 401x106	470.7 1.948 375x106	\$40.5 1.726 245x'06	214,2 1,495 96290	1.436 1.975 -50.2	2.097 2.793 -512.9	5.425 1.939 -142.7	2.376 2.376 -166.5
ZIZ	T No 12 Lund	7865 3.113 -1.3832106	9909 1.830 -1.340x106	8998 1.941 831x106	6870 2.273 962x136	6917 2.296 -1,046x106	620.7 2.830 101x106	545.1 1.696 373×106	597.6 1.494 2431106	244.4 1.249 -95669	1,038 1,965 -£6	2.658 2.056 502.7	4.892 2.010 -162.5	2.130 2.055 -478.9

TABLE B-4. CONTINUED
WING TORSIONS AND WING SHEAR FLOWS, CASES 313-323

		ت ا	E) WIN	G TORE	NG TORSIONS AND WING SHEAR FLOWS,	IND WI	THO DN	T YUR	, E	3000	CASES 515=565	6.5		
L		50	23	22	23	24	25	56	2.1	લ	ĸ	3	32	×
5					Wing 7	Wing Torstons, MygA						- Ving Shear Flow	er Plove	
		WS 103	48 145	161 8W	NE 263	WS 337	401 UN	087 SH	NS 388	VC (68	Wr 1r3 From beam	WS 103 Rear Beam	WB 337 Front beam	NB 35' Rear Bys
ä	¥ 0.3 2.0 2.0 3.0 3.0 3.0 3.0 3.0 3.0 3.0 3.0 3.0 3	10960 2,395 -1,237×106	8201 2,934 -1,4172106	9755 2.845 753×106	7356 2.194 90'x106	6067 2,439 3,003×106	660.2 2.732 399x106	193.6 2.042 376x106	545.5 1.521 246×106	218.9 1.343 -96931	1,276 1,918 -12.0	1.631 3.837 -198.8	1.839 1.852 -137.2	1.810 2.908 -176.0
켰	16 N M	8876 2.65: -1.295x106	6110 3.523 -1.4681106	8483 1.784 788x106	\$996 2.273 928x106	5048 2.515 -1.0212106	653.3 2.633 399x106	558.8 1.776 374×2106	601.2 1.21 244106	249.2 1,126 -96495	3.95h 1.893 -69.1	1.989 2.798 .482.6	1.893 1.893 -135	2.03. 2.363. 1.70.0
â	K 20 3	12940 3.786 768x106	13860 3.673 9201105	13530 3.091 235x106	13240 141.8 201x704	13320 3.068 5502106	1199 4, 345 2482106	959.8 4.089 -32200	632.3 2.616 . 43800	233.5 1.653 -12430	3.947 ?.907 30.456	3.616 2.222 - 380.6	6.467 2.773 11.355	3,394 2,792 -348,2
376	No No Load	13920 3.787 -1.564x10	13980 3.731 -1,692×106	2,968 2,968 -,985x1.0	14050 3.065 -1.009x106	14060 3,009 -1,096x106	1310 4,346 3972106	1041 h. 159 - 36725 6	711.1 2.486 2400106	264.0 1.591 -94200	1.584 2.776 -117.4	2.935	6.9 <b>63</b> 2.705 -163.2	2.788 2.788 -508.8
Ħ	No Lond	13850 3.827 -1.564x136	13900 3.762 -1.692x106	14260 2.939 925x106	13530 3.045 -1.029x106	13590 2.980 -1.096x106	1282 4,293 397x106	1015 4,011 -, 363×106	709.9 2.400 2400106	269.4 1.518 -94200	4.735 2.739 -117.4	2.085 2.086 -538.1	6.137 2.703 -163.2	3.53h 2.724 -503.8
gg g	16 50 X	14240 3.700 -1.564x106	14030 3.707 -1.6921106	15500 2.927 925x106	14520 3.021 -1.0292106	14740 2.992 -1.096x106	1320 4.378 397×106	1044 4,111 363×106	679.8 2.634 240x106	249.3 1.692 -94200	2.705 2.746 -117.4	3.685 -536.1	7.433 2.693 -163.2	3.389 2.951 -508.8
â	18 No 24	12450 4.524 -1.8472106	13610 3.880 -1.856x13	13210 3.728 834×106	12050 3.933 8851106	12390 3.753 951x106	1701 4.913 Olutio	1127 5.055 029x106	681.2 3.256 3.040x106	245.6 2.191 2.01x106	3.079 4.828 -283.4	3.119	6.409	2.607 4.780 -170.9
8 X	K PO	15280 4.218 -1.901x106	18110 3.393 -1.8972106	11920 4,039 -,8652106	1170 3.950 904106	13.70 3.94 -1.068106	1729 4,857 01x10	1137 5.027 0282106	714.7 3.090. 3.0301.06	267.5 1.943 30206	3.190 4.983 -309.7	3.385 2.837 -433.6	6.385 3.387 -155.0	2.9?7 4.243 -498.7
결	الا م الا م الا م	25170 2.119 -1.3431106	20790 2,307 -1,448:206	26650 2.742 534x106	23770 2,991 -,694x106	22150 3.136 3.8212105	1793 4.875 .0152106	1434 4,239 -,044×106	928.0 2.663 054x106	328.5 1.293 0.5x206	9.280 2.969 -13.5	2.151 2.751 -537.8	12.38 2.794 1.4.7	2.889 4.806 -517.6
×	K 602	19500 2.306 -103x106	15200 2,640 -1,495x106	23210 2.910 5882106	20450 3.235 715x106	19790 3.370 834x106	1802 4,842 .0143106	1418 4.249 42x106	977.9 2.457 052x106	363.2 1.636 014x106	8.128 1.941 -75.4	3.406 1.989 -722.3	10.79 2.962 -1.3	3.140 4.377 -509.6
×	Xo Xo 1g Ioas	10060 3.935 576x10€	10900 3.750 734x106	10360 3.250 1442106	10190 3.284 3102106	10430 3.191 447×106	970. b	719.8 3.642 0292206	509.3 2.203 U40x106	193.8 1.369 0115x106	3.258 3.154 .46.9	3.024 1.693 -3175	5.523 2.988 +20.4	2.727 2.067 -294.1

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(h) FUSELAGE LCADS AND HORIZONTAL TAIL TABLE B-4. (g) FUSELAGE LOADS, CASE 301-312

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		37	82	33	O.	141
Case			- Puselage	Londs		Boriz.
		95½ 8.4	F8 456	82, PS 976	75 ST	Tail
313	A Lond	222.8 1.765 -18398	24770 2.102 -2.222x10 <sup>6</sup>	79.32 1.996 -9379	17630 1.862 1.628130	
314	¥ ¥ ¥ ¥ ¥ ¥	267.7 1.811 -10398	31190 2.176 -2.822x106	1.503 1.503 -5972	21550 1.508 .935x106	
325	R Lond	304.0 1.735 -19658	37050 2.0e7 -2.231x136	101.3 3.469 -5710	2.060 1.577 9021:00	117.56 1.373 -4189
316	A M Le Lond	354.5 1.750 -18396	43330 2.034 -2.222x106	115.4 1.652 -682	1.09341 5	129.7 11.463 -5309
31.7	1g Load	368.5 1.725 -18398	2.306 2.306 -2.222×106	119.2 1.630 -6829	23860 1.686 1.0932106	1.458 1.458 -5309
ere	le Irra	323.7 1.519 -18398	39180 2.121 -2.222x10¢	93.36 1.545 -6379	19450 1.551 1.0932106	99.84 1.757 -5309
61X	A M foad	567.0 2.246 -17875	69570 7.433 -2.0658206	71.09 3.198 -15773	17730 3.131 2.612x1c6	
8	A Lond	671.5 2.261 -178?5	1900 2.460 -2.065110 <sup>6</sup>	73.68 3.008 -15773	19767 2.732 2.612x106	
ra ra	1€ Kond	1.865 1.865 -17875	49013 2.141 -2.365x135	88.61 2.747 -14787	2092) 2.620 2.445x106	
83	X 16 Load	518,1 1.784 -17875	(233) 2.017 -2.0651106	2.3.38 -14787	25640 2.081 2.4-5x106	
 <b>183</b>	A H lg Lond	250.0 1.793 -18701	30460 2.030 -2.324×206	84.01 1.412 -5038	16997 1.352 .78321.06	

17090 1.98h 1.7122106

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TABLE B-5. RESULTS OF LATERAL GUST DYNAMIC ANALYSIS, MODEL 188 MISSION ANALYSIS SEGMENTS

Case		Fore Body	Fore Body	Aft Body	Aft Body	Áft Body	Fin	Fia	C.G.	Flight Station
		Sy	МZ	s <del>,</del>	H <sub>Z</sub>	ų,	Py	Hx	Ху	n,
8 <b>01</b> .	X <sub>o</sub>	123.4 .6999	44680. .6565	114.4 .5726	.1136E .7315	31550 .6534	228.7 .6534	18070. .6534	.00464 •5759	.00195 2.657
505	X	140.4	51650.	122.7	.1376B6	37330	269.7	21310.	.00564	.00233
	No	.7308	.6836	.6519	.8856	•7872	.7872	•7872	.6170	3.253
203	Ä	125.6	46060.	111.8	120886	33310	240.6	19010.	.00491	.001 <i>8</i> 9
	¥o	.6616	.6183	.5847	.8023	.7047	.7047	•7047	.5544	3.172
204	X	147.9	53580.	133.1	.1391E6	38070	275.1	21740.	.00540	.00234
	No	.7167	.6724	.6379	.8711	•7715	.7715	.7715	.6053	3.149
205	X	119.1	42970.	108.5	.111926	30560	220.8	17 <b>440.</b>	.00425	.00175
	¥o	.6 <b>30</b> 9	•5932	.5422	.7125	.6378	.6378	.6378	.5304	2.743
206	I I	130.9 .7188	48380. .6784	107.4 .6439	.1271 <b>3</b> 6 .8 <b>50</b> 6	34700 •7542	250.7 .7542	19810. .7542	.00523 .6214	.00237 2.830
207	X	114.6	12320.	95.21	.112216	30650	221.5	17490	.00460	.00197
	No.	.6652	.6268	.5885	•77 <b>9</b> 5	.6907	.6907	.6907	.5719	2.763
508	X	168.7	61360.	142.2	.1587E6	43080	311.2	24590	.00607	.00292
	Yo	•?\59	•7047	.6 <b>95</b> 9	.9576	.8458	.8458	.8453	.6466	3.171
209	X	137.5	50150.	138.4	.1308E6	35570	256.6	2027u	.00496	.00229
	No	.6763	.6378	.5500	.8375	•7411	.7411	.7411	.5815	2,922

TABLE B-6. RESULTS OF LATERAL GUST DYNAMIC ANALYSIS, MODEL 188 DESIGN ENVELOPE CASES

<b>a</b>		Fore Body	Fore Body	Aft Body	Aft Body	Art Body	Vertical Tw <sup>1</sup>	Vertical Tuli	c.c.	Flight Station
Case		S <sub>y</sub> .	Хg	Sy	N <sub>g</sub>	Уx	Py	Hg	n y	n <b>y</b>
601	¥ <sub>o</sub>	189.8 .6711	69050 .6493	125.6 .6213	.1275H6 .6672	47900. .7914	346.1 .7914	27340 •7914	.00546 .5017	.00250 3.396
602	X	187.9	68734	127.1	.1025B6	47900.	345.7	27320.	.00486	.00382
	No	.6665	.6439	.6164	.7008	.7859	.7859	.7879	.6325	2.214
603	X	179.5	66109.	127.7	.1066E6	47692	344.6	27220.	.00532	.00224
	No	.6447	.6272	.6075	.6914	•7735	•1735	•7735	.5746	3.558
604	X	152.4	54890	106.3	85491	39940	2 <b>66.</b> 6	22 <b>800.</b>	.0044	.00175
	No	•5575	•5480	.5390	.6033	.6738	.6738	.67 <b>3</b> 8	.5047	3.337
605	X	122.2	₩870.	70.32	64476.	31610	228.4	18043.	.00356	.00125
	No	.4730	.456€	.4201	.4936	•5481	.5481	•5481	.4174	3.134
606	X No	240.4 .7213	88380. .7017	.6978	128900 •7979	60820 .8936	439.5 .3936	34717 .8936	.00687 .6631	.00315 3.748
607	X	235.9	8663ī.	.8061	141500.	61700	445.8	35215	.00686	.nc303
	No	.71.83	.6986	.8061	.8340	.8881	.8881	.8881	.6609	3.781
608	X	226.0	85396.	160.6	130758	61118	443.8	35058	.0069a	.00302
	No	.4357	.6946	.6996	-7958	.8814	.8844	•8844	.6602	3.702
609	X	173.7	63870.	122.8	99400	16160	335.7	26521	.00513	.00206
	No	.6288	.6090	.6067	•6908	.7704	.7704	.7704	.5699	3.654
610	X	135.4	19994.	96.4	7.990 <b>.</b>	36530.	263.9	20849.	.00402	.00145
	No	.5064	.1893	.4801	•5480	.6117	.6117	.6117	.4531	3.293
வ	X	142.2	56700.	541.9	81200.	43860.	316.8	25030.	.00673	.00278
	No	.6784	.6621	1.575	.7448	.8570	.8570	.8570	.6466	3.583
612	X	117.2	70700.	69.0	99440	55563.	401.5	31716.	.00f10	.00331
	No	.7475	.7348	.7329	.8744	.9806	.9806	.9806	.73\8	4.089
613	N	235.6	75780.	95-33	170050.	10000.	289.1	22840.	.00024	.0036A
	X	.7061	.7070	-9229	•7554	.9460	.9460	.9460	.7119	3.552
614	X	296.3	95140.	116.5	219000	50845	367.4	29022.	.01.026	.00k30
	No	.8000	.8020	.9980	.8246	1.086	1.080	1.080	.7968	k.065
615	X No	137.4 .6550	53490. .6367	50.85 .6342	71685 •74 <b>0</b> 9	40550. .8393	.8393	23146, .8393	.00659 .6300	.0249 3.746
616	λ	151.6	53170.	99.17	81850.	39250.	283.6	22400.	.0CA37	,00208
	H <sub>o</sub>	.5587	.5512	.5398	.6200	.6896	.6896	.6896	.5228	2,754
617	X N <sub>C</sub>	183.6 .6803	65540. .6 <del>5</del> 92	118,1 .6407	122000, .6937	46700, .8162	.8165	26650. .8162	.00533 .6300	.00261 2.934
618	N	119.7	43280.	63.78	•272°	30630	221.3	17500.	.00945	.00153
	N	.4798	.4646	.4308	•273°	.5676	.5676	.5676	.4379	2.525
619	X No	.6292	623 <b>80</b>	114.2 .6146	94950. .7105	45550. •7923	329.1 .7913	26000. •1913	.00503 .5861	.00246 3.07?
620	Ä No	131.1 .5158	47690 .5000	87.52 . <b>195</b> 9	72700 •5745	.6404	252.* ,6404	19951. .6404	.00585 .4757	.00179 2.680
623	F.	e. 1,0 ,453b	81413 .7060	146.7 •7161	122417 .8295	<b>59080.</b> •9214	426.9 .9214	35723 .9214	.00656 .6860	.00355 3.151

TABLE B-7. RESULTS OF LATERAL GUST DYNAMIC ANALYSIS. MODEL 749 MISSION ANALYSIS SEGMENTS \_\_\_\_

		ببدور	177	******		4744	WT 191	UE C	IMEN	10
Case		Pore Body	gody.	Body	Aft Body	Dody Act	Yertical Tail	c.g.	Flight Station	Vertical Tail
		87	N <sub>3</sub>	87	Mg	M <sub>x</sub>	Py	H <sub>y</sub>	n <sub>y</sub>	<b>"</b> y
101	N <sub>O</sub>	28,85 1,182	3220. 1,662	105.4 .5504	11313. .5503	1819 .5501	131.2 .5509	.003545 .5344	5°130 '00115#	.008789 .5603
302		20.74 1.815	2590. 2.539	139.4 .6579	15005. .6542	10347 .6664	171.5 .6762	.00362 .5650	.002574 2.056	.01.095 .7786
103		17.34 2.032	2356. 2.69	148.8 .6640	16054. .6595	110 <b>6</b> 2. .6702	181.4 .6864	.003461 .5641	.002809 1.899	.9619 .01052
204		20.33 1.796	2479. 2.510	144.8 .6420	15630. .6387	10686. .6496	176.1 .6585	.003557 .5507	.092434 .2053	.01.065 .7568
105	X	16.72 2.207	2555. 2.614	141.4 .7187	15255. .7241	10kb9 .7300	172.4 .7426	.003184 .6068	.002949 1.902	.01061 .8856
106		19.63 1.739	2320. 2.571	140.6 .6172	15158. .6138	10\12 .62\9	172.1 .6339	.003567 .52 <del>0</del> 9	.002377 2.022	.01071 .7301
107		18,32 1.953	2432 2.641	150.9 .6644	16292. .6600	11135. .6748	183.4 .6868	.003507 .5659	.002765 1.941	.01111 .8216
108	X Yo	17.34 1.668	1994. 2.517	124.7 .5941	13\71. •9908	9192. .6017	151,2 ,6105	.903062 .5136	.001932 2.075	.009024 .7078
109	X	17.91 1.619	200 <b>\.</b> 2.515	129.8 .5725	14006. .5696	9599. •5790	158.4 .5867	.003281 .4902	.002034 1.985	.009717 .6107
110	X No	18.42 2.016	2557. 2.613	151.2 .6769	16308. .6724	11173. -5877	184.4 .6999	.003528 .5772	.002921 1.913	.0113k .8355

TABLE B-8. RESULTS OF LATERAL GUST DYNAMIC ANALYSIS, MODEL 749 DESIGN ENVELOPE CASES

		Fore Body	Fore Body	Aft	Aft Body	Aft Body	Vertical Tail	C.G.	Flight Station	Vertical Tail
Case		Sy	N <sub>z</sub>	Sy	Mg	×	Py	H <sub>y</sub>	237	<sup>B</sup> yr
501.	X W <sub>o</sub>	29.67 1.625	3309. 2,306	185.6 .645	20190. .643	13450 .651	217.6 .659	.003% .548	.00242 2.093	.01.090 .757
502	X X	20.86 2.750		252.3 .7569	28122. .7383	18142. -7714	291.1 .7880	.6215	.00381 1.992	.01332 1.031
503	¥,	28.42 1.621	30590. 2.392		20800. .6040	13270. .6344	214.6 .6419	.00360 .5249	.00230 2,116	.01.074 .7409
50k	X X	36,61 1,521		247.6 .7365	27700. .7164	17810. .7516	2'5.8 .7681	.003/54 .5948	.00368 2,03	.01305 1,0164
595	X No	18.36 2.959		246.0 .7282	27558. .7074	17694. .7434	263.9 .7607	.00362 .5844	.00362 .005	.01217 1.068
506	X No	27.11 1.632		182.3 .610	20705. . 584	13139. .6176	212.5 .6255	.00355 .4958	.00220 2.162	.01.061 .7290
507	Ä	18,50 2,70		229.5 .6894	25030. .6539	16521. . 7030	265.4 .7185	.00351 .5439	.00328 1.979	.01226 .9386
508	Ĭ,	25.10 1.530		169.4 .5624	19590 •5324	122 <b>80.</b> . <b>568</b> 2	198.7 •5750	.00335 •4595	.00200 2,045	.00998 .6648
509	Ã X	19.13 2.369		206.5 .6537	23440. .6264	14900. .6655	239.6 .6791	. 30336 . 5054	.00262 2,005	.01030
510	X M	27.14 1.255		159.0 .4902	18840. - 4554	11560. . 1938	187.6 • 4963	.00341	.000.67 2.048	.00972 .5544
511	X No	33.50 1.036		127.4 .4851	15600. .4374	9320. .4858	152.2 .4873	.00337	.00110 2.783	.0084
512	Ā,	23,53 1,519		167.5 .⊊73	18250. • 5246	12160 -5337	196.7 .5413	.00330 .4058	.00187 2,095	.00985 .6375

TABLE B-9. RESULTS OF VERTICAL GUST DYNAMIC ANALYSIS, MODEL 188 PARAMETER VARIATION
(a) C.G. ACCELERATIONS AND WING SHEARS, CASES 202-202-7

5	ACCELERATIONS	7337	777	-	2	W LLVC		SUPPLIE		CASES	-202	707
		1	2	~	.3	5	9	7	8	9	10	
Cus		C. G.				Ming -	Shear, S.					
		Accel	WB 83	WB 119	₩ 167	WB 209	WB 275	MB 346	¥18 380	WB 1448	VB 516	
Chue)	A No 1g Lond	. (2133 1.201 1.0	253.9 1.686 19055	247.8 1.841 16386	220,0 2,118 11862	274.1 1.993 13979	237.8 1.601 9889	181.2 1.787 5300	162.7 1.237 7679	94.74 1.433 4161	39.56 1.834 1531	
202 81 <b>6</b> 14	× °2,	.01913	192.5 1.554	173.7	129.4 1.575	194.5 1.345 Sume As	155.1 1.310 Case 202	97.61 1.328	145.5	83.69	33.70	
202 Ctick Fland	¥ 20 37	.02259 1.037	280.0 1.995	269.0 1.758	234.0 2.060	296.1 1.480 Seme An	252.5 1.513 Case 202	1.772	152.5	106.3	1,632	
202-1	N N N N N N N N N N N N N N N N N N N	.02141 1.241	236.5	250.6 1.886	223.2	276.9 1.595 Semo As	239.6 1.496 Gree 202	1.602 1.602	162.9	95.19	2,185	
200-2	1, 50 M	.02148 1.205	257.6 1. TOS	231.7	223.7	278.3 1.536 Same As	241.8 1.530 Case 202	183.8 1.702	166.7	97.05 1.411	40,48 1.813	
202-3	No Ioed	.02156	24′.3 1.TP	254.8 1.902	27.2	281.7 1.546 Same As	244.5 1.438 Case 202	186.2 1.615	167.0 1.246	97.52	41.05	
4-808 4-18	¥ 2.5 2.5 3.4	.0216 1.21 1.0	250.3 1.757 19055	243.7 1.912 16386	215.8 2.195 11862	269.8 1.647 13979	233.3 1.641 9889	177.4 1.835 5300	160.0 1.282 7679	93.27 1.508 1161	39.08 1.961 1531	
200-5	le Load	, cerzo 1, 164	249.8 1.652	242.8 1.807	214.0 2.093	269.1 1.558 Same As	232.5 1.566 Case 202	175.9	162.1 1.219	8.4 1.43	39.31	
9-808	7, % N 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	1.168	250.5 1.683 1.872	243.3 1.849 15067	214.1 2.151 10760	272.9 1.538 13060	235.3 1.579 922 <sup>1</sup>	177.6 1.780 1872	166.6 1.188 7349	96.37 1.383 3978	10.10 1.782 1459	
202-6 N1g14	N of part of	.01989 1.168	194.6	175.2 1.438	129.4 1.477	199.9 1.271 Bane As	159.1 1.240 Cane 202	99.47 1.257 6	151.3	67.09 1.088	1,8% 1,8% 1,0%	
202-7	K 5 34 1084 1084	.02116 1.215	252.3	245.9 1.882	218.0	272.5 1.598 844 As	236.2 1.600 Case 200	179.7 1.779	161.6	94,13	39.33	
206-7 Rigid	N N 1¢ load	.arb96 1.261	191.5	172.8 1.479	128.8 1.507	193.1 1.328 Sume As	153.9 1.290 Case 20P	96.42 1.296	1.174 1.174	82,92 1,153	33.38 1.132	
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	C. C. ACCELERATIONS AND WING SHEARS, CASES 202-9-207-1
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TABLE B-9. CONTINUED	ARS
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v. C.C.	ACCELERATIONS	LERA	TIO		AND	NINC NINC	WING SHEARS,	ARS,	- 1	CASES	202-7-202	7-7
		1	æ	3	7	\$	9	7	0	6	97	
		0.				MIN.	Wing Shears,	_ Z .				
		Accel	WS 83	911 8M	WB 167	WS 209	VB 275	316 BH	08£ SN	844 8M	418 S16	
208-9	X. 16 load	,02159	254.7 1.555	216,9 1,689	216.4 1.944	275.6 1.475 Bame Ao	237.5 1.516 Case 202	178.0 1.711	1,891	97.84 1.243	40.73 1.544	
202-9 R1614	No.	.01945 1.183	196.1 1.433	176.7	134.1 1.42h	199.2 1.202 Some As	158.5 1.154 Chee 202	99.3 1.162	1,030	36.20	34.12 .970	
202-10	A No 1g Loed	.02264 1.243 1.0	285.6 1.698 1856	282.7 1.829 15961	256.6 2.053 11564	303.4 1.576 13775	268.7 1.587 9800	210.3 1.7% 5289	169.3 1.270 7687	98.69 1.485 4175	41.30 1.980 1539	
202-10 Rigid	¥ 2° 34	.01965 1.243	205.4 1.575	188.0 1.553	1,5,1	200.3 1.367 Sume Au	162.9 107.0 1.340 1.376 Cure 202-10	10.0 1.376	143.6 1.176	1.155	33.22	
202-11	16 foed	.02601 1.280 1.0	320.9 1.713 1967	115.3 1.865 16238	262.9 2.133 10631	347.4 1.550 12401	303.1 1.560 7712	231.8 1.734 2967	203.9 1.271 5473	118.7 11.440 2646	1,791 360	
202-11 Rigid	No.	.02269 1.332	231.5 1.736	209.0 1.706	156.2	232.1 1.511 Same Ass	185,1 116,8 1,469 1,481	11.481	172.7 1.321	99.27	39.96	
208-12	₩ 20 10 10 10 10 10 10 10 10 10 10 10 10 10	.01692 1.145 1.0	223.5 1.701 17655	218.1 1.853 15376	193.8 2.133 11325	2/1.1 1.618 13605	209.1	159.8 1.808 5822	143.2 1.217 8248	83.47 1.418 4601	34.89 11.828 1736	
202-12 Rigid	No.	.01709	170.8 1.434	154.2 1.467	1.513	173.2 1.28% Same Ass	138.2 86.99 1.246 1.260 coar 202-12	86.99 1.260	130.0	7.82 1.084	30.15	
202-13	No Lond	.0047 1.067 1.0	344.0 1.409 23769	333.3 1.507 20708	299.3 1.686 15646	339.8 1.468 17289	293.1 1.538 12495	225.4 1.717 7168	187.3 1.134 9194	110.1	1.563 1.964	
207-1	76 18 1℃3	.01\$13 1.10¢ 1.0	1.7.3 1.772 16201	168.3 1.893 14358	147.0 2.163 10861	193.4 2.063 13829	163.6 1.996 10637	122.4 2.072 6536	112.1 1.478 3989	65.96 1.726 5181	28.52 20.52 20.53	

	9	WING	B		B-9. C	B-9. CONTINUED MOMENTS, CASES		202-202-7	2-7	:
		11	75	13	14	15	16	17	18	19
Cuse					*	Just Bending Moment,	Moment, M <sub>X</sub>			
		¥S 83	₩3 119	WS 167	W3 209	WB 275	948 3¥	WB 380	भट्ट केक	WB 516
Case)	Ä No 1g Ioud	80620 1.423 3.923x106	71710 1.416 3.298x206	6076 1.393 2.609×106	50610 1,386 2,080x106	34030 1,361 1,318x106	20050 1.357 Blixit	1,420 1,420 ,599x136	5906 1,608 211x106	1345 1.034 .0533×106
202 Rigid	7. 18. Lond	\$8290 1,333	\$1700 1.308	44450 1.271	37650 1.245	26240 1.211 Same As Case	17250 1.164 202	12930	5137 1.137	1146
Stick	K° X ¥ Ford	87190 1.342	1.305	65720 1.285	54850 1.274	37070 1.243 Same As Case	22330 1.199 202	16420	1.420	1504
208-1	16 Lond	81220 1,338	72220 1.322	01160 1.297	50910 1,394	34220 1.336 1.6 As Case	201.10 1.456 202	1,561	59560 1.852	1364 2.185
206-2	No No Load	82090 1.367	73070 1.358	62000 1.335	51720 1.326	34850 1,315 7 An Cuse	20550 1.332 202	15010	6047 1.587	1376
202-3	36 Fond	82850 1.293	73740 1.275	62520 1.250	\$2110 1.253 500	35090 1.301 e An Chue	20650 1.426 202	15080	6099	1396 2.147
202-4	اد قو الم	79330 1,462 4,204x136	70520 1.4%2 3.638×106	59740 1.427 2.900×10 <sup>6</sup>	1,415 2,307×10 <sup>6</sup>	33490 1.405 1.500x10 <sup>6</sup>	19770 1,420 .950x106	14440 1.491 .659x106	\$828 1.704 .257x106	1330 1.957 .0656x106
308.5	No No Lond	79230 1.388	70'70 1.379	59770 1.356	1,343	33580 1.327 Some An Chne	15920 1.335	14580	5874 1.587	13% 1.811
9-202	X Xo 1g Load	80070 1, 395 3,64 3x106	11290 1, 385 3,068×106	60610 1.359 2.438×106	50630 1.344 1.952-106	34170 1,321 1,242x106	20420 1.311 .773×106	14990 1.371 .5708x106	6040 1.558 .2008alné	1374 1.782 .0504x106
208-6 Rigid	No. No. 1 E Lond	\$9680 1.258	53040	45740 1.203	38840 1.179 5.	27120 1.147 Cune An Cuse	17920 1,104 202-6	13450	5349 1.078	1,066
200-1		80120	71260	6.280 1.395	\$0300 1.383	33820 1. 467 Utere As Chor	19920 1,373 202	1,438	5869 1.629	1337
Rigid	₹° 16 £md	\$7860 1.309	51,310 1,287	14090 1.25.4	37350 1,235	26020 1 1.205 3,720 A: Chee 202	17100 1.168 202	12810 1.157	5089 1.143	11.132

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(d) WING BENDING MOMENTS, CASES 202-9-207-1

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e e					ding Bending Moments,	Moments, M				
		48 83	क्षा अ	VB 167	402 SM	WS 275	NS 346	NS 380	MS NA8	NS 516
202-9	No. 1g foed	81270 1.345	72350 1.342	61480 1.325	\$1340 1.313 Sa	34650 1.280	20660 1.211 208	15120	6091 1.373	1385
208-9 Nigid	X <sub>0</sub> 1⊈ Load	59580 1.178	\$2890 1.151	45520 1.116	38990 1.090	26920 1.056 1.056	17750 1.017	13310	.987 1987	911. 0070.
202-10	No No Load	90160 1.415 3.886x10 <sup>6</sup>	80060 1,406 3.277×106	67390 1.387 2.606x10 <sup>6</sup>	55850 1.380 2.706×106	37280 1.371 1.319×10 <sup>6</sup>	21160 1.396 .802x106	15260 1.474 .6004×106	6158 1.679 .212×106	1404 1.920 .0535×10€
202-10 Rigid	× 20.34	6.0890 1.3%	53820 1.335	45850 1.296	38610 1.268 Se	26750 1.232 As Case	17160 1,175 202-10	12760	5067 1.116	1.13
202-11	Ho 16 Load	102700 1.402 3.200x106	91390 1.391 2.570x106	77410 1.369 1.9162106	64460 1.360 1.448x106	4332) 1.345 8162106	25260 1. 43 .478x106	18360 1.128 3684106	74.08 1.592 106x106	1687 1.791 .0265×106
202-11 Rigid	No No Lond	69640 1.495	61720	\$2980 1.430	104.1 1.401	31220 1.365 ne As Case	20480 1.317 202-11	15140	6093	1359
308-12	K. K. 1g Zoud	70870 1.448 3.971×106	63010 1.441 3.386x10 <sup>6</sup>	53380 1.418 2.731×10 <sup>6</sup>	1,463 2,213×10 <sup>6</sup>	29880 1.377 1.44420	17630 1.351 .905x10 <sup>5</sup>	12900 1, koć 666kalo <sup>6</sup>	2805 1.598 24134106	1.888 1.888 06192106
202-12 Rigid	الا <sup>الا</sup> الا الا الا الا الا الا الا الا الا	51910 1.270	46070 1.245	39630	33590 1.181	23430 1.147 ne As Case	15400 1.101 202-12	11.066	1,594	1.065
202-13	No No Load	101900 1.353 5.194×106	89730 1,354 4,387×10 <sup>6</sup>	74690 1.336 3.471x10 <sup>6</sup>	61410 1.313 2.756x106	1.267 1.771×10 <sup>6</sup>	23430 1.214 1.082106	16990 1.264 .7792106	6884 1. 398 . 292×10 <sup>6</sup>	1572 1. 963 .07912106
207-1	A Ko	55020 1.761 1.2262106	1,793 3,672106	1.8310 3.0312106	34820 1.833 2.4932.06	23980 1.770 1.685x106	13850 1.687 1.079#106	10210 1.730 .7912106	11.970 1.970 .30£:206	969.3 2.252 .082±106

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	CASES 202-202-7
TABLE B-9. CONTINUED	WING TORSIONS AND WING SHEAR FLOWS. CASES 202-202-7

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		3.0	รา	22	23	24	25	56	27	28	જ	33	31	SX.
Care					gu <sub>1/1</sub>	Hing Torcione, PyEA	YZY					- Ving Chear Flovs	ar Flove	
		180 8 <b>3</b>	P. 119	19t :11s	VIS 209	VS 275	9મદ દ્યા	110 380	११४ व्या	316 31/	MC 83 Front Denm	VS 63 Rear Benn	IR 346 Front Beam	12 346 Rear Bena
200 (Ref Case)	Ig Ice	18470 2,842 -1,519x106	17460 2,968 -1,480x106	16410 3,090 1,429x106	15710 2.090 908x106	14180 2.261 8261106	13080 2,396 -,732×306	3026 1,303 270x106	1,96 1,328 -,186x106	511.5 1.557 101x106	6.109 2.127 61.79	2.152 3.930 -537.51	9.356 2.152 -177.14	2.431 3.258 -385.67
Negata Negata	A 1°, 1¢ Lond	8479 2.547	6586 2,999	11996 3.955	1.851	1479 2.344	2418 3.593 Sume	2850 1.153 As Case 202	1392	1,84,4	3.984	1.418 2.344	2.645	1.20
202 3tick Fixed	N X 16 Exad	18580 3.045	17540 3.185	16520 3, 323	15660 2.137	14,000 2, 345	12880 2, 496 Same A	3388 1.170 As Cace 202	1652 1.198	577.4 1.424	6.473 2.211	3,501	9.272 2.189	2.656 3.225
208-1	Le Fond	1%210 2.812	17190 2.931	16120 3.060	15570	14060 2.173	12940 2,303 Sume	3014 1.340 As Chie 202	1464	511.7	6.095 2.063	2.20k	9.348	2.377 3.232
206-2	7, 50 % S.	18700 2.719	17680 2.831	16580 2.954	15860 1.974	14280 2.150	13080 2,289 Same A	3100 1.302 As Cate 202	1505	32.36	6.203 2.131	2.162 3.767	3.371 2.044	3.191
206-3	1,5 € 7 × 10 × 10 × 10 × 10 × 10 × 10 × 10 ×	18530 2,674	17500 2.786	16400 2.907	15810 1.894	14220 2.055	13030 2.180 Same	3088 1.338 As Case 232	1,427	5.3.6 1.818	6.197 2.0°1	2,228 4,184	9.422	2.410 3.178
208-b	14 ° 5 ≥ 1 10 1 10 1	18040 2.848 -1.671×106	17030 2,975 -1,606x1.06	15980 3.113 -1.5112106	15420 2.124 -1.008x106	13900 2.299 892×106	12830 2.437 761×106	3045 1.312 318x106	14% 1.337 2092106	619 1.567 109×106	6.306 2.088 27.23	2.021 4.202 -555.44	9.762 2.166 -236.6	2.510 3.211 -359.0
208-5	A Load	17580 2.783	16530 2.913	15430 3.056	15070 2.045	13500	12380 7.377 Same A	3021 1,289 As Case 202	1,311	510.1	5.927 2.057	2.081 3.898	8.923 2.136	2.308 3.20%
9-202	No.	17680 2.960 -1.704#106	16730 3.084 -1.495x105	15780 3.207 -1.451x106	15190 2.133 903x135	13680 2, 317 815×1.06	12610 2.156 717x106	3105 1,254, -,277×106	1510 1.277 1892106	526.6 1.502 102×105	5.881 2.185 -52	2.2% 3.810 .494	9.028 2.191 -182	2.485 3.221 -373
202-6 #1 <b>g</b> 14	N° 1g Lond	7915 2.667	3.218	4059 4.341	6963 1.838	4282 3.399	3.850 3.850	2958 1,101 te Case 202-6	1,081	501.7	3.886	2.156	2.547	1.344
206-7	16 50 ≥1 50 ≥2	18320 2.827	17300 2.948	3.080	15530 2,068	13980 2.234	12960 2.367 Seme	3004 1.318 1s Case 202	1,345	507.9	2.03 200 200 200 200 200 200 200 200 200 2	2.151 3.970	9.22 2.126	3.258
208-7 Nigid	A No 14 Load	2.444	664.8 2.865	4590 3.750	7079 2.833	2.270	2451 3,443 8ene Ar	2835 1.163 ts Caur 202	1380 1.143	1,122	3.976 1.741	1.412 2.427	2.646 2.042	1.208 2.048

		Ξ	WING T	TORSI	TABLE B-9. CONTINUED ORSIONS AND WING SHEAR FLOWS.	TABLE B AND WINC	B-9. CC	CONTINUED EAR FLOWS	WS. CA	CASES 2	202-9-207-1	7-1		
L		20	23	82	23	77.2	25	%	27	88	8	2	٤	2
Case					Via.	- Ving Torstons, Myg.						- Wing She	Wing Shear Plove	
		WG 83	113 119	W3 167	NS 209	WS 275	948 3H	MS 380	844 EN	915 SW	VS 83 Pront Beam	WS 83 Sear Beam	VS 346 Fron. Bean	NS 346 Reer Bean
202-9	Xo 16 Loud	16640 2,822	15530 2 970	14380 3.131	11490 1.970	12820 2,175	11620 2, 345 See	3101 1.132 As Case 202	1506 1.146	522.5 1.325	5.864 2.074	2.036 3.443	8.627 2.098	2.1kg 3.0k6
202-9 Rigid	F Cord	9247 2.754	6389 3.331	294.1 1,462	7012 1.865	4365 2.510	2367 4,086 Same	2935 1,034 As Cane 202	1429	497.1 .981.3	3.971 1.766	2.461	2.591 2.218	1.36 8.330
202-10	No No	22.302 2.362 -1.3172106	21570 2, 164 -1,275x106	19980 2.597 -1.221x136	19140 1.880 830x106	17340 2.033 746x106	15890 2.172 652×106	3127 1.236 271x106	1517 1,254 1872106	527.2 1.503 108x106	7.431 1.949 -84	1.769	11.36 2.338	2.330 3.189
202-1J	No No Load	1.2960 2.282	11010 2.506	2.923	9270 1.847	6664 2.166	4493 2.763 Same	2841 1,163 As de @ 202-10		481.5	4.940 1.833	3.401	2.040	3.469
208-11	Xo 1€ Lond	22980 2.750 -2.267x106	21590 2.874 -2.1952106	20010 3.023 -2.081x106	19700 2.004 -1.495x1c6	17690 2.185 -1.342x106	16100 2.341. -1.1732106		1813 1.442 266x106	628.3 1.649 137×106	7.773 2.141 -29		11.75 2.084 - 798	2.715 3.444 513
202-11 Rigid	No Lond	11220 2.580	6921 2,954	6279 3.748	8835 1.970	5708 2.412	3.502 · Sene /	2	1653 1.283 11	575.0	4,976 1,976	1.559 2.840	3.320	2.338 3.338
202-12	76. 74 1€ Ioad	16600 2881 -1,2091106	15790 2.997 -1.190x100	14970 3.114 -1.1632106	14050 2.149 696x106	12740 2,300 645x106	11830 2.411 5854136	2678 1.277 208x106	1308 1,308 1484106	1,5% 1,5% 0832136	5.395 2.156 -81	3.858 1.65	8.36 2.164 -110	2.291 3.229
202-12 Rigid	n No	7159 2.451	5470 2.928	3628 3.971	6182 1.750	3839 2.243	1995 3.561	2556 1.087 18 Case 202-12	1245 1.068	433.5 1.047	3.472	2.176	2.2% 2.3%	1.121
20 <b>2-1</b> 3	No. No.	22790 2.333 -1.225x106	21550 2,409 -1,201x106	20150 2.512 -1.1681106	19120 1.980 7562106	17350 2.160 694x106	16020 2,320 6192106	3385 1.277 247×106	1666 1.311 1752106	581.9 1.506 0975x136	8.253 1.680	3.282	2.110	2.678 3.072
207-1	A No 1 <b>g</b> Lond	19190 3.757 582106	18720 3.819 •611x106	18250 3.869 6492106	2.870 2.870	11450 2.984 2954106	3.0% 3.0% 3.0%	21,52 1.574 0665x106	1058 1.707 0606x106	3%.6 2.154 .041x106	2.849	2.97' 1.048	6.553 ?.438	3.198

TABLE B-9. CONTINUED
(g) FUSELAGE LOADS, CASE 202-202-7

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A TANAMAN A

		(g)		FUSELAGE	E LOADS,		CASE 2	202-202-7	02-7		
		33	34	35	36	3.7	38	39	04	17	24
8					2	Puselage Loads	48 m				
		<b>*</b>	Ý	ຕຸ	*y	ω <b>#</b>	χ.	20	حج	8 8	×
		75 350	76 350	rs 500	FS 500	r8 571	ารรณ	FS 695	FG 695	rs 1006	FS 1006
202 (Ref Case)	X No 1g load	251.4 1.336 -10185	38410 1,299 -1,601×10 <sup>6</sup>	369.9 1,281 -16168	78990 .1, 339 .3,5191106	435.1 1.259 -19242	107500 1.3) ? .4.7762106	296.6 1.483 -21436	26400 3.564 7.308x106	3.722 3.722 -12836	24690 2.577 1.987×106
206 Rigid	Д 16 гова	224.9 1.962	29360 2.129	328.9 1.750	70490 1.966	395.0 1.644 Same As	95830 1,889 0ase 202	256.8	23910 4.948	61.86	26170 3.518
202 Sylck Flued	1. 50 M	66.74 1.334	39830 1.367	432.3 1.255	94450	501.8 1.224 Seen As	1.295 1.295 Case 20E	310.3	26130 3.199	3.418	1,359
208-1	X No 1g Loud	252.0	38560 1.341	371.0 1.309	79070 1.358	436.5 1.291 Sene As	107700 1.339 Case 2.0	299.1 1.613	3.737	3.639	2,416
206-2	X No 1g Load	253.4 1.308	38690 1.296	373.0 1.273	79530 1.313	438.9 1.259 Same As	106300 1.298 Case 202	299.6 1.190	25850 3.257	47.19 3.333	23770 2.135
208-3	X Ko 1g Iond	254,2 1,348	38840 1.337	374.3 1.315	79790 1.353	1.301 See As	108700 1.338 0ase 202	302#1 1.611	26740 3.517	47.17 3.330	23680 2.051
4-202	1. 1.0ہ	249.4 1.451 -10185	37950 1,311 -1,601×106	366.3 1.357 15168	78250 1.454 -3.5192106	1.30.5 1.30.5	106500 1.417 1.7768106	292.3 1.526 -21436	26920 3.961 7.3082106	-128% -128%	25450 2.980 1.987x106
20K-5	No.	249.2	381:.0 1.259	366.9	78220 1.322	431.7 1.234 See As	106600 1,298 Case 272	294.3 3.444	25740 3.556	30.04 3.670	24450 2.505
208-6	X, 1€ ford	274.1 1.319 -16248	39020 1.258 -203.14106	398.2 1.860 -26195	86020 1.322 -5.0952106	1.234 1.234 -27922	116600 1.299 -6.930x10 <sup>6</sup>	260.3 1.488 -23626	18920 5.205 6.886x106	73.86 2.963 -10681	29800 2.441 1.635#106
202-6 Rigid	A No le Load	249.1 1.904	35090 1.267	359.9 1.708	781.00 1.908	119.6 1.608 Same As	105700 1.838 Case 202-6	227.9 1.262	20750 6.193	3.841	30800
208-7	1, K. A. Iond	250.5 1.36	38120 1.265	368.3	78630 1.364	433.0 1,259	107130 1,336 Case 202	294.5 1.475	26920 3.666	3.943	24740
202-7 Rigia	14 To 15 A	2.006 2.006	33780 1.282	327.5 1.777	70340 2,082	384.1 1,655 State At C	95550 1.935 Case 202	275.1 1.272	24940 4.911	64.07 4.778	267.10 3.749

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		3	FUS	TARIE FUSELAGE	E B-9. C	DS. C	CONCLUDED (CASES 202-9-207-1	DED 202-	9-207-	<b>–</b>	
		33	34	55	92	37	gg.	33	01	1,1	Ŋ
3							Puseinge Lo	Loads -			
		รีร	Ý	S <sub>s</sub>	¥,	G XI	₹,	8	Ý	ω <sup>84</sup>	<b>م</b> ري
		FC 350	FS 350	F8 500	75 500	ro 571	FB 572	FS 695	173 695	rs 1006	rs 1006
5.08-9 303	A No Lg Load	235.0 2.367	38850 1.248	375.0 1.292	80010 1.369	1,260 3,260 Same As	109000 1.340 Case 202	301.6 1.366	3.261	3.917	24090 2.580
202-9 Rigit	26 Ko	729.8 1.997	34580 1,308	335.2 1.723	72010 1.998	393.0 1.589 Same As	97810 1,900 Chee 202	262.8 1.302	25920 5.356	64.78 5.385	27490 4.208
20:-10	No No Is Load	270.6 1.362 -15812	40950 1.336 -1.965#106	397.6 1.313 -?3542	84970 1.365 -4.946x106	1.294 1.294 -26720	11.345 1.345 -6.7312106	319.9 1.487 -19751	29250 3.266 4.6722106	47.67 4.036 -5955	2.673 2.673 752×106
202-10 Elgid	% № 18 ford	241.7 1.994	35010 1.347	338.8 1.781	72640 1.998	397.6 1.675 See As	98730 1.921 Case 202-10	263.8 1.314	26280 4.726	61.38 4.873	3.650
20g-11	No 1€ Load	305.1 1.394 -15569	47070 1.363 -1.926×10€	450.1 1.353 -23180	95790 1.398 -4.363x106	530.1 1.336 -26300	130600 1.381 -5.620x106	373.7 1.508 -19391	33650 2.880 4.593x106	49.83 3.604 -5858	27380 2.268 747476
202-11 Rigid	X No le Lond	26410 2.251	344.5	387.1 1.986	82800 2.255	1.856 1.856 Same As	112600 2,159 Case 202-11	315.0 1.491	31070 5. læ7	71.16 5.740	30810 4. 313
208-12	A No 16 Lond	221.5 1.493 -15866	34120 1.238 -1.4732106	325.8 1.363 -23622	69520 1,495 -4,965x106	383.3 1.305 -26813	94660 1.446 -6.755×106	763.9 1.449 -19844	25080 3.949 4.6892106	53.66 3.956 -5977	2.954 2.954 7533106
202-12 Nig1d	No No 18 Lend	197.8 1.915	30420 1.225	290.1 1.699	62000	3h1.1 1.591 Same As	84360 1.841 Case 20:-12	230.4 1.210	21290 1.732	%.3 %.8	23940 3.237
202-13	A No 1g Lond	246.5	36660 1.147	360.6 1.386	77350	1.321	105100 1.475	264.8 1.349	£1580 4.628	63.88 3.477	26670 2.573
20f-1	A No 1g Load	139.2 2.179	22.330 2.376	217.8 1.772	48120 2,168	259.1 1.581	64870 2.035	146.0 1.913	1,0000 1,271	88.65 4.032	3.591

#### APPENDIX C

# APPLICATION OF THE MATCHING CONDITION TECHNIQUE TO THE MODEL 188 WING

In order to provide a detailed illustration of the application of the principles discussed in Sections 11-1 and 11-2, a set of enveloping design conditions is now generated for the Model 188 wing. These conditions match the loads defined statistically by the mission analysis approach, at an arbitrary frequency of exceedance approximating the limit-strength value. Generation of enveloping conditions to match design envelope, rather than mission analysis, loads would be quite similar. However, as indicated in Section 11.1, matching the mission analysis loads provides a somewhat more severe test of the method, as it brings in problems that do not arise in matching design envelope loads.

The loads generated in this section also provide the basis for extensive stress analysis, which leads to a more exact determination of the value of N(y) corresponding to limit strength of the Model 188 wing. This determination is described in Appendix E, which also makes further use of the results of the stress analysis to indicate an ultimate-strength N(y) value and limit and ultimate strength values of  $\sigma_{\rm w}\eta_{\rm d}$ 

It should be emphasized that the detailed procedure described in the following paragraphs is illustrative only. Wide variations in the specific approach are to be expected, depending upon the degree of conservat'sm acceptable and the specific airplane being treated. In attempting to follow the details of the work for the Model 188, the reader should not lose sight of the basically simple concepts described in Sections 10, 11.1, and 11.2, which will apply under any circumstances.

# C.1 Nomenclature

The following nomenclature is used in this Appendix:

Ratio of root-mean-square load to root-mean-square gust velocity

C<sub>T.a</sub> Lift curve slope per radian

C<sub>Ma</sub> Moment curve slope per radian

E<sub>1</sub> Elementary distribution for static mode

E<sub>2</sub> Elementary distribution for dynamic bending mode

<b>E</b> 3	Elementary distribution for dynamic torsion mode
Ē	Ratio of load in static mode elementary distribution to statistically defined load
<b>E</b> <sub>2</sub>	Ratio of load in dynamic bending mode elementary distribution to statistically defined load
<b>E</b> <sub>3</sub>	Ratio of load in dynamic torsion mode elementary distri- bution to statistically defined load
K <sub>GN</sub>	Unsteady aerodynamic function due to gu t on nacelle - i.e., lift at given frequency divided by lift at zero frequency
K <sub>GW</sub>	Unsteady aerodynamic function du∈ to gust on wing - i.e., lift at given frequency divided by lift at zero frequency
K <sub>IN</sub>	Unsteady aerodynamic function due to a unit change in angle-of-attack on the nacelle - i.e., lift at given frequency divided by lift at zero frequency
XIM	Unsteady aerodynamic function due to a unit change in angle-of-attack on the wing - i.e., lift at given frequency divided by lift at zero frequency
L	Any load; subscript S denotes statistically defined design-level value; subscript D denotes a design condition value
N <sub>o</sub>	Average number of zero crossings with positive slope for rms load quantity
$M_{\mathbf{X}}$	Wing bending moment (inlb.)
My	Wing torsion moment (inlb.)
S	Aerodynamic reference area (ft. <sup>2</sup> )
$\mathbf{s_z}$	Wing shear (lb.)
T	Transfer function
V	Airplane forward velocity (in./sec.)
W	Gust velocity (in./sec.)

Xnac	Generalized coordinate of nacelle elastic plunge deflection relative to the wing (chords)
z <sub>o</sub>	Generalized coordinate of fuselage plunge displacement (chords)
Z	Vertical translation of any point on the wing relative to the fuselage (in.)
al	Loading coefficient for elementary distribution $\mathbf{E}_{\mathbf{l}}$
a <sub>2</sub>	Loading coefficient for elementary distribution E2
a <sub>3</sub>	Loading coefficient for elementary distribution E3
C	Chord (in.)
ट	Mean aerodynamic chord (in.)
f	Frequency (cps)
g	Acceleration of gravity (386 in./sec.2)
i	√-1
$\boldsymbol{l}_{\mathbf{x}}$	Location of mass item relative to wing elastic axis (in.)
n <sub>z</sub>	Load factor (g's)
nzc.g.	C.G. load factor (g's)
nzbal.	Rigid body load factor required to maintain balance in the dynamic elastic modes (g's)
p	Laplace operator
P	Free-stream dynamic pressure in psf, or beam shear flow in pounds per inch
x	Denotes in general a length in the chordwise direction (in.)
У	Denotes in general a length in the spanwise direction (in.)
$\theta_{\text{nac.}}$	Generalized coordinate of nacelle elastic pitch rotation relative to wing at nacelle (rad.)

R <b>X</b> T	Summation over the wing span from the tip to the root
<b>•</b> o	Generalized coordinate of fuselage pitch rotation (rad.)
<b>∳y</b>	Output power spectral density for quantity y
Ω	Forcing frequency (rad./chord)
a	Aerodynamic angle-of-attack (rad.)
$oldsymbol{\delta_{B_{ij}}}$	Wing bending influence coefficient (in./lb.)
$oldsymbol{\delta_{T_{i,i}}}$	Wing torsion influence coefficient (rad./inlb.)
<b>p</b>	Wing twist elastic deflection (rad.)
Subscripts:	
A	Airload
EA	Wing elastic axis
FB	Wing front beam
I	Inertia load
AI	Arbitrary load axis to which wing loads are referred
RB	Wing rear beam
N or NAC	Nacelle
W	Wing
i	General location of the wing
j	Designation of nacelles
Matrices:	
	Square matrix
	Diagonal matrix

The second secon

Column matrix

Matrix multiplication

Dots are used to denote the derivatives of a quantity with respect to time.

A quantity preceded by a  $\Delta$  denotes that the quantity is the increment for that particular wing panel.

denotes the modulus of a complex quantity.

## C.:. Preliminary Considerations

The intermination of design load conditions divides naturally into two distance parts. In the first, several "elementary" or "unit" distributions are developed. In the second, these are used as building blocks to generate one or more design load conditions, such as to match or envelope closely the statistically defined loads resulting from the power-spectral analysis.

Before embarking upon the generation of the elementary distributions, it is necessary to decide which mission segment or segments these should be based upon and determine what modes should be used as a basis. Consciplently, it is pertinent to look at some results of the power-spectral analysis.

The loads obtained from the Model 188 mission analysis are shear, bending moment, and torsion at wing stations 83, 119, 167, 209, 275, 346, 380, 448, and 516, and front and rear beam shear flows at wing stations 83 and 346. (The nacelle locations are wing stations 188 and 359.) Values of these loads are read from the frequency-of-exceedance curves at a frequency of exceedance of 10<sup>-5</sup> cycles per hour. The actual frequency of exceedance value to be used for design of a new airplane had yet to be established at this stage of the analysis, but the value selected here is the right order of magnitude and hence will be satisfactory to illustrate the method. Later work, described in Appendix E, indicates this to be quite close to the actual limit strength value for the Electra.

A typical frequency of exceedance curve - for bending moment at wing station 119 - was shown in Figure 9-9(b). It is seen that the bending moment at  $10^{-5}$  cycles per hour is 12.1 million inch-pounds. It is apparent from the figure that mission analysis case 202 is the major contributor to the total bending moment. Similarly, it was established that case 202 is a major contributor to all of the other load quantities,

except for torsions in the outer wing. Outer wing torsions are produced predominantly by mission analysis case 201.

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Loads for the total mission, and separately for mission analysis cases 201 and 202, are summarized in Table C-1, at the frequency of exceedance of 10<sup>-5</sup> cycles per hour. In Table C-1, loads for the total mission are shown in column 3; loads due to mission analysis case 201 alone and 202 alone, at the same frequency of exceedance per hour of total flight, appear as columns 4 and 5 respectively. One-g loads for mission analysis cases 201 and 202 are shown as columns 6 and 7. The resulting "gust incremental" loads are shown in columns 8 through 11. In columns 8 and 10, the gust increment is taken as the difference between the net load based on all mission segments and the one-g load for the segment indicated. In columns 9 and 11, the gust increment is the increment for the given mission segment a ne. Columns 12 and 13 show, based on mission segments 201 and 202 respectively, the ratio of gust increment due to the given segment alone to the total gust increment based on all segments.

In column 13, the ratios for shear, bending moment, and beam shear flow are all approximately .90. Ignoring for the present the wing torsions, the following conclusions can be drawn. First, if design conditions were to be generated to match the gust incremental loads for condition 202 alone (column 11), these could then be "ratioed up" by dividing by .90 and would closely reproduce the column 10 incremental loads. Then, if the condition 202 one-g loads were to be added, a match to the net loads of column 3 would result. Thus, to obtain a match to the statistically defined net loads, only the gust increment need be considered, and this can be confined to condition 202.

Now let us examine the torsions. Over the region from the fuselage to the inboard nacelle, the ratio in column 13 is approximately .80; between nacelles it is approximately .85. Since these ratios are not far below the .90 ratio for the other load quantities, use of case 202 on an incremental basis should also give a fair representation of the torsions from the fuselage to theoutboard nacelle. For outer wing torsion, case 202 gives a poor representation of the total for the mission; consequently, it is necessary to use mission analysis case 201. Here, however, the cause is primarily the large difference in one-g flight torsion, rather than a difference in gust incremental torsion. Consequently, incremental torsions based on case 202 can be expected to be satisfactory even in the outer wing, if combined with the one-g loads for case 201.

As a result of the foregoing considerations, it is concluded that gust incremental loads for the total mission may be obtained by utilizing elementary distributions derived from a consideration of mission analysis case 202 only. These will then be added to case 201 or case 202 one-g loads as appropriate.

TABLE C-1. MISSION ANALYSIS LOADS AT N(y) = 10<sup>-5</sup> CYCLES PER HOUR, MODEL 188

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Э	0	9	9	6	9	0	0	0	9	<b>(2)</b>	0	0
Load	K.8. In:	Net Loads Mission Analysis	Wet Loads Case 201	Net Loads Case 202	One-G Losé. Case 201	One-G Load Case 202	(Net Hise.) -(1-g 201) (3 - (6)	(102 9-1)- (102 9-1)- (101 101)	(Net 112.8.) -(1-g 202) (3 - @	(Net 202) -(1-£ 202) © - ©	Ratio Case 201 ( / (	Ratio Case 202 (D) / (G)
28	83 77.	1,9200 1,6700	39400 33000 33000	00E47 00F47 007L7	15773	19055 16386 11869	33427 32459 28821	19627 18759	30145 30314 27038	28345 27914 25338	.587 878.	9 <del>4</del> 6.
Mine	£8473	287622 287622 28700 27700 16200	20000 21000 213000 21300 21300 21300 21300	24 24 24 24 24 24 24 24 24 24 24 24 24 2	28.59 6.99 7.98.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.5 7.88.	1337 2330 1516 1511	33937 28902 21913 18443 10815 4363	26637 18422 14213 12243 7315 3113	23400 23400 23400 23400 12033 12033	30,53,5 26,811 20,800 17721 10,539 4,569	66. 64. 64. 64. 64. 64. 64. 64. 64. 64.	ġġ <b>ġ</b> ġġġġ
10-by, Wing Wing Memor Mount Electic Age	2007-1-03 2007-1-03 2004-1	13.80 10.10 10.10 13.50 14.50 19.68 19.68	10.80 9.03 1.95 1.95 1.96 1.96 1.98	યા સ્થાપન સ્વાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્થાપન સ્યાપન સ સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ સ્યાપન સ સ્યાપન સ સ સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ્યાપન સ સ સ સ સ સ સ સ સ સ સ સ સ સ સ સ સ સ સ	4.3.5.5.4. 4.3.5.7.6.1. 4.0.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.	3.98 3.98 3.98 3.98 3.98 3.11 3.98 3.11 3.11 3.11 3.11 3.11 3.11 3.11 3.1	9 66 8.57 5.69 3.88 3.188 1.65 1.15	6.056 5.446 3.3724 2.552 2.523 1.103 1.006	9.877 8.877 7.491 7.491 2.493 2.499 1.841 1.756	9.027 7.952 6.741 5.570 3.732 2.239 1.601 .6806		2.36.25.25.25.25.25.25.25.25.25.25.25.25.25.
10-54, Wine Porsion Porsion Mout Electic Axis	113 167- 209 209 200 300 300 300 300 300 300 300 300 300	1.130 1.080 1.280 1.280 1.070 1.070 1.033	980 976 1,000 1,995 1,76 1,76 1,000	600 000 000 000 000 000 000 000 000 000	. 547 . 547 . 547 . 233 . 236 . 053 . 053	11.519 11.429 11.429 1908 1826 1732 1732 186	1.688 1.557 1.433 1.433 1.368 1.368 1.35 039	1.476 1.407 1.332 1.273 1.166 1.093 1.228 1.13	2.649 2.329 2.329 1.966 1.966 1.83 4.53	2.089 1.980 1.869 1.656 1.565 1.562 1.310	908 408 898 873 879 970 978	.789 .792 .834 .842 .846 .856 .728
G Nem Shear 710v	83 83 83 84 84 84 84 84 84 84 84 84 84 84 84 84	995 -785 1086 -690	28 87. <del>1</del>	₹. 8% 8%	158 -305 20 -247	62 -538 -177 -389	663 1060 1060 1443	¥€3 -227 770 -200	753 -247 1257 -301	683 -237 1097 -281	.698 .724 .726 .124	

It will be observed that the net load levels obtained from the mission analysis depend primarily on the rms or A values, which in turn depend upon the total area under each output power spectral density curve. However, in establishing distributions of loads that might actually occur at particular instants of time, consideration must be given to the shapes of the output power spectral density diagrams.

The output power spectral densities of shear, bending moment, torsion, and front and rear beam shear flow at wing station 83 and 346 were shown in Figure 9-3. It is evident that there are three peaks in the power spectral density plots: the first, at approximately .4 cps, is associated with the short period mode; the second, at 2.1 cp., is due to the first coupled wing bending mode; and the third, at 4.4 cps, is due to the first coupled wing torsion mode. It is also apparent that the relative contributions of the three modes differ from one load quantity to another for example, as between chear, moment, and torsion at any one wing station, and also, from one wing station to another.

For example, consider first the shear and torsion power spectral density of Figure 9-3(a). The 2.1 cps mode contributes about 1/3 of the total area for shear, but about 3/4 of the total area for torsion. Consider now the shear power-spectral densities of Figures 9-3(a) and (b). In Figure 9-3(a), the 2.1 cps mode contributes about 1/3 of the total area while in Figure 9-3(b) it contributes approximately 2/3 of the total area. The significant conclusions to be reached at this point is that since there are three dominant peaks in the power-spectral densities, it will be necessary to derive three elementary distributions - one corresponding to each of the peaks.

In order to provide a more complete picture of the various power spectral densities, a summary of the relative peak values of the power-spectral densities for all load quantities is shown in Table C-2.

In connection with the power-spectral density information presented in Figure 9-3 and Table C-2, some additional observations are pertinent in anticipation of developing the several elementary distributions. First, it becomes apparent that all loads outboard of the outboard nacelle are predominantly static in nature - i.e., dynamic effects are so small that they are negligible. For the region just inboard of the outboard nacelle shear and torsion are predominantly dynamic and are due to the 2.1 cps mode; bending moment in this region, on the other hand, is predominantly static. Just outboard of the inboard nacelle and between the inboard nacelle and the fuselage, shear and torsion exhibit a somewhat less pronounced dynamic effect, and dynamic effects in the bending moment are no longer small. In general, dynamic effects are more pronounced for torsion than for shear or bending.

TABLE C-2. POWER SPECTRAL DENSITY FUNCTION PEAKS, MODEL 188 CASE 202

1	@	3	<b>(</b> b)	<b>③</b>
Load	w.s	<b>©</b> y f = .4 cps	•y f = 2.1 cps	<b>•</b> y <b>f</b> = 4.4 cps
10 <sup>-4</sup> S <sub>z</sub>	83	48.45	33-25	.5066
	119	4314	<b>38.</b> <i>2</i> 2	.5987
	167	24.91	39.90	.6707
	209	53.00	41.80	1.661
Wing	275	35-37	37.87	.9835
Shear	346	15.33	28.83	.4423
	380	29.10	3.150	.1271
	448	9.901	1.189	.06636
	516	1.647	.2681	.02866
10 <sup>-8</sup> M	83	485.9	354.9	8.776
	119	385.6	278.7	7.284
bing	167	285.6	187.6	5-373
Bending	209	205.2	121.3	3.517
Moment	275	99.98	47.04	1.283
About	346	42.09	7.646	.3142
Elastic	380	23.48	2.874	.1676
Axis	<b>448</b>	3 <b>-7</b> 73	.5221	• 04092
	516	.1904	.03099	.003313
10 <sup>-8</sup> My	83	7.865	27.78	4.103
	119	4.507	27.36	3.958
Wing	167	1.617	26.53	3-779
Torsion	209	6.888	25.01	.8719
Moment	275	2.889	23.48	.7431
About	346	-7749	21.96	.6236
Elastic	380	1.072	.01761	.02532
Axis	448	.2601	.002732	.007162
	516	.03164	.0001018	.001413

## C.3 Elementary Distributions

It is now possible to proceed to the generation of the elementary distributions.

Basically, the elementary distributions will consist of one or more static distributions together with one or more distributions associated with dynamic overtravel in each elastic mode.

The static distribution consists of the incremental loads associated with gust encounter on a static aeroelastic basis - i.e., static aeroelastic wing twist is accounted for, but forces due to accelerations and velocities in the elastic modes are not considered. This distribution could be obtained by the usual static loads methods. However, for the Model 188 it was considered more convenient to start from scratch utilizing low frequency results from the dynamic analysis. This approach also ensured combining the right magnitude of inertia forces with the aerodynamic forces, since the inertia forces depend upon how the tail and fuse-lage forces phase with the wing air loads.

The elastic-mode distributions can be obtained fairly directly when natural modes are used as generalized coordinates in the dynamic analysis. It is required only to obtain the inertia and aerodynamic forces associated with oscillations at the natural frequency of the mode. However, the dynamic analysis of the Model 188 utilized elementary deflection shapes, rather than natural modes, as generalized coordinates. Consequently, for the Model 188, the natural mode shapes are approximated based upon inertia and aerodynamic forces obtained from the dynamic analysis at the respective resonant frequencies.

The solution for the elementary distributions are to a certain extent arbitrary and need be only approximations to the actual distributions of loads in the modes. It is highly desirable, however, that the elementary distributions be fairly good approximations to the actual load distributions in order that the resulting design loads be realistic. It is the intent herein to define a method that is basically simple yet yields realistic loads.

Looking ahead briefly, the procedure for determining the elementary distributions, both static and dynamic, can be summarized as follows:

1. At the appropriate resonant frequency (or, in the case of the static distribution, at any frequency well below the first elastic mode frequency), obtain the wing loads from the dynamic analysis. These are simply values of the appropriate transfer functions. Retain real and imaginary parts.

- 2. Use these to compute the mode shape. Retain real and imaginary parts.
- 3. Bas d on this mode shape, obtain panel aerodynamic and inertia forces. Retain real and imaginary parts.
- 4. Take either the modulus of these panel loads (with sign that best approximates the actual phasing) or the component in phase with some appropriate single load quantity. Integrate spanwise to obtain shears, bending moments, and torsions. This constitutes the elementary distribution.

In carrying out this precedure, the first step required is to define a reasonable spanwise distribution of unit airloads  $(\Delta S_{ZA}/a_1)$  and  $\Delta M_{YA}/a_1$ . In addition to this, the spanwise distribution of pertinent unit inertia data  $(S_Z/n_Z, M_Y/n_Z)$ , etc.) and the matrix of wing bending and torsional influence coefficients must also be defined. All other necessary data may be obtained from the transfer functions used in obtaining the output power spectral densities and subsequently the  $\overline{A}$  and  $\overline{M}_O$  values.

The static-mode elementary distribution is considered first. For the static mode it will be assumed that velocities and accelerations in the elastic modes are negligible. It is not necessary that the static-mode elementary distribution be defined at the airplane thort period frequency; in fact, it is desirable to define the loads at a lower frequency, say about .05 to .10 cps, to ensure that dynamic effects are, in fact, negligible. The determination of the static-mode elementary distribution is as follows:

- 1. Obtain the complex quantities  $Z_0$ ,  $\Phi_0$ ,  $n_{Zcg}$ , and  $M_{yi}$ ; these are simply values of the corresponding transfer functions.
- 2. Define the complex unsteady aerodynamic functions  $K_{\text{GW}}$ ,  $K_{\text{IW}}$ ,  $K_{\text{GN}}$ , and  $K_{\text{IN}}$ .
- 3. Compute the complex root angle-of-attack.

$$\alpha_{\text{Root}} = K_{\text{GW}} \frac{W}{U} + K_{\text{LW}} (\phi_{\text{O}} - i\Omega Z_{\text{O}})$$

- 4. Verify that  $a_{\rm ROOt}$ ,  $\theta_{\rm nac.}$ , and  $M_{\rm Yi}$  are nearly in phase or nearly 180° out of phase relative to  $n_{\rm Zcg}$ . (This condition normally will be met, at the low frequencies specified.)
- 5. Convert all quantities to a load per "g" basis by dividing the modulus of the quantity by the modulus of c.g. load factor.

6. Compute the local aerodynamic angle of attack acting at each wing panel:

$$(a/n_z)_i = (a_{Root}/n_z) + (\Delta a_{Twist}/n_z)_i$$

where

$$\left\{ \left( \Delta a_{\text{Twist}} / n_{z} \right)_{i} \right\} = \left[ \delta_{T_{i,j}} \right] * \left\{ \left( \Delta | T_{M_{y_{i}}} | / | T_{n_{Z_{cg}}} | \right) \right\}$$

(Note that the unsteady aerodynamic effects are neglected in evaluating  $\Delta a_{twist}$ ; this is valid only if  $|K_{IW}| = 1.0$ .)

7. Compute the local aerodynamic angle of attack for each nacelle:

$$(a/n_z)_j = (a_{Root}/n_z) \div (\Delta a_{Twist}/n_z)_j + (\theta_{Nac}/n_z)_j$$

(Note that the unsteady aerodynamic effects are neglected in evaluating  $\theta_{\rm Nac}$ ; this is valid only if  $|K_{\rm LN}| \approx 1.0$ .)

- 8. Plot  $(\alpha/n_z)_i$  and  $(\alpha/n_z)_j$  versus wing station.
- 9. Obtain the static-mode elementary distribution

$$S_{z_{i}} = \sum_{T}^{R} \left( \frac{\Delta S_{z_{A}}}{\alpha} \right)_{i} * \left( \frac{\alpha}{n_{z}} \right)_{i,j} + \sum_{T}^{R} \left( \frac{\Delta S_{z}}{n_{z}} \right)_{i} * (-1.0)$$

$$M_{x_i} = \sum_{T}^{R} s_{z_i} (\Delta y_i)$$

$$M_{y_{i}} = \sum_{T}^{R} \left( \frac{\Delta M_{y_{A}}}{a} \right)_{i} * \left( \frac{a}{n_{z}} \right)_{i,j} + \sum_{T}^{R} \left( \frac{\Delta M_{y_{I}}}{n_{a}} \right)_{i} * (-1.0)$$

It should be noted that the wing stations at which loads must be defined for stress analysis purposes are different in

location and number from those at which loads are obtained in the power-spectral analysis. This step is a convenient point at which to go to these more closely spaced stations.

Next, consideration is given to the calculation of the dynamic-mode distributions. In obtaining these distributions, the loads due to gust velocity, and body pitch, and rigid body plunge are not considered, since the are included in the static-mode elementary distribution. In other which the loads to be computed are to be those associated only with the dynamic overtravel in the modes. In obtaining the dynamic mode elementary distributions, it is necessary to utilize values of the transfer functions at the actual peak-response frequencie. The determination is as follows:

- 1. Obtain the complex quantities  $\Delta S_{z_i}$ ,  $\Delta M_{y_i}$ ,  $\theta_{nac.}$ , and  $X_{nac.}$ ; these are simply values of the corresponding transfer functions.
- 2. Define the complex unsteady aerodynamic functions KIN and KIN.
- 3. Compute the complex wing rotation  $(\phi_i)$  and complex wing deflection  $(Z_i)$  relative to the fuselage.

$$\begin{cases} \phi_{i} \\ \end{cases} = \begin{bmatrix} \delta_{T_{i,j}} \\ \end{cases} * \begin{cases} \Delta M_{y_{i}} \\ \end{cases}$$
$$\begin{cases} Z_{i} \\ \end{cases} = \begin{bmatrix} \delta_{B_{i,j}} \\ \end{cases} * \begin{cases} \Delta S_{Z_{i}} \\ \end{cases}$$

4. Compute the local complex aerodynamic angle of attack.

Wing

$$\left\{\alpha_{i}\right\} = K_{IM} * \left(\left\{\phi_{i}\right\} - \frac{i\Omega}{c}\left\{Z_{i}\right\}\right)$$

Nacelles

$$\left\{\alpha_{i}\right\} = K_{LN} * \left(\left\{\phi_{i}\right\} + \left\{\theta_{nac}\right\} - \frac{i\Omega}{c}\left\{Z_{i}\right\} - i\Omega\left\{X_{nac}\right\}\right)$$

(Note that the effect of  $\phi_i$  on vertical velocity is neglected, since it is small.)

## Wing

$$\left\{n_{z_i}\right\} = -\frac{p^2V^2}{gc^2} \left(\left\{z_i\right\} + \left[\mathcal{L}_{x_{\text{wing}}}\right] * \left\{\phi_i\right\}\right)$$

#### Nacelles

$$\left\{n_{z_{i}}\right\} = -\frac{p^{2}v^{2}}{g\overline{c}^{2}}\left(\left\{z_{i}\right\} + \left[\mathcal{L}_{x_{nac}}\right] * \left\{\phi_{i}\right\} + \overline{c}\left\{x_{nac}\right\}\right)$$

6. If mass items are present that have relatively large pitching moments of inertia, compute the local complex pitching

#### Wing

$$\left\{ \stackrel{\cdot \cdot \cdot}{\phi} \right\} = -\frac{p^2 V^2}{\bar{c}^2} \left\{ \phi_1 \right\}$$

#### Nacelles

$$\left\{ \boldsymbol{\dot{\varphi}} \right\} = -\frac{p^2 V^2}{c^2} \left( \left\{ \boldsymbol{\phi}_1 \right\} + \left\{ \boldsymbol{\theta}_{\text{nac}} \right\} \right)$$

- 7. Obtain the modulus of  $\alpha_i$ ,  $\beta_i$ ,  $\alpha_{2i}$ ,  $\beta_i$ ,  $\beta_i$  and  $\beta_i$ . Check to see that the quantities are relatively in or out of phase, and plot the modulus vs wing station, using the appropriate sign.
- 8. Solve for the rigid body load factor required to keep the mode in balance i.e., make the summation of vertical forces equal to zero. (It is assumed that "balancing" the mode does not change the aerodynamic angle-of-attack. It is also assumed that, owing to the extremely large pitching inertia of the fuselage, modal balance in pitch is not required.)

$$\frac{-\sum_{\mathbf{T}}^{\mathbf{R}} \left(\frac{\Delta \mathbf{S}_{\mathbf{Z}_{\mathbf{A}}}}{\boldsymbol{\alpha}}\right)_{i,j} * \boldsymbol{\alpha}_{i,j} - \sum_{\mathbf{T}}^{\mathbf{R}} \left(\frac{\Delta \mathbf{W}}{\mathbf{n}_{\mathbf{Z}}}\right)_{i,j} * \mathbf{n}_{\mathbf{Z}_{i,j}}}{1/2 \text{ gross weight}}$$

9. Obtain new spanwise load factor distribution.

$${n_{z_i}}_{adjusted} = n_{z_{balance}} * {1.00} + {n_{z_i}}$$

10. Obtain the dynamic mode elementary distribution.

$$S_{z_{i}} = \sum_{T}^{R} \left(\frac{\Delta S_{ZA}}{\alpha}\right)_{i,j} * (\alpha_{i,j}) + \sum_{T}^{R} \left(\frac{\Delta S_{Z}}{n_{z}}\right)_{i,j} * (n_{z_{i,j}})_{adjusted}$$

$$M_{z_{i}} = \sum_{T}^{R} S_{z_{i}} (\Delta y_{i})$$

$$M_{y_{i}} = \sum_{T}^{R} \left(\frac{\Delta M_{yA}}{\alpha}\right)_{i,j} * (\alpha_{i,j}) + \sum_{T}^{R} \left(\frac{\Delta M_{yT}}{n_{z}}\right)_{i,j} * (n_{z_{i,j}})_{adjusted}$$

$$+ \sum_{T}^{R} \left(\frac{M_{U}}{\theta}\right)_{i,j} * (\phi \text{ or } \theta_{j})$$

As in the determination of the static-mode elementary distribution, this is a convenient point at which to go to the more closely spaced wing stations at which loads must be defined for use in the stress analysis.

The arbitrary elementary distributions for the Model 188 are now determined, following the procedure outlined in the above discussion. As indicated earlier, mission analysis case 202 is the major contributor to the wing loads and will be used in deriving the elementary distributions.

The required unit airload distributions are presented in Table C-3. In column 2 is shown the spanwise distribution of "additional" airload for the rigid wing, as used in static loads determinations. Column 3 gives the incremental airloads acting at each panel, and column 4 refers airloads to local panel angle of attack. Column 5 gives the nacelle airload shears, and column 6, the combined wing-nacelle airload shears.

TABLE C-3. UNIT AIR! OAD DISTRIBUTIONS MODEL 188 CASE 202

<b>(1)</b>	@	3	<b>©</b>	<b>③</b>	6	The state of the	8	9
V.8.	S <sub>2</sub>	<b>∆</b> 8 <sub>3</sub>	Δs <sub>z</sub> AN	∆ 8 <sub>8</sub>	ΔB <sub>B</sub> A	x,	10 <sup>-6</sup> N <sub>Y</sub> IA RAC	10-6M <sup>k</sup> IV
#.5.	C 4 2	C <sub>2</sub> q 8/2	α <sub>1</sub>	αı	α,	(in.)	α <sub>i</sub>	ai
	Given	(C) - (C)+1	846550(3)	*	<b>(</b> } + (6)	1C <sub>1</sub> ***	Below	10 <sup>-6</sup> 697 +8
0	1,000	.138	116850	0	116820	-22.70	0	-2.652
65	.862	•075	63 <del>49</del> 0	0	63 <b>1</b> 90	-21.21	0	-1.347
101	-787	.078	66030	0	66030	-20, 39	0	-1.346
137	.709	.067	56720	0	56720	-19.55	0	-1.110
167	.642	0	0	0	0	0	0	0
167	.642	0	0	25110	25110	0	3.700	3.700
167+	.642	.022	18620	-14530	4090	-18,88	0	077
179	.620	•031	26240	-20480	5760	-18,60	O	107
197	.589	.023	19470	-15200	<b>4270</b>	-18,19	0	078
209	.566	0	0	0	0	0	0	0
2091	.566	e	0	25110	25110	0	3.700	3.700
209 <sup>+</sup>	•566	.065	55030	0	55030	-17.91	0	- <b>.</b> 985
239	.501	.074	62650	0	62650	-17.23	0	-1.079
275	.427	.037	31,320	0	33,320	-16.40	0	514
293	.390	075	63490	0	63490	-15.99	0	-1.015
329	.315	.030	25 <b>4</b> 00	0	25400	-15.17	0	385
346	.265	0	0	0	0	0	0	0
3 <b>\6</b> "M	.285	0	0	31.300	31300	0	4.339	<b>4.339</b>
3 <b>\</b> 6 <sup>+</sup>	<b>.</b> 285	.033	27940	-50680	-22740	-14,78	0	.336
38o <sup>-</sup>	.252	0	0	0	0	0	0	0
38 <b>0</b> 1	.252	0	0	19380	19380	0	2,686	2,686
380 <sup>+</sup>	.252	.022	18620	0	18620	-14,00	0	-,261
397	.230	.061	51.640	0	51640	-13.61	0	703
431	.169	.050	42330	0	¥2330	-12,83	0	543
465	.119	.043	36400	0	36×90	-12,05	0	439
199	.076	.035	29630	o	29630	-11,27	0	334
533	.042	.032	27090	0	27090	-10.49	C	284
584	.009	.009	7620	0	7620	-9-33	0	071

q = 263.7 pef	c <sub>L</sub>	= 4.847 /Red.	q S C <sub>L at lat</sub> = 846,550
* Macelle Airloads:		Outhourd	** c <sub>1</sub> = 227229 ① <sub>1</sub> (At Bacelles X, = 0.0)
d E C C	50222	50679	(AL MICELLES A1 = 0,0)
d S <sup>R</sup> C <sup>M</sup> G <sup>M</sup>	2,430,000	2,454,000	
q S <sub>H</sub> C <sub>L</sub> X <sub>H</sub>	4,972,000	4,572,000	

Column 7 lists the wing airload torsion moment arms. Column 8 gives the incremental nacelle airload torsion; and column 9 gives the combined wing-nacelle airload torsions.

The required unit inertia data are shown in Table C-4. Column 2 gives the spanwise distribution of inertia shear, and column 3, the spanwise distribution of inertia torsion. Columns 4 and 5 are the panel increments corresponding to columns 2 and 3 respectively. Column 6 gives the unit inertia pitching moment due to the large mass concentration at the nacelles.

The matrices of wing torsion and of wing bending influence coefficients are shown in Table C-5.

With the necessary preliminary data established, the elementary distributions can now be determined.

The derivation of the static-mode elementary distribution is shown in Table C-6 and Figure C-1.

In Table C-6, the pertinent information taken from the transfer functions is listed first. The computation of unsteady lift growth functions is shown next; this involves taking the Laplace transforms of the familiar Wagner and Kussner functions (as approximated in exponential form) and replacing p with  $i\Omega$ . Next, the root angle of attack is computed. This is followed, in Table C-6(d) with computation of the increment in angle of attack due to twist and the net angle of attack per "g" as a function of wing station. The resulting spanwise variation of angle of attack per "g" is then plotted in Figure C-1.

The final spanwise variation of loads in the static mode is obtained in Table C-6(e). This table is self-explanatory. The loads defined therein are with respect to the arbitrary load axis that is used in the stress analysis.

In Table C-6(f), the loads of Table C-6(e) are converted to a form such that the design conditions generated using the elementary distributions can be compared directly with the statistically defined loads in Table C-1. The axis with respect to which moments are defined is rotated and shifted to conform to the axis system used in the ten-degree-of-freedom analysis, and the loads are listed at the wing stations where the loads are given in Table C-1. In addition, two rather minor adjustments are made, in order that these distributions be consistent with the less exact way in which the loads were summed in the ten-degree-of-freedom program.

TABLE C-4. UNIT INERTIA LOADS, MODEL 188 CASE 202

0	(2)	3	-	MODEL 188 C	
W.S.		+ -	0	<u> </u>	6
	82	10 <sup>-6</sup> MyLA	$\left( A \frac{s_z}{s_z} \right)$	10-6 & MyLA	10 <sup>-6</sup> A My
}	n <sub>z</sub>	nz		\ \left(\frac{12A}{h_z}\right)	
	I.b	InLb	1 1 1	/1	
<u></u>	Given	Given	② 1 - ② <sub>1+1</sub>	3 1 - 31+1	Given
0	22798	.1812	740	0429	Olven
65	22058	.224	2948	1344	
101	19110	- 3585	1008	0874	Ö
137	18105	.4459	700	0381	0
167-	17402	. 4840	1179	+.0170	0
167-	16223	.4670	1925	+.1915	.01570
167+	14298	.2755	447	0093	0
179	1,3351	.2848	350	0074	
197	13501	•2922	167	0035	
209-	13334	-2957	1108	.0123	0
509-7	12226	.2834	1925	.1915	.01570
209+	10301	.0919	1157	0549	0
239	9144	.1468	1566	0700	ő
275	7578	.2168	638	0276	0
293	6940	.2444	765	0327	o
329	6175	.2771	257	0108	o
346-	5918	.2879	351	003k	0
346 N	5567	.2913	2378	.2157	.01384
346+	3189	.0756	582	0213	0
380-	2607	.0969	218	0020	o
380- <sub>M</sub>	2389	.0989	1472	+.1335	.00856
380+	917	0346	152	0070	0
397	765	0276	165	0073	ő
431	600	0203	155	0063	0
465	445	0140	125	0043	0
499	320	0097	130	0041	0
533	190	0056	170	~.0050	0
584	so	006	20	0006	o l

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TABLE C-5. DEFLECTION INFLUENCE COEFFICIENTS, MODEL 188

Torsional Influence Coefficients  $\sim [\delta_{\rm T_{1,j}}] \sim ({\rm Rad/In,-Lb})$ 

				7		1					
	WS	65	101	143	188	239	311	359	414	28 4	550
	65	12,2	12.2	12.2	12.2	12,2	12.2	12.2	12.2	, 12.2	12.2
	101	12.2	20.1	20.1	20.1	20.1	20.1	20.1	20.1	20.1	20.1
	143	12.2	20.1	30.8	30.8	30.8	30.8	30.8	30.8	30.8	30.8
	188	12.2	20.1	30.8	9.4	9.4	9.44	9.44	9.44	9.44	9. <del>11</del>
	239	12.2	20.1	30.8	9.4	т. ₹9	64.1	64.1	₽.1 7.0	64.1	64.1
[8]	12	12.2	20.1	30.8	9.4	64.1	103.7	103.7	103.7	103.7	103.7
- C - C - C - C - C - C - C - C - C - C	359	12.2	20.1	30.8	9.4	45	103.7	143.9	143.9	143.9	143.9
	414	12.2	20.1	30.8	9.4	64.1	103.7	143.9	218.8	218.8	218.8
	482	12.2	20.1	30.8	9.4	64.1	103.7	143.9	218.8	369.3	369.3
	550	12.2	89.1	30.8	9.44	64.1	103.7	143.9	218.8	369.3	369.3

Bending influence Coefficients  $\sim \left[\delta_{B_{1,1}}\right] \sim (\text{In./Lb})$ 

			1								
	82	65	18	143	188	239	311	359	414	28 <u>4</u>	550
	6	ė	1.7	2.7	3.6	4.8	<b>4.9</b>	4.7	3.6	10.1	11.6
	101	1,1	3.6	6.	8.3	11.11	15.0	17.7	20.7	4.45	28.1
	143	2.7	5.9	10.5	15.6	21.5	29.1	35.1	4.14	7.6 <del>1</del>	56.9
	188	3.6	8.3	15.6	8.4%	35.4	50.4	60.5	72.0	86.1	100.1
. [	239	4.8	11.1	21.5	35.4	53.5	7.61	97.2	117.2	142.0	166.7
ST A	Ħ	4.9	15.0	7.68	50.4	79.1	128.2	161.7	200.2	247.7	295.2
	359	7.4	17.7	35.1	60.5	97.2	161.7	210.2	266.8	336.7	1,06.7
	414	8.6	20.7	41.4	72.0	117.2	200.2	266.8	351.1	457.7	564.3
	28 <sub>4</sub>	10.1	4.48	49.8	36.1	142.0	247.7	336.7	457.7	630.3	30 <b>9.</b> 4
	550	11.6	28.1	56.9	1001	166.7	295.2	1,06.7	564.3	₹608	1101.9

# TABLE C-6. CALCULATION OF STATIC MODE ELEMENTARY DISTRIBUTIONS, MCDEL 188 CASE 202

#### (a) INFORMATION FROM TRANSFER FUNCTIONS AT f = .1 CPS

# (b) TRANSIENT AERODYNAMIC FUNCTIONS

$$K_{GW} = 1 - \left[ \frac{.236 \ \Omega^2}{.013456 + \Omega^2} + \frac{.513 \ \Omega^2}{.529984 + \Omega^2} + \frac{.171 \ \Omega^2}{23.4256 + \Omega^2} \right] - i \left[ \frac{.027376 \ \Omega}{.013456 + \Omega^2} - \frac{.373464 \ \Omega}{.529984 + \Omega^2} + \frac{.82764 \ \Omega}{.23.4256 + \Omega^2} \right] = .99552 - .0498 \ i; \ |K_{GW}| = .99603 \approx 1.0$$

$$K_{LW} = 1 - \left[ \frac{.165 \ \Omega^2}{.0081 + \Omega^2} + \frac{.335 \ \Omega^2}{.36 + \Omega^2} \right] - 1 \left[ \frac{.01485 \ \Omega}{.0081 + \Omega^2} + \frac{.201 \ \Omega}{.36 + \Omega^2} \right]$$
$$= .99490 - .03669 \ 1; \left| K_{LW} \right| \approx 1.0$$

# (c) ROOT ANGLE OF ATTACK

$$\alpha_{\text{Root}} = K_{\text{G}} \frac{\text{W}}{\text{V}} + K_{\text{L}} \left( \Phi_{\text{S}} - i \Omega \cdot \mathbf{S}_{\text{O}} \right)_{\text{S Since W/V}} = 1$$

$$\alpha_{\text{Root}} = .9952 - .04298 i + (.99490 - .03669 i) [-.59003 + .21672 i -.015699 i (.84695 - 26.833 i)]$$

$$= -.00315 + .19651 i$$

$$T\alpha_{\text{Root}} = .1965$$

# TABLE C-6. CONTINUED (d) SPANWISE VARIATION OF ANGLE OF ATTACK

Solving for  $\alpha/n_z$ 

$$\frac{\alpha_{\text{ROOT}}}{n_z} = \frac{.1965}{4.6249} = .04249 \text{ RAD}$$

$$\frac{\theta_{\text{OUT'B}}}{n} = \frac{.005866}{4.6249} = .00127 \text{ RAD}$$

$$\left|\frac{\Delta \alpha_{\text{TWIST}}}{n_z}\right| = \left[\delta_{\text{Tij}}\right] * \left|\frac{\Delta \left|\text{T}_{\text{my}}\right|}{\left|\text{T}_{\text{n_z}}\right|}\right| = \left|\frac{\alpha_{1}}{n_z}\right| = \frac{\alpha_{\text{ROOT}}}{n_z} \left\{1.0\right\} + \left|\frac{\Delta \alpha_{\text{TWIST}}}{n_z}\right| + \left|\frac{\theta_{\text{NAC}}}{n_z}\right|$$

$$\text{ROTE: } \left[\delta_{\text{Tij}}\right] \text{ is given in Table C-5}$$

w.s.	10-6 T	Δα TWIST	MAC	<u> 2</u> 1
	Tnz	n <sub>z</sub>	n <sub>E</sub>	n <sub>z</sub>
65	+.2615	.00081		.04332
101	+.1075	.00114		.04363
143	+.1372	.00146		.04395
188	2313	.00168		.04417
188N		.00168	.00120	.04537
239	+.1464	.00244		.04493
311	+.1316	. 20342		.04591
359	05 <del>4</del> 3	.00388		.04637
359N		.00388	.00127	. O4764
414	+.0850	.00515		.04764
482	+.0545	.00641		.04890
550	+.0296	.00707		.04956

TABLE C-6. CONTINUED
(e) LOADS AT STRESS ANALYSIS STATIONS

2. アンコンはのできる。 1. アンコンはのできる。 1. アンコンはのできる。

-		بصسح	_			_	_		_	-	_			_		_			_		_	_			_	_	_			
3	10 <sup>-6</sup> Myra Bat	<b>®-</b> @	0900	0803		1250	1143	09T3	or34	0793	ogeo	0820	0697	Ob.73	0583	0799	0841	0705	0635	-,06K	0575	0944	<b>385</b>	0922	087J	0611	0413	02k3	0120	0089
Э	10 <sup>-6</sup> M <sub>E</sub>	*	4.72	3.855	3.44.8	3.0%	2.73	2.75	2.73	2.67a	2.490	2.367	2.367	2.367	2.063	1.656	1.491	1.23	1.108	1.108	1.108	.8427	. 8k27	.8427	y689°	54g4.	1613.	1244	.0499	.0018
(3)	χŧ	Z/(***)/2	8.8	18.0	18.0	15.0	•	•	0.9	9.0	6.0	•	•	25.0	18.0	9.0	18.0	8.5	ı	,	17.0	•	,	8.5	17.0	17.0	17.0	17.0	25.5	5.0
9	3. East	O-0	15608	11385	11583	9770	7918	7606	ž.	18 %	10218	10225	11333	12111	10821	9578	8767	6653	5739	9699 9	6269	1136	88 88 88	726	% %	6374	8617	2853	1528	ž
<b>@</b>	10 <sup>-6</sup> MylA	Table 0-4	अधाः	. 2241	.3585	654.	0484.	ora.	.2775	. 2848	. 2962	.2957	.283t	.0919	.1468	.2168	न्यक.	.em	.2879	.291.3	.0756	6960	6960	0346	02T6	0203	040	009T	9500:-	0000
Θ	2 <sub>8</sub>	Table C-b	86J.23	22058	19110	18102	1740e	16823	14296	13831	13501	13334	12226	10301	110	7578	0 <b>16</b> 6	61.13	9318	5367	30 S	2607	2369	917	ě	8	ž.	84	85	&
0	Y <sub>A19</sub> _ot	<b>⊙⊙</b> ‡	<b>8160</b> °	.2038	.2622	.3809	.3697	.3697	1908.	.2055	.2100	.2137	.2137	9440.	986.	1369	.1603	.2066	1482	1162	.ag	.000	5300.	1268	-,1116	081k	0533	0360	a.76	0035
0	ay v	00 ₹	30406	33443	30693	27812	25,260	23,800	24183	24003	23749	23559	23559	21422	19965	17750	15727	12628	17697	11657	10168	12511	112211	10268	9415	£69	4943	21.73	1728	379
Θ	8 m 8	-	64840	.04331	.04363	.04393	ŧ	.04529	90440°	.04414	876.	1	.04568	.04448	.04493	64845.	99540.	.04612	•	. Ot 135	.04628	•	.04816	. ot.689	.04726	£799	.04861	11640.	64949.	.04975
Θ	10-6 MYA	Table 0-3	-2.652	-1.347	-1.346	-1.110	•	3.73	077	107	ero	0	3,700	 86	-1.079	418	-1.025	£	o	4.339	.336	o	3.686	198: -	703	543	439	\$6	28	on
0	Agh.	Table 0-3	116820	63490	96030	\$6720	•	25110	060 <del>4</del>	2760	e e e	c	92TO	55030	62650	33.00 13.00	63.60	85400	0	31300	-827to	0	19380	18680	51640	42330	36.68	29630	27090	7680
Θ	9	Reference	·	ક	101	137	191	167	167*	119	197	502	200	203	82	E	8	8	¥,	3461	\$	ğ	<b>100</b>	bg.	282	#	\$6	<b>66</b>	533	<b>1</b>

(f) LOADS AT DYNAMIC ANALYSIS STATIONS

_			_		_				_			-
(3)	or Fairer	Nefer to Note 3	.335T	. 2245	orf68	3495	2070	. 0839	1621.	780.	.2089	
<b>③</b>	AYALIA Ta.	67.8 - 0842 (3)	60.BL	57.78	53.74	50.30	44.65	38.67	35.80	30.08	24.35	
(3)	10-61 11-11-11	@·@	0583	1058	1167	0407	0799	0750	0875	0512	a8z	
0	10-6 14, In13	Nefer tof Note 1	•	6400.	00ek	9900.	,	0115	7400.	•	•	
0	10-61 In15	Table C-6(e)	0583	1107	1143	0473	0799	0635	0922	0512	0182	
Θ	10 <sup>-6</sup> 14 InLb	Nefer to Note 2	3.6173	3.2233	2.7826	2.3690	1.6721	1,1001	.8259	.3338	.0745	
0	8 <sub>Z</sub> Ad3.	@·@	11484	10407	7953	11744	9572	6497	9037	% *	2191	
ග	¥ <sup>₹2</sup>	Refer to Note 1	•	-240	+35	-367	ı	+758	*8£	1	•	
9	क्ष <b>क</b>	Table 0-5(e)	18411	10647	7918	12121	2172	5739	9371	<b>X</b>	2191	
0	Wing Station	Olven	83	119	167	503	273	346	380	911	216	
0	Lump Ptetion	Given	101	143	188	230	Ħ	329	414	<b>2</b> 4	550	
0	Panel	Oaven	œ	m	4	•	9	~	<b>&amp;</b>	6	91	
				_		_	_	_		_	_	•

inadvertartly defined at wing stations 83, 122, 165.5, 213.5, 275, 335, 386.5, 448, and 516. To provide consistency with the mission In the ten degree-of-freedom analysis, insrtia loads are defined at the wing stations listed in Column 3 . Airloads, however, were analysis loads, the slight correction is applied. Or 1:

To provide consistency with the mission analysis results, the bending moment is integrated in a manner consistent with the ten-degree-NOTE 2:

"x-" [@... (@... -@.) - @.( @. - @.)]

HOTE 3: NyEA, = .9964 MyIA, -.0842 My + 5g, AX EA-IA

MEAN SHEAN PLANS

 $q_{TB} g_3 = .02167 g_a - 26 (10^{-7} M_A) + 164 (10^{-6} M_y) = 209.9 LB/IH.$   $q_{TB} g_3 = -.01892 g_a + 18 (10^{-6} M_\chi) + 163 (10^{-6} M_y) = -97.4 LB/IH.$   $q_{TB} M_G = -.03116 g_a = 70 (10^{-6} M_y) + 390 (10^{-6} M_y) = 195.2 LB/IH.$   $q_{TB} M_G = -.02636 g_a + 45 (10^{-6} M_y) + 390 (10^{-6} M_y) = 89.0 LB/IH.$ 

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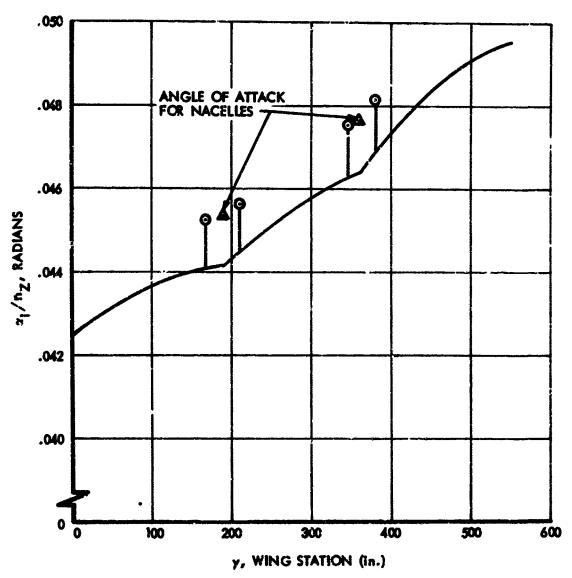


FIGURE C-1. SPANWISE VARIATION OF  $\alpha_i/n$  IN STATIC MODE, MODEL 188 CASE 202

The derivation of the dynamic bending mode elementary distribution is accomplished next and appears in Table C-7 and Figure C-2.

In Table C-7, the pertinent information taken from the transfer functions is listed first. Next, the computation of the unsteady lift growth functions is shown, followed by the computation of the wing elastic deformations.

The determination of the resulting local angle of attack for the wing and nacelles is next presented, in Table C-7(d). Determination of the local load factors for the wing and nacelles is shown in Table C-7(e) through (h). The spanwise variations of angle of attack and of load factor are then summarized in Table C-7(i). These are shown in complex form in columns 2, 3, and 4. The modulus of each is then obtained in columns 5, 7, and 9; and in columns 6, 8, and 10 the modulus is arbitrarily multiplied by .0400 to reduce the magnitude of the loads to a more convenient level for the ensuing computations. Columns 6 and 8 are plotted in Figure C-2.

Spanwise distributions of the loads in the dynamic bending mode are then obtained in Table C-7(j). In Table C-7(k), the loads are converted to a form such as to permit direct comparison of the design conditions that will be generated with the statistically defined loads. The axis with respect to which moments are defined is rotated and shifted, and the loads are listed at the wing stations where the statistically defined values are available. The same two small adjustments discussed above in connection with Table C-6(f) are also made.

The derivation of the dynamic corsion mode elementary distribution is identical in form to that for the dynamic bending mode distribution. For the sake of brevity, only the final spanwise distribution of loads is presented for the dynamic torsion mode. These are shown as Tables C-8(a) and (b).

The one-g flight loads for mission analysis cases 201 and 202, at the wing stations and in the axis system required for stress analysis, are given in Table C-9. (One-g flight loads consistent with the dynamic analysis appear in columns 6 and 7 of Table C-1.)

In determining the elementary distributions for the Model 188, it was found that, at the resonant frequency, the model displacements and rotations tended to be reasonably well in phase. As a result, the various panel loads also tended to be reasonably well in phase. Consequently, when a set of panel loads was established by taking the modulus of each complex panel load, and these were integrated to give shears and torsions, and the shears in turn were integrated to give bending moments, the shears, torsions and bending moments thus obtained were all in good

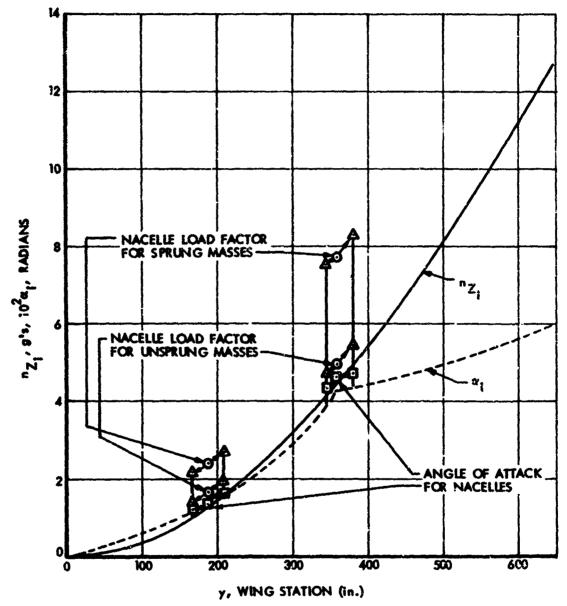


FIGURE C-2. SPANWISE VARIATION OF  $\alpha$  AND  $n_z$  IN DYNAMIC BENDING MODE, MODEL 188 ÇASE 202

# TABLE C-7. CALCULATION OF DYNAMIC BENDING MODE ELEMENTARY DISTRIBUTION, MODEL 188 CASE 202

### (a) INFORMATION FROM TRANSFER FUNCTION AT f = 2.1 CPS

W.S. (In.)	∆S <sub>Z1</sub> ~ Lb Panel Shear	10 <sup>-6</sup> A N <sub>yi</sub> ~ InLb Fanel Torsion	θ <sub>Mac</sub> ~ Rad	X <sub>Nac</sub> ∼ Chords
65	119453 + 63030 i	5.817 - 1.216 1		
101	36064 + 73300 i	2.292693 i		
143	55049 + 22400 1	2.599 - 1.460 i		
188	-25752 + 26600 1	.812 - 2.641 1	.0225902923 1	.000339003009 1
239	35856 - 55400 i	1.961 - 2.836 i		
317	27708 - 138700 1	1.090 - 2.865 1		
359	-83699 - 620690 1	-7.551 -78.778 1	.0158910417 i	0244807739 1
414	11617 - 119330 1	.179 - 1.414 i		
482	- 1172 - 99819 1	063755 i		
550	-11244 - 89261 1-	109137 i		

### (b) TRANSIENT AERODYNAMIC FUNCTION

$$\mathbf{K}_{IM} = 1 - \left[ \frac{.165 \ \Omega^2}{.0081 + \Omega^2} + \frac{.335 \ \Omega^2}{.36 + \Omega^2} \right] - 1 \left[ \frac{.01485 \ \Omega}{.0081 + \Omega^2} + \frac{.201 \ \Omega}{.36 + \Omega^2} \right]$$

- .76676 - .18331 i

K\_IR = 1.C - Oi (Nacelle mirloads tend to develop instantaneously since most of the resulting mirload is due to the propeller.)

### (c) COMPLEX WING ELASTIC DEFLECTIONS

$$\left\{ \phi_{1} \right\} = \left[ \delta_{T_{1},1} \right] * \left\{ \Delta N_{T} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}} \right\} = \left[ \delta_{B_{1},1} \right] * \left\{ \Delta S_{Z_{1}$$

NOTE:  $[\delta_{T_{1,j}}]$  and  $[\delta_{B_{1,j}}]$  are from Table 0-5.  $\Delta$  My<sub>1</sub> and  $\Delta$  S<sub>Z1</sub> are from the above TRM output.

# TABLE C-7. CONTINUED (d) COMPLEX LOCAL AERODYNAMIC ANGLE OF ATTACK

WING

$$\left\{\alpha_{1}\right\} = K_{\text{LW}} * \left(\left\{\phi_{1}\right\} - \frac{i\Omega}{c}\left\{\Xi_{1}\right\}\right) = \begin{bmatrix} -.0269 - .0854 & i \\ -.0572 - .1366 & i \\ -.1064 - .2030 & i \\ -.1776 - .2848 & i \\ -.2810 - .3951 & i \\ -.4793 - .6126 & i \\ -.6544 - .8312 & i \\ -.7719 - .8115 & i \\ -.9282 - .7772 & i \\ -1.0896 - .7324 & i \end{bmatrix}$$

NACELLES

$$\left\{ \sigma_{j} \right\} = K_{IN} * \left( \left\{ \phi_{i} \right\} + \left\{ \theta_{NAC} \right\} - \frac{i\Omega}{c} \left\{ \Xi_{i} \right\} \right\}$$

$$-i\Omega \left\{ X_{NAC} \right\} = \begin{cases} -.1134 & -.4320i \\ 0 & 0 \\ -.6031 & -1.3112i \\ 0 & 0 \end{cases}$$

NOTE:  $\bar{c} = 168.7$  in.

## TABLE C-7. CONTINUED (e) COMPLEX LOCAL I OAD FACTORS

The location of the local masses relative to the wing elastic axis is obtained from the IRM input data. Positive  $\hat{x}_{x}$  denotes that local mass is forward of the wing elastic axis.

1		١.
W.S.	Ax wing - in.	Ax nac - in.
65	4.71	-
101	3.51	-
143	1,81	-
188	54.82	151,40
239	1,90	-
311	- 1,11	-
359	14.20	128, 21
414	-11,11	-
482	- 8,50	-
550	- 8,40	-
1		

(f) WING TRANSLATIONAL LOAD FACTORS

$$\left\{ \begin{array}{l} n_{z_{1}} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \right\} + \left[ \begin{array}{l} x_{wing_{2}} \\ x_{wing_{2}} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{2} \end{array} \right] \right)^{2}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \\ n_{z_{3}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{2} \end{array} \right\} + \left[ \begin{array}{l} x_{wing_{2}} \\ x_{wing_{2}} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{2} \end{array} \right] \right)^{2}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \\ n_{z_{3}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{2} \end{array} \right\} + \left[ \begin{array}{l} x_{wing_{2}} \\ x_{wing_{2}} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{2} \end{array} \right] \right)^{2}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \\ n_{z_{3}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{wing_{2}} \\ v_{2} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{2} \end{array} \right] \right)^{2}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \\ n_{z_{3}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{2} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{1} \end{array} \right] \right] \right\}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \\ n_{z_{3}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{1} \end{array} \right] \right\} \right\}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{2}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} v_{1} \\ v_{1} \end{array} \right] \right\} \right\}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{1}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \right\}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{1}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \right\}$$

$$\left\{ \begin{array}{l} n_{z_{1}} \\ n_{z_{1}} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} z_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right]$$

$$\left\{ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right\} = -\frac{p^{2} v^{2}}{g^{2}} \left( \left\{ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right\} + \left[ \begin{array}{l} x_{1} \\ v_{1} \end{array} \right] \times \left[ \begin{array}{l} x_{1$$

(g) NACELLE TRANSLATION LOAD FACTORS

$$\left\{ \begin{array}{l} n_{z_{j}} \right\} = \frac{p^{2}v^{2}}{g^{2}} \left( \left\{ z_{1} \right\} + \left[ x_{\text{wing}} \right] + \left\{ x_{1} \right\} \right) - \frac{p^{2}v^{2}}{g^{2}} \left\{ x_{\text{nac}} \right\} = \begin{cases} 0 \\ -.580-59.8991 \\ 0 \\ -9.74-192.671 \end{cases}$$

(h) NACELLE PITCH ACCELERATIONS

$$\left\{ \begin{array}{c} 0 \\ 0 \\ 1 \end{array} \right\} = \frac{p^2 \sqrt{2}}{c^2} \left( \left\{ \begin{array}{c} 0 \\ 1 \end{array} \right\} + \left\{ \begin{array}{c} 0 \\ 0 \\ 0 \end{array} \right\} \right) = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -13, 45 - 232, 811 \end{bmatrix}$$

TABLE C-7. CONTINUED ... (i) SUMMARY OF a, n, AND 8

	(B	To Be Plotted	<b>⊚</b> ₹0.					ಕ ಕ				9.35			
	ၜ	T						77.95				233.0			
	@	Beg To Be Flotted	D 10.	91.	8.	5.	1.65	9. F2	2.09	3.48	まず	7.72	5.76	2.66	9.61
	0	Trat	Medulus or (3)	<b>90°</b> ₹	9,18	18,63	41.20	59.98	52.30	01.10	123.45	193.00	144.00	191.69	240.20
	@	G 1 To Be Plotted	<b>⊙</b> ₹0.	<b>9£00</b> °	6500.	2600.	.0134	.0176	.019t	.0311	.0423	.0570	8440.	1840.	.0526
N	ල	Tori Sed	O 20	9680.	1941.	.2293	.3357	2144.	o‱.	.7780	1.0575	1.4245	1,1205	1.2105	1.3145
	<b>છ</b>	0, - Rad/Sec	Table C-7(h)					4.50- 75.761				-13.45-232.811			
	<u>ල</u>	e ,9 - Tag	Table C-7(f)	3490°4 -020° -	133- 9.4821	376- 18.6191	750- 41.9771	580- 59.8991	- 1.56 - 52.291	- 3.04 - 87.051	- 4.72 -123.301	- 9.74 -192.671	- 5.64 -143.881	- 7.95 -191.42d	-10,45 -239.801
	<b>©</b>	Cr 1 - Rade	Tuble C-7(d)	145806360	057213661	106420301	177628481	1134 43201	281039511	479361261	654483124	6031-1.31124	771981151	9282 77721	-1,089673241
	G	v. s. Id.	Reference	65	īg	143	186	19811	239	377	359	3598	414	784	\$20

(地方) (地方は) (地方の) (地方の)

(i) LOADS AT STRESS ANALYSIS STATIONS

	9	30-6	200 00.00	2. TT98	8.7000	2.4605	表站	2.30%	2.3403	2.2121	2.20%	1,1997	2.1969	\$,2000	1.9676	1.9717	2.0809	2.0517	2.1354	2.1707	2.1797	.6937	新.	.7433	- 250	\$657	8068	-156	10fe	06%	0093
	<b>③</b>	10 <sup>-6</sup> Nu <sub>LAnet</sub>	: ,	18:76	15.916	14.229	12.434	10.919	10.919	10.919	10.305	9.360	8. 76t	8.761	6.761	7.872	5.52	4.690	3.006	2.370	2.370	2.370	1.4613	1.603	1.4613	1.2361	. 61.76	<b>1</b>	. 2566	.1048	ogoo.
	0	<u>♣</u> ¥	Given	2,3	18.0	18.0	15.0	٠	•	6.0	9.0	6.0	•	•	15.0	18.0	9.0	16.0	8.5	•	•	17.0	•		8.5	17.0	17.0	17.0	17.0	2.2	\$.0
SNC	•	B. set	<b>∞</b> • ∞ ‡	43248	<b>डरभभ</b>	1864	99606	1905	51410	05605	21385	51589	\$1550	51657	06664	19864	17988	16094	step18	11937	10610	99698	98963	14163	15061	13777	10%5	4510	5709	3370	89
STRESS ANALYSIS STATIONS	<b>(3</b>	20-6 NyLA	4-0 erqui	0489	481	0674	03th	5 to .	31913	0093	00Th	0035	.0483	.1915	0549	0700	0e76	0387	ao	¥00	2157	0213	00%	.1335	00Te	0073	0063	0043	0041	00%	000
LYSIS	0	V44 9-04	Table 0-3	-2.652	17.41	-1.76	-1.110	٥	<u>\$</u>	077	107	076	•	3.78	8.	7.93	<b>3.</b>	-1.005	£	•	4.339	Š	٥	%. \$3.	198	. 703	£	£4. •	\$.	Ž	тю. <b>-</b>
SANA	0	20-6 AN	Table 0-4						.01570					or\$20.							. a. 364			,000.							
STRES	0	:•*	Table 0-7						ę ę					đ				•			84			N.							
LOADS AT	Θ	Ra 3 sorr		-1.96	7.7-	**	7.2	20:	8	٠ ٤	8.	53	8.	<b>3</b> 5	83	۲۰.	Ę	14.1	1.95	3.8	5.40	2.19	3.40	6.23	37.75	r.	\$.5	\$.\$	6.33	7.65	6.91
- 1	9	$\left( \Delta_{\frac{n}{n_k}}^{\frac{n}{2}} \right)_i$	Table 0-4	740	246	1008	8	£11	1961	ž	ጷ	167	100	ž.	1157	3. 3.	3	Ę	22	ž	2376	뫉	ដ	11/12	*	ž	155	ş	83	5	&
ĵ.	<b>©</b>	Pag.	 ©	8.	2.	4	હ	3.50	2.13	1.10	۲. ت	2.5	8:7	T	8:1	34.9	8. a	3.46	8.	\$ \$	7.4.7	まず	× 4.5	9.59 	2.17	š.	2.3	7.63	3	3	10.96
	9	* *	71¢. 02°	9100.	.00.	9200	9070		82.80	eno.	8. 8.	94 g	•	820.	sa.	9000	980	ă ă	.0370	•	.0433	٠. 8	•	40.	ę.	845	.0463	20.0	966	0	:055
	Θ	A SaA	table 0-3	116820	63490	66030	<b>26</b> 720	•	भार	26 26 26	<b>3</b>	22	0	20110	35030	<b>68</b>	200	63.430	824.8	•	3300	Callas-	0	19380	19660	51640	18330	84	268	27030	1880
	Θ	,	Otven	x	8	â	851	167	167	Ë	ž	ğ	ģ	8	ź	2	췵	a	ន័	34	*	Š.	8	Š	8	114	3	3	316	88	*
	Θ	2	Olven	0	s	ള	137	74	17.72	167	22	5	\$	8008	662	239	£	ŝ	8	, <u>%</u>	30 A	ķ	Þ,	8	ş,	Ř	#	Ş	<b>§</b>	53	ş

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TABLE C-7. CONCLUDED

The second of th

(k) LOADS AT DYNAMIC ANALYSIS STATIONS

9	10-6 18.24 In13	Nefer To Mote 3	899T <b>'</b> ₹	4, 1646	4.11ks	3.7340	3.6675	3.589	œn.	.0538	.0125
<b>(3</b> )	A Xma-rA	67.8 - 0842	18'09	57.78	53.74	8.8	44.65	38.67	35.80	30.08	<b>24.3</b> 5
(3)	10-6 1974A61 1815	<b>©</b> •@	2. <b>26</b> 01,	2.1032	2.0044	1.7612	1.8120	1.9526	- 2455	1736	0954
0	10 <sup>-6</sup> 4 MyA 10-62 MyA	Nefer To Note 1	***	6000*	000	\$300*	:	009	1100*	:	•
0	47-41 111-41		2, 2801	2, 1023	2.0050	1.7587	1.8120	1,9618	- 2099	1796	0854
0	10 <sup>-6</sup> N <sub>X</sub> InEb	Nefer To Mote 2	14.9595	13.2193	10.8077	8,6968	5.4953	2.3143	1.4966	.6319	11511
9	es Ads.	<b>0</b> .0	\$6872	h96m	50673	9696	47388	tants	14753	\$30\$	0454
<b>©</b>	• • • • • • • • • • • • • • • • • • •	Refer To Note 1	:	£4 -	8	-140	:	909	oge.	;	i
0	នឹង	13.b).c7(3)	3,6872	69830	1900	06664	47338	11537	15061		4510
9	Wing Station	Given	ક	ST.	Ľ,T	8	275	346	윷	944	316
0	Lump Station	Gtven	ğ	143	887	ŝ	a	339	424	284	8
Θ	Page	diven	œ	м	*	*	9	۴-	•	٥	ន

ore in in the ten degree-of-freedom analysis, imerias loads are defined at the wing stations listed in column (3). Airloads, however, were insderrently defined at wing stations \$3, 122-165.5. 213.5, 275, 335, 366.5, 448, and 316, To provide consistency with the mission analysis loads, the slight correction is applied.

Note 2: To provide occasistency with the mission amblysis results: the bending moment is integrated in a manner consistent with the ten degree-of-freedom program.

ses Spear 7low

432 83 = .021678<sub>2</sub> · 26(10<sup>-6</sup>M<sub>2</sub>) + 164(10<sup>-6</sup>M<sub>3</sub>) = 1310.1 La/ld. 432 83 = .0109268<sub>2</sub> + 13(10<sup>-6</sup>M<sub>2</sub>) + 163(10<sup>-6</sup>M<sub>3</sub>) = 61.6 La/ld. 432 316<sup>-2</sup> · 031168<sub>2</sub> - 70(10<sup>-6</sup>M<sub>2</sub>) + 390(10<sup>-6</sup>M<sub>3</sub>) = 2551.1 La/ld. 432 316<sup>-2</sup> · 026368<sub>2</sub> + 45(10<sup>-6</sup>M<sub>2</sub>) + 390(10<sup>-6</sup>M<sub>3</sub>) = 393.1 La/ld.

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# 100 mm d

TABLE C-8. DYNAMIC TORSION MODE ELEMENTARY DISTRIBUTION, MODEL 188 CASE 202

			<b>Q</b>											,		_		•													
	9	10 <sup>-6</sup> 18 Lanet	2 000 : 000 : 000	-2.0706	-2.0860	-2.1091	-2.1066	-2.0979	-2.0933	-1.5186	-1.51%	-1.5086	-1.5057	-1.5090	-1.0303	9699	6412	TrBT	6899	6536	6410	3668	3998	2570	2041	T.T	96(1	101.	0795	0495	0051
	3	10" <sup>6</sup> Maranet	:	966Z*¶	3.7735	3.4657	3.1450	2.8756	2.8756	2.8756	2.7.30	2.4732	2.3155	2.3155	2.3155	17.8471	1.3495	1.1343	. 7563	.597	A797.	A797.	.3697	769€.	7690.	.3195	. 2309	.1515	.000	.0386	. 00088
	(2)	7 T	Given	<b>%.</b> 5	18.0	18.0	15.0	•	•	6.0	9.0	6.0	•	•	15.0	18.0	9.0	18.0	8.5	•	•	17.0	•	•	8.5	17.c	17.0	17.0	17.0	23.5	5.0
CIONS	0	384.8	<b>©</b> 9 · <b>©</b> 0 ‡	\$£6L	8658	2468 2468	£,71	196e	5626	13679	19433	13606	13073	12774	16171	15058	12587	11365	7196 11	9006	7843	828	9636	4315	गळ	1692	2517	2153	1816	0127	<b>%</b>
STRESS ANALYSIS STATIONS	<b>(3</b> )	120 0 10 10 10 10 10 10 10 10 10 10 10 10	Table C-b	6240'-	194	of	03BL	or to.	.1915	0093	00T	0035	.0123	.1915	0547	•. m∞	0276	0327	a.ob	4£00	.2257	0213	0060	.1335	0070	0073	0063	0043	0041	0050	•.000
ALYSI	<b>©</b>	10-6 Mg.	Table 0-3	-2.652	-1.347	-1.346	-1.110	•	3.73	110.	107	. of	•	3.70		-1.079	112	-1.005	÷.	۰	è. 339	%	•	%.6 <del>8</del> 6	æ: •	703	£	o£ 4	\$	<b>€</b>	٠. م
S AN	0	10-6 Mg	Table 0-9						.a.570					.01,570							.a36			96900.							
S		2	4						•												٠.										
TRES	0		T.						. 9.89					. 8.29			<del></del>	-			-15.99			-15.99							
			n-bea + (5)	ж· -	15	8.	¥.	- :51		- - 8.	*:	- 6.	ri.		8:1	1.91	3.5	3.3	3.73	SH.	-15.99	93.7	4.23		5.16	8.%	6.83	8.2	8.81	¥.01	n.03
LOADS AT STRES	<b>©</b>	:•"		16° - 042			¥.	117927	- 9.89	99. 144		16. 191		8.89				3.05		35.1	-15.99	94.4	210 4.23	-15.99	152 5.16	165 5.08	155 6.83		-	170 10.7	20 n.03
	@ Ø	ie inter	2, 1001 - O		2948	1006			-2.18 - 9.29			1.35 167	72. 8011 69.	-1.27 1925 -1.65 - 8.29	1.68 1157	1566	636	765 2	257		2378 .09 -15.99	ž		.99 -15.99		165			-	ę,	8
LOADS AT	0 0 0	(A ns./) ns.ager 6.	2, 1001 - O	740	8762 68.	9001 94.	00L 1L.	.11 11.79	1925 -2.18 - 5.29	744 86.	1.12 350	1.35 167	72. 8011 69.	-1.27 1925 -1.65 - 8.29	1.68 1157	2.39 1566	3.82 636	<b>3</b> 6	1,17 257	3.70 351	2378 .09 -15.99	7.8c	4.61 210	1472 .99 -15.99	25.1 25.5	6.36 165	7.21 155	125	9.19 130	ę,	m.43 80
LOADS AT	0 0 0	ns, (\alpha \frac{\beta}{n_k}) \ \frac{\beta}{n_k} \ \alpha \frac{\beta}{n_k} \ \alpha \frac{\beta}{n_k} \ \alpha \frac{\beta}{n_k} \ \end{align*}	Table C-b abal + (5)	047 70. 8000	0022 .23 2948	0033 .46 1008	0045 .74 700	11. 11.9	-1.80 1925 -2.18 - 5.29	744 86. 4500-	0059 1.12 350	0065 1.35 167	72. 8011 59	0088 -1.27 1925 -1.65 - 8.29	0071 1.68 1157	0083 2.29 1566		at of 3.43 765	01.00 4.17 257	- 3.70 351	0169 . i. 7 2378 . 09 -15.99	0138 h. 86 5f2	- 4.61 210	a63 1.37 1472   .99  -15.99	0145 5.94 152	0153 6.26 165	a.64 7.21 155	0176 8.20 125	0182 9.19 130	0204 10.42 170	021 11.k3 20
LOADS AT		a, n <sub>n,1</sub> (a n <sub>n,1</sub> ), n <sub>n,1,0,0,0</sub>	2, 1001 - O	047 70. 8000 058911	63490 0062 -83 2948	660300033 .46 1008	\$67200045 .74 T00	0 - 0	0073 -1.80 1925 -2.18 - 9.29	744 86. 4500 0604	57600059 1.12 350	hero0065 1.35 167	72. 8011 59 0	251100008 -1.27 1925 -1.65 - 8.29	550300071 1.68 1157	626500083 2.29 1566	31.360094 2.82 638	63490 01.08 3.43 765	25,4000120 4.17 257	0 - 3.70 351	113000169 .47 2378 .09 -15.99	-227400138 4.86 5f2	0 - 4.61 210	19360 ads 1.37 1472 .99 -15.99	18620 0145 5.54 152	516400153 6.26 165	423300164 7.21 155	364000176 8.20 125	296300182 9.19 130	270900804 10.42 170	76200217 11.43 20

# TABLE C-8. CONCLUDED

# (b) LOADS AT DYNAMIC ANALYSIS STATIONS

					_						
(3)	72. 3.DT	Nefer To Note 3	-1.3899	-1.8582	-1.8452	4045	3866	3559	um	5.0672	0318
<b>@</b>	AX. ■A. In.		60.81	57.78	53.74	50.30	14.65	38.67	35.00	30.08	24.35
9	10-6 Marada InId	<b>⊚</b> ∙⊚	-1.4784	-1,4891	-1, 4764	6726	1884 ·	2918	-, 2056	1225	0645
0	10-6a. Mga In-ai	Refer To Mote 1	:::	-,000t	£000°+	0011	:	0600+	0015	:	
0	10-6 1671A		-1.4784	-1.4897	-1.47.87	5179	4884 -	8462.	2041	1225	5₩90
0	10 <sup>-6</sup> M <sub>71.8</sub> In.—15	Refer To Mote 2	3.5333	3.2187	2.7892	2, 2601	1,3200	. 5585	. 3744	. 1823	.0514
9	S <sub>k</sub> AdJ.	<b>⊙</b> •⊙	697PD	8927	8958	06291	12587	1188	3315	2335	1513
0	A 5. A	Refer To Note 1	****	4 1.8	- 13	+ 59	1 1	-197	£0 <del>1</del>	1	
0	41	Table C-8(a)	8549	8303	9981	16171	13621	8006	3212	2335	1513
<b>©</b>	Wing Station	Oiven	83	677	191	68	213	346	<b>8</b> 6	87	216
0	Lum Station	Given	101	143	88	239	ส	359	<b>*T</b> *	182	550
Э	Panel	Otven	c,	m	. <del></del>	50	9	-	80	٥	ន

Note 1: In the ten degree-of-freedom analysis: inertia loads are defined at the wing stations listed in column (3). Airloads: however, were insdvertently defined at wing stations g3: 123-15, 5, 213.5: 275: 335: 366.5: 448. and 516. To provide consistency with the mission analysis loads: the slight correction is applied.

And 2: No provide consistency with the mission analysis results the bending moment is integrated in a manner consistent with the ten degree-of-fraedom program.

$$\mathbf{x} \cdot \mathbf{x}^{\text{mot}} \left[ \mathbf{O}_{1,d} \cdot (\mathbf{O}_{1,d} \cdot \mathbf{O}_{1}) \cdot \mathbf{O}_{1} \cdot \mathbf{O}_{2} \right]$$

Note 3: Myza, " . 9964 Myza, - . 0842 M, + 3, Axm.za

Beam Shear Flow

 $q_{yy} = g_3^{-1} \cdot 021 L i 7 g_2^{-1} \cdot ... (10^{-6} M_{\chi}) + 164 (10^{-6} M_{\chi}) = -213.3 \text{ Le}/\text{Im}.$   $q_{yy} = g_3^{-1} \cdot 0.0992 g_3^{-1} + 16 (10^{-6} M_{\chi}) + 163 (10^{-6} M_{\chi}) = -402.9 \text{ Le}/\text{Im}.$   $q_{yy} = \frac{1}{3} \frac{1}{3} \frac{1}{3} \cdot ... \cdot 0.3116 g_2^{-1} \cdot ... (10^{-6} M_{\chi}) + 390 (10^{-6} M_{\chi}) = 96.7 \text{ Le}/\text{Im}.$   $q_{yy} = \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \cdot ... \cdot 0.2636 g_2^{-1} + 45 (10^{-6} M_{\chi}) + 390 (10^{-6} M_{\chi}) = -345.9 \text{ Le}/\text{Im}.$ 

TABLE C-9. ONE-g FLIGHT LOADS AT STRESS ANALYSIS STATIONS, MODEL 188

		Case 201			Case 202	
W.S.	S	10 <sup>-6</sup> M <sub>x</sub>	10 <sup>-6</sup> M	Sz	10 <sup>-6</sup> K <sub>x</sub>	10 <sup>-6</sup> M
	Lb	InLb	InLb	Lb	InLb	InLb
65	16373	4.547	-1.1203	20248	4.490	-2.4303
101	15174	3-957	-1.0860	17863	3.781	-2.2450
137	13309	3-455	-1.6182	14910	3.202	-2.0372
167-	10979	3.065	- <b>.9</b> 228	11862	2.774	-1.8401
167+	14083	3.065	9046	14966	2.774	-1.7771
179	13118	2.885	8575	13819	2.585	-1.6965
197	11768	2.701	7868	12248	2,390	-1,5799
209-	10630	2.527	-•7395	10946	2,208	-1.5006
209+	13663	2.527	7087	13979	2,208	-1.4290
239	11927	2.111	-,6286	11796	1.788	-1,2646
275	10598	1.728	6008	9889	1.420	-1,1516
293	9710	1.531	<b>5</b> 695	8817	1.232	-1,0799
329	7655	1.241	5031	6328	<b>•9</b> 853	-•9345
346-	6787	1.117	4678	5300	.8876	8657
346+	9516	1,117	4308	8029	.8876	7174
380-	7567	•8201	-,3629	5989	.6425	5938
380+	9257	•8501	3152	<b>7</b> 679	<b>.€</b> ::	-•1 <del>9</del> 29
397	8378	<b>.</b> 6749	2861	6804	<b>.</b> 5263	-•4405
431	6334	.4179	2162	4950	.3148	3386
465	4437	.2215	-,1589	3373	.1589	2461
1499	2713	•1109	1025	2004	.0794	1689
533	1461	• <b>059</b> 5	0605	1058	.0503	0981
584	102	<b>•00</b> 45	0080	66	*00/1/1	01.38

agreement with the values given by the modulus of the complex shears. torsions, and bending moments respectively. It is conceivable, however, that in some circumstances the panel loads may be less closely in phase-In such a situation, more than one elementary distribution might be required for each mode. It is believed, however, that such distributions could be obtained without undue difficulty. The procedure would be to retain  $\alpha_1$  and  $n_{Zi}$  in complex form and then obtain panel shears and torsions likewise in complex form. These would then be expressed in the form of modulus and phase angle. Next, the panel loads would be grouped roughly by phase angle. For each group, a representative phase angle would be selected, and the in-phase components of all panel loads determined. Integration spanwise would then give the modal-load distribution. Some experimentation might be required to obtain satisfactory groupings of the panel loads; and checks would be required - either at this stage or later - to assure that in matching the loads in one part of the wing the desired loads at other points were not exceeded.

In order to give added confidence that all necessary ingredients have been included in the determination of the elementary distributions, it is pertinent to compare the loads defined by each elementary distribution with the total loads as taken directly from the transfer functions at the respective frequencies. Exact agreement is not to be expected, of course, since at any one resonant frequency the total load contains some contribution from other modes as well as predominant contribution from the resonant mode. However, as indicated by the plots in Figure 9-3, the contributions of the non-resonant modes should generally be fairly small.

Such a comparison is shown in Table C-10. The loads in solumn 3 are those comprising the static elementary distribution of Table C-6(f). For comparison, column 4 gives the modulus of loads per "g" as obtained from the transfer functions at a forcing frequency of .1 cps. Similarly, column 5 is taken from Table C-7(k), and thus represents the dynamic bending mode elementary distribution. The modulus of the loads obtained from the transfer functions at a forcing frequency of 2.1 cps appears in column 6; the level of loads in column 6, however, is adjusted such that the shear at wing station 346 is the same as that in column 5. Loads for the torsion elementary distribution taken from Tal e C-8(b) appear in column 7. The corresponding loads from the transfer functions at a forcing frequency of 4.4 cps are shown in column 8. Here the level is adjusted such that shear at wing station 167 is the same as that in column 7. The minus sign on the loads from the transfer functions is used to denote a load modulus that is relatively 180° out of phase.

in comparing column 3 to column 4, and column 5 to column 6, it is seen that the agreement is excellent. The comparison of columns 7 and 8 shows fairly good agreement for spanwise shear and bending and for torsion

TABLE C-10. COMPARISON OF ELEMENTARY DISTRIBUTIONS WITH LOADS INDICATED BY TRANSFER FUNCTION PEAKS, MODEL 188

<b>①</b>	0	3	<b>(</b>	<b>⑤</b>	6	0	3
		Static	Node	Dymmic Ben	ding Mode	Dynamic Tor	rsion Mode
Load	W.S. in.	Riementary Distribution	Transfer Function	Elementary Distribution	Transfer Function	Elementary Distribution	Transfer Function
	Ref.	Table 0-6(1)	IBM Output	Table C-7(k)	13M Output	Table C-8(b)	IBM Output
Sz	83	11484	11133	<b>5687</b> 2	45260	8549	7794
	119	10407	10236	49807	48526	8927	8473
	167	7953	7984	50673	49583	8968	8968
Wing	209+	11744	11597	<b>49850</b>	50748	162 <b>3</b> 0	14115
Shear	275	9572	9451	47389	4830k	12587	10860
	346	<i>5</i> 497	6217	42145	k2145	8817	1 <b>/26</b> 2
	380+	9037	873"	14751	13932	3315	3904
	448	5436	5123	9505	<b>3560</b>	2335	2 <b>821</b> .
	516	2191	2105	4540	4064	1513	1854
10 <sup>-6</sup> Nx	83	3.617	3.532	14.960	14.787	3-533	3.°4,k
	119	" <b>3.2</b> 23	3.147	13.219	13.103	3.219	2.355
Wing	167	2.783	2.710	10.808	10.750	2.789	2.536
Bending	209 <sup>4</sup>	2.369	2,299	8.697	3.644	2,260	2.05k
Moment	275	1.672	1.611	5.495	5.384	1,320	1.241
About	<b>∌</b> 6	1.100	1.053	2.3i4	2.170	.5585	.61.38
Elastic	380*	.8259	.7887	1.457	1.332	.3744	.4483
Axis	448	.3336	.3175	.632	.567	.1823	.2215
	516	.0745	.0716	.154	.139	.0514	.0630
10-6	83	•3357	.4062	4.1668	4.1374	-1.8699	-2.2180
	119	.2245	.2987	4.1646	4.1060	-1.8582	-2.1785
Wing	167	.0768	.1615	4.1145	4.0432	-1.8452	-2.1287
Torsica	209+	.3495	.3928	3.73%	3.9257	· .4045	-1.0225
Homest	275	.2370	.2464	3.6675	3-7923	3886	9440
About	346	.0839	.1148	3.5894	3.6629	- •3559	8648
Elastic	390*	.1621	.1691	.1120	.1042	1177	1742
Axis	448	.0844	.0841	.0548	.0403	0672	0927
	516	.0289	.0276	.0125	.0062	0318	0412
نـــــن		4	L	<u> </u>	<u> </u>	L	

inboard of the inboard nacelle. The agreement for torsion outboard of the inboard nacelle, however, is relatively poor. Thus with respect to torsions outboard of the inboard nacelle, it appears that, for the dynamic torsion mode, the loads due to dynamic overtravel in the mode would not be adequately approximated by the total loads developed at the resonant frequency. It is also pertinent to observe, however, that the contribution of this mode to the total mean square value of the torsions outboard of the inboard nacelle is comparatively small, as indicated by Table C-2. Consequently, with respect to these loads, considerable inaccuracy in obtaining the elementary distribution could be tolerated.

### C.4 Upbending Conditions

With the mission analysis loads of Table C-1, the elementary distributions of Tables C-6, C-7, and C-8, and the one-g flight loads of Table C-9 all available, design loads required for the stress analysis of the wing can now be generated. This is accomplished in Tables C-11 through C-14.

In Table C-11, the statistically defined design load levels which it is desired to envelope appear in column 3. These are taken from column 3 of Table C-1. As pointed out earlier, the incremental and one-g loads can be handled independently. Consequently, the one-g loads for mission analysis cases 201 and 202 are subtracted from the net mission analysis loads of column 3 to define the incremental design level loads to be matched. These statistically defined loads appear in columns 6 and 7 and are designated Ls. Columns 6 and 7 are identical to columns 8 and 10, respectively, in Table C-1.

The elementary distributions obtained in Tables C-5, C-7, and C-8 are shown in columns 8-10, respectively. These distributions are designated the  $E_1$ ,  $E_2$ , and  $E_3$  distributions. The values of the 31 load quantities for the three distributions are also designated  $E_1$ ,  $E_2$ , and  $E_3$ , in order that a single column heading can apply collectively to shears, bending moments, torsions, and front and rear beam shear flows.

The statistically defined loads, Ig, are now to be enveloped by one or more design condit. is. Each of these design conditions will be made up of an appropriat in tion of the three elementary distributions. The contribution of e. ementary distribution will be defined by a value of its respective. If ficient, al, al, or all the complete set of loads comprising the conditions is then given by the expression,

 $L_D = a_1 E_1 + a_2 E_2 + a_3 E_3$ 

For each additional design condition, a new set of values of the coefficients is determined.

In generating the enveloping conditions, it is, of course, desired that as many of the  $L_S$  values as possible to matched by the corresponding  $L_D$  values defined by a single set of the loading coefficients,  $a_1$ ,  $a_2$ , and  $a_3$ . To facilitate determining appropriate values of the loading coefficients, each load for the elementary distributions is divided by its corresponding design level load,  $L_S$ . The resulting ratios are designated  $\overline{E}_1$ ,  $\overline{E}_2$ , and  $\overline{E}_3$  respectively. The values obtained using the  $L_S$  values of column 6 are listed in columns 11, 12, and 13; the values obtained using the  $L_S$  values of column 7 are listed in columns 14, 15, and 16.

For the first design condition, torsions in the outer wing will be matched. Outer wing torsion is predominantly a static loading and is produced by mission analysis case 201. As a result, the increment loads to be matched are those of column 6 and can be reproduced by use of the  $E_1$  distribution only, as given by column 8. The required "amount" of this distribution, to be defined by a value of the coefficient  $a_1$ , can be determined by looking at the  $E_1$  values in column 11. For torsion at WS 380, 448, and 516, the  $E_1$  values are .689, .715, and .734 respectively. The average is approximately .715. The indicated value of  $a_1$  is therefore 1/.715 = 1.40. Thus the incremental loads for Condition I are simply:

### 1.40 B<sub>1</sub>

A comparison of the complete Condition I loads thus defined with the statistically defined design level incremental loads is then shown by the ratios,

$$\frac{L_D}{L_S} = \frac{1.40 E_1}{L_S} = 1.40 \overline{E}_1$$

These ratios are shown in column 17. It is seen that the ratios for the cuter wing torsions are close to unity, indicating good agreement. For all other loads, the ratio is considerably below unity. In particular, outer wing shear and bending are about 70% of the mission analysis values. This result is consistent with column 12 of Table C-1, which indicates that, whereas the outer wing incremental tersion is produced almost entirely by case 201, the total increments in outer wing shear and bending moment, relative to the case 201 one-g values, are contributed largely by other cases.

TABLE C-11. DETERMINATION OF LOADING COEFFICIENTS FOR UPBENDING DESIGN CONDITIONS, MODEL 188

(a) COLUMNS 1 - 16

	by s'		Mississ	Analysi	s Essaes		Element	ery Dietr	ibutious		Eleges	tery Dist	ributi	on Entio	
<b>(3)</b>	U	3	0	9	0	0	9	9	69	3	(9)	(3)	(9)	(9)	(9)
lead.		Bet Leads	28 E 6	2 3 5 5 2 3 5 5 2 3 5 5 2 5 2	L <sub>g</sub> Cace SOL	1 <sub>8</sub> Com 202	<b>5</b> ,	R <sub>2</sub>	23	Relat	ive to	Case 202 T <sub>3</sub>	Relat	ive to C	T <sub>3</sub>
	ac Print	Barai G	© R 2 Z	OB2	825 B	20 20 30 30 30 30 30 30 30 30 30 30 30 30 30	Poble C-6(E)	Toble C-T(k)	C-S(b)	<u></u>	<u> </u>	<u> </u>	<u>୍</u> ଡାଡ	ଡାଡ	<b>8</b> 0
S <sub>E</sub>	83 119 167	49200 46700 38800	15773 18241 10979	-905 163 <b>86</b> 11 <b>8</b> 62	3342 / 324%; 28821	3031 <sup>1</sup> . 27936	11464 10407 1953	16872 19807 50673	851-9 8927 8968	.343 .321 .346	1.402 1.534 1.758	.256 .275 .311	.301 .343 .265	1.555 1.643 1.84	.284 .294 .321
area i	209 275 346	47600 39540 28700	13663 10998 6187	13979 9889 5300	33931 20902 21913	33621 25611 25400	11744 9572 6657	13850 17388 12115	16230 12587 8811	.31 5 .331 .296	1.640 1.923	78 .436	.349 .323 .218	1.483 1.600 1.801	.463 .425
Neg.	380 448 556	27700 1600 6450	9257 5305 2087	76'; 9 4161 1531	1843 10815 4363	20021 12039 4919	97-37 5436 2191	14751 9505 4544	3315 2335 1513	.489 .502 .502	.800 .879 1.040	.180 .216 .347	.451 .451 .445	.737 .789 .939	.166 .194 .308
10 m	83 119 167	13.80 12.17 10.10	4.144 3.604 2.976	3.923 3.298 2.609	9.66 8.57 7.03	9.877 8.872 7.491	3.617 3.223 2.783	14.960 13.219 10.808	3-533 3.219 2.789	.374 .376 .391	1.5kg 1.5k3 1.517	.3% .3% .3%	.366 .363 .371	1.515 1.490 1.442	.358 .363 .372
Darding Masers Blandie Ante	209 275 346	8.30 5-75 3-31	2 458 1.671 1.074	2.000 1.318 .£115	5.84 3.86 2.24	6,220 4,232 2,497	2.369 1.672 1.100	8.697 5.495 2.314	2.260 1.320	.405 .431 .492	1.409 1.417 1.035	.307 .340	.301 .395	1.398 1.298	.363
Mile Person	30 34 34	2.44 .966 .229	.791 .303 .016	.9966 .211A .0534	1.65 .757 .151	1.84 .7966 .1796	. 8299 . 3338 . 0745	1.457 .632 .154	.3744 .1823 .0514	.501 .502 .493	.883 ,950 1.080	.221 .274 .340	.449 .441 .424	.791 .835 .877	.203 .241 .293
10 <sup>-6</sup> 14	83 119	1.130	498 537	-1.519 -1.480	1.628 1.557 1.487	2.50n	.3357 .2245	4.167 4.165 4.114	-1.870 -1.858 -1.855	.206 .144 .052	2.559 2.6?5 2.767	-1.149 -1.193 -1.241	.127 .090	1.573 1.666 1.767	706 743 792
Throise Meson Hisonic Ario	209 215 346	.900 1.266 1.140 1.070		-1.129 908 826 732	1.495 1.411 1.368	2.329 2.168 1.966 1.802	.3495 .2070	3-734 3-668 3-569	40A 369	.236 .147	2.50L 2.600 2.603	271 276 260	.161	1.722 1.865 1.992	157 158 197
AND SELECTION OF S	380 148 536	.15;	052 053 051	270 186 108	.235 .118	.453 .251 .103	.1621 .0844 .0889	.112 .0536 .0125	118 0672 0518	.689 .715	.4% .4% 317	502 569 807	.358 .336 .281	.247 .214 .121	258 309
4	83 78 83 78 96 78	81.5 -785 1080	152 -305 20	-538 538	663 -480 1060	753 -247 1257	210 - 37 158	1310 62 2551	-213 -405 91	.317 .202 .149	1.976 129 2.407	3.1 .840 .091	.279 -393 .126	1.740 251 2.029	263 1.631 .077
	346 ED	-690	-247	-360	-443	-301	- 89	393	-346	.200	067	. 762.	.296	-1.306	1.150

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TABLE C-11. CONCLUDED
(b) COLUMNS 17 - 32

	Rat	io of Des	ign Net L	oads to M.	A. Net Lo	ads		De	sign Net	Loads				Design A. Net	
17	(18)	<u>(19</u>	<b>®</b>	<u>(2)</u>	<b>②</b>	(3)	(24)	<b>(3)</b>	<b>6</b>	<b>(27)</b>	<b>®</b>	(8)	<b>139</b>	<u> </u>	3
Cond.	First Iter. Cond. II	Second Iter. Cond. II	Cond. II	First Iter. Cond. III	Cond. III	First Iter. Cond. IV	Cond. IV	Net Loads Cond. I	Net Loads Cond- II	Net Loads Cond. III	Net Loads Cond. IV	Ratio Cond. I	Ratio Cond. II	Ratio Cond. III	Ratio Cond. IV
1.40(1)	1.742 (L) 1.180 (S) 1.251 (G)	1.80 (1) +.17 (1) +.23 (6)	1.88 (1) +.16 (3) +.20 (6)	.756 (4) •.448 (5) •.042 (6)	.80 (L) +.45 (E)	1,095 (b) •.458 (1) •.187 (6)	.40 4.47 (E) 25 25	©(7) + (4)	<b>7</b> @ •(j	T29	<b>T</b> @	<u>න</u> ල	<u>8</u>	<u></u>	<u>®</u>
.480	1.015 .967	1.015	.967	•973 •983	1.004	1.076	.812 .836		49854 45706	49335 47125	43541 41726	.65 .62	1.01 .98	1	i 1
.386	.903	.895	.390	1.014	1.044	1.082	.886	22113	36715	41027	36618	.56	.92	1	.92
.484	.996	.991	•99€ 01/0	.908 .943	-947 070	.971 1.007	.716	30105 2 <b>3999</b>	47280 37984	45807 38871	38049 32843	.63	.99	.96 .98	.80 .83
.463 .414	-957 -903	.951 .893	.949 .885	1.001	•979 1.032	1.058	.775 .863	15883	26020	29463	25829	.55	.91		.90
.685	.960	.975	1.000	.771	.693	.800	.485		27692	21547	17398	.79	1.00		1
.703	.976	.990	1.014	.686	.716	.819	.503	12995	16368	12787	10219	.80	1.01	.79	.63
.703	1.019	1.031	-1.047	.744	.772	.860	-535	5154	6679	5327	4163	.80	1.04	. 83	.65
.524	1.000	-999	1.002	.940	•975	1.028	.769	9.208	13.823	13.549	11.518	.67	1.00	.98	.83
.526	•992	.990	•994	-927	.961	1.012	.755	8.116	12.116	11.825	9.995	.67	1.00	-97	.82
.547	•999	<b>.99</b> 8	1.004	.912	.946	•998	- 734	6.872	10.128	9.699	8.105	.68	1.00	.96	.80
.567	1.006	1.007	1.012	.699	•934	•990	.719	5-775	8.377	7.889	6.550	.70	1.01	•95	.79
.603	1.000	1.003	1.013	<b>.</b> 867	•900	•969	.690	4.012	5.605	5.128	4.239	.72	1.01	.92	.76
.689	•990	1.001	1.020	-739	.769	.864	•555	2.614	3.361	2.733	2.199	.79	1.02	_	
.701	•975	-989	1.011	.685	.715	.816	.501	1.947	2.459	1.915	1.520	.80	1.01	.78	1
.703	•979	•991	1.011	-697	• 729	.820	•509	•770	.9765	.7628	•5964	.80	1.01	·79	.62
.690	.970	.980	•997	.701	• 734	.811	•509	.1823	.2284	.1823	.1427	.80	1.00	.80	.62
.288	.327	• 334	• 349	.830	.809	.991	.966	0280	5952	.625	1.041	∞	53		.92
.202	.270	.274	.287	.845	.821	1,000	1.005	2227	7632	•574	1.032	22	75	.56	
.073	.177	.178	.186	.850	.821	-993	1.042	4795	9952	.484	-997	55	-1.11	•54	1.11
.328	•543	-539	.541	-902	.904	1.000	.921	.2563	.2656	1.052	1.088	.20	.21	.83	.86
.206	.469	.460	.456	.924	.92h	1.007	.968 1.004	.0188	.0722	.990	1.078	.02	.06 37	.87 .89	.95 1.01
.085	.391 .603	.378 .646	.367 .660	.936 .392	.93 <sup>1</sup> 4	.554	.324	.1749	.0291	0899	1231	-,17 .96	.16	,	67
.965 1.001	.556	.579	.613	.361	• 397 • 365	.516	.302	.0652	0322	0943	1102		50	-1.45	-1.70
1.028	.434	.455	.485	.280	.279	.421	.246	.0031	0510	0723	0756		-25.50	-36.15	-37.80
141414	.728	.733	.746	1.002	1.006	1.155	1.000	446	624	820	815	•55	٠π٠	1.01	1.00
.283	1.049	1.039	1.024	.116	.201	.010	369	-441	-791	-588	-447	.56	1.01	- 75	-57
.209	.604	.589	.576	1.001	1.014	1.053	.985	241	548	1097	1061	.22	.51	1.02	.98
.281	•56 <del>9</del>	•575	-577	410	351	489	783	-372	-563	-283	-153	•54	.82	.41	.22

For the second design condition, an attempt will be made to match bending moments throughout the span, and shears at least in the outer wing. Loads for this condition are produced predominantly by case 202 and may include contributions from all three elementary distributions. For a first estimate, a<sub>1</sub>, a<sub>2</sub>, and a<sub>3</sub> will be determined such as to provide an exact match of bending moments at wing stations 83, 167, and 275. The following equation must be satisfied for each of these three load quantities:

$$L_S = a_1 E_1 + a_2 E_2 + a_3 E_3$$
 or   
 $1 = a_1 \overline{E}_1 + a_2 \overline{E}_2 + a_3 \overline{E}_3$ 

Substituting the values of  $\overline{E}_1$ ,  $\overline{L}_2$ , and  $\overline{E}_3$  from column 14 - 16 for each of the three load quantities in turn yields three equations in the three unknowns,  $a_1$ ,  $a_2$ , and  $a_3$ . Solution of these equations gives:

$$a_1 = 1.742$$
,  $a_2 = .180$ , and  $a_3 = .25$ 

Thus the incremental loads for Condition II as given by this first iteration are:

$$E_0 = 1.742 E_1 + .180 E_2 + .25 E_3$$

A comparison of the complete Condition II loads (at this stage) with the statistically defined design level incremental loads is then indicated by the ratios

$$\frac{I_{D}}{I_{S}} = \frac{1.742 E_{1} + .180 E_{2} + .25 E_{3}}{I_{S}} = 1.742 E_{1} \div .180 E_{2} + .25 E_{3}$$

These ratios are listed in column 18. The ratios for snear and bending moment throughout in span are seen to be close to unity, although tending to be several per cent low in the outer wing. However, by referring to columns 14 through 16, it is seen that outer wing shear and bending can be increased relative to inner wing shear and bending by increasing all and reducing all and all such a modification is therefore made, with the results shown in column 19.

It is seen that a further adjustment in the same direction would provide a further improvement. This is accomplished in column 20.

The ratio of design load to mission analysis load is now approximately unity for all wing bending moments, outer wing shears, and wing shear at wing stations 83 and 209.

Actually, it is unlikely that such a distribution of load would occur at any single instant in flight through turbulence, since this particular combination of static, dynamic bending, and dynamic torsion distributions is no more likely than any one of numerous others, each of which might produce design level values for only a very few of the 31 loads under examination. However, it is noted that no load quantity at any location in the structure has been exceeded; this condition, in effect, then represents an envelope of many possible conditions.

Reference to columns 17 and 20 shows that an adequate match has not yet been achieved for some of the wing shears, all wing torsions inboard of the outboard nacelle, and front beam shear flows. For Condition III, these wing shears and front beam shear-flows will be matched. Here again the pertinent E's are those in columns 14 through 16. The initial iteration for Condition III is shown in column 21, where a<sub>1</sub>, a<sub>2</sub>, and a<sub>3</sub> are selected such as to provide an exact match for shear at W.S. 346 and front beam shear flows at W.S. 83 and 346. A further adjustment yields the results shown in column 22. This condition represents a predominantly dynamic distribution of load. Load quantities matched are shear at W.S. 83, 167, 275, and 346, and front beam shear flows at W.S. 83 and 346. The wing bending moment ratios vary from about .73 at the tip to .98 at the root. For wing torsion, the ratios are .92 between nacelles and .82 inboard of the inboard nacelle.

Condition IV is included in order to match the wing torsions inboard of the outboard nacelle. The first iteration for condition IV is shown in column 23, based upon an exact match of wing torsion at W.S. 119, 209, and 346. Final condition IV load ratios appear in column 24, where it is seen that front beam shear flows at W.S. 83 and 346 and wing torsions inboard of the outboard nacelle are matched.

A quick review of columns 17, 20, 22, and 24 of Table C-11 indicates that all of the loads listed - except rear beam shear flow at W.S. 346, which will be shown later to be of negligible consequence - have been closely enveloped by one or more of the four design conditions. Closer examination of these numbers, however, is needed to assure that critical phasings have been achieved.

The power-spectral density information contained in Figure 9-3 and Table C-2 as well as the breakdown between mission segments indicated by Figure 9-9(b) and Table C-1, can assist in this examination. However, the most direct information on phasing is provided by the match of internal loads or stresses, either in actual structural elements such as the front and rear beams or in fictitious structural elements as discussed in Section 11.2.

The match of front beam shear flows for Conditions III and IV indicates that, for the wing inboard of the outboard nacelle, Condition III contains an appropriate amount of torsion with its design-level shears, and Condition IV contains an appropriate amount of shear with its design-level torsions.

However, phasing of bending moment and torsion is also important - from the standpoint of strength of the upper and lower surfaces. In order to check the adequacy with which this phasing is represented, as well as to provide a more complete picture of the shear-torsion and shear-bending phasings, use is made of the "equal probability", or phase-plane, ellipses shown in Figure 11-2. Conditions I - IV as generated in Table C-11 are shown spotted in on the ellipses. In spotting in these conditions, it was necessary to ratio down the design condition values to account for the fact that the total increment (relative to the case 202 one-g loads) due to all mission segments is greater than the increment for case 202 alone. To accomplish this, the values plotted were obtained by taking the ratios shown in columns 17, 20, 22, and 24 of Table C-11 and multiplying by the corresponding maximum load values indicated on the ellipses. Thus, in plotting the Condition IV shear-torsion point at W.S. 83 on Figure 11-2(a), for example,

$$S_z = .812 \times 28400 = 23000 \text{ lb.}$$

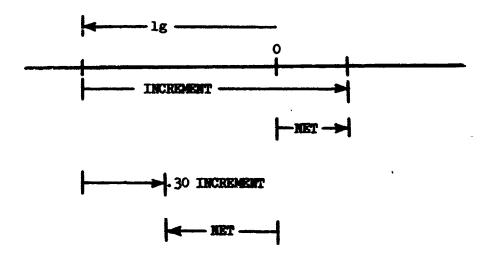
$$M_y - .966 \times 2.10 \times 10^6 = 2.03 \times 10^6 \text{ in.lb.}$$

It is seen that Conditions I through IV excellently represent the equal probability combinations of positive bending moment, shear, and torsion.

To assure that the excellent match indicated on an incremental basis in columns 17, 20, 22, and 24 of Table C-11 is preserved when the one-g loads are added, similar comparisons on a net-load basis are shown in columns 29 - 32. These are based on the net loads for each condition indicated in columns 25 - 28.

For Condition I, the match of outer wing torsions is seen to remain excellent (column 29). The value 1.55 for the ratio at W.S. 516 has no significance, since the net torsions are very small. The difference between the statistically defined and the Condition I net torsion, while 55% of the statistically defined net torsion, is less than 3% of the incremental torsion.

The Condition II shears and bending rowents match at least as well on a net load basis as on an incremental basis. The rather drastic change in the torsion ratios is a natural consequence of the one-g and incremental values having opposite sign and is not of concern, as can be seen from the following sketch:



For Condition III, as for Condition II, the match of the pertinent quantities is seen to be at least as good on a net load as on an incremental load basis.

For Condition IV, the match of torsions is slightly less good on a net load basis than on an incremental basis. However, the good match of front beam shear flows is retained.

It is therefore concluded that, on a net load as well as an incremental load basis, the enveloping of the statistically defined loads by the design conditions is satisfactory.

### C.5 Downbending Conditions

Design loads for the downbending mission analysis conditions were obtained in a manner similar to that just outlined for the upbending conditions. Mission analysis net loads for the case of downbending are given in column 3 of Table C-12, and the resulting incremental loads are given in column 4. For each design condition the ratio of design incremental load to mission analysis incremental load appears in columns 5 through 8. These are designated as Conditions V, VI, VII, and VIII respectively. The appropriate downbending design condition points are then shown on the phase plane plots of Figure 11-2, with the same adjustment included as described above for the upbending conditions. It is seen that, as for the upbending conditions, Conditions V through VIII excellently represent the equal probability combinations of negative bending moment, shear, and torsion.

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A comparison of the downbending design conditions with the statistically defined loads on a net load basis appears in columns 9 - 12 of Table C-12. As in the case of the upbending conditions, the agreement is generally as good on a net as on an incremental load basis. The large values of the ratio for rear beam shear flow are associated with opposite signs for the one-gload and the increment; consequently, they are not of concern. In all cases, the largest value of the ratio, times the statistically defined net load, gives a load that is smaller (arithmetically) than the net load for the upbending conditions shown in Table C-11.

### C.6 Loads in Other Quadrants

It will be observed that design conditions have been defined for upbending and downbending conditions. Actually, consideration must be given to four rather than two types of condition - up and down bending, each combined with positive and negative torsion. In other words, in the phase-plane plot of Figure 11-2(f), for example, consideration must be given to possibly critical conditions in all four quadrants. The general shape of the ellipses shown in Figures 11-2(a), (c), (d), and (f), however, suggests that the upper left and lower right quadrants are not likely to be critical; and examination of the design load envelopes based on all the conditions to which the airplane was originally designed confirms this conclusion. Even if the procedure described herein had been employed in the original design of the Model 188, one could probably have established at an early stage that other conditions would be more critical in these quadrants than the power-spectral gust conditions.

TABLE C-12. DOWN BENDING DESIGN CONDITIONS, MODEL 188

											<del></del> 1
1	ten	Mission Am	lysis Loads		utio of Design Loads To M.A.			7	ntio of Deci		
0	<b>②</b>	<b>①</b>	0	<b>③</b>	<b>©</b>	<b>①</b>	0	0	69	(i)	(g)
Joed 1		Net Loads Mission Analysis	L <sub>a</sub> Case 202	Cond. Y	Cond. VI	Cond. VII	Cond. VII	Comit.	Comd. VI	Cond. VII	Cond. VIII
	N.S. (1m.)	Prequency of Encedance Curves	<b>③</b> - <b>③•</b>	2.135 <b>()</b> - (i)	(1.61 <b>(6)</b> +.17 <b>(6)</b> +.36 <b>(6)</b> - <b>(6)</b>	(1.05 <b>@+</b> +.39 <b>@+</b> ) - <b>(</b> )	(.65 <b>@*</b> •.43 <b>@*</b> •.10 <b>@*</b> ) - <b>(</b>	$\begin{array}{c c} \bullet & \\ \bullet & \\ \hline \bullet & \\ \hline \end{array}$	(O)	() () () () () () () () ()	( <b>()</b> ( <b>()</b> () () () () () () () () () () () () ()
5,	83	-12100	-32155	. 181	.948	.974	.859	.46	.87	- 93	.64
-	119	-14200	-30586	.726	.930	.992	.892	.41	.85	.98	.77
Ì	167	-16000	-27862	.609	.885	1,009	-935	.32	.80	1.01	.89
3	209	-19400	-33379	-751	-995	.952	.822	-57	.99	.92	.69
1	2175	-19200	-29089	.703	.963	.980	.871	.55	.94	.97	.80
3	346	-17200	-22500	.617	.924	1.034	.954	.50	.90	1.04	.94
3	380	-11100	-19079	1.011	-95T	. 199	.623	1.02	.93	.67	-37
	148	- 7150	-11311	1.026	.991	.832	.653	1.04	.98	•73 ~0	.45
	516	- 3250	- 4761	.978	1.013	. 852	.675	.97	1.02	. 78	.52
10 <sup>-6</sup> Ne	83	-5-55	-9.473	.815	1.017	1.017	.890	.68	1.03	1.03	.81
_ و	119	-5.25	-8.548	.805	)005	-999	.872	.68	1.01	1.00	.79
T S	167	-4.70	-7.309	.813	1.002	.976	.845	•72	1.00	.96	.76
	209	-3-95	-6.030	.839	1.013	•975	.838	•75	1.02	.96	•75
Election 2	217	-2.70	-4.018	.866	1.021	.970	.826	.83	1.03	-95	- 74
	346	-1.57	-2.302	.986	,993	. 864	.694	.96	.94	•79	.46
Ving About	380	-1.14	-1.739	1.01	.985	.825	.661	1.02	.98 1.00	•73 •77	.52
34	448	500	7114	1.002	-999	.839 .846	.670	1.00 .96	1.01	-77	.51
-	516	110	1634	.973	1.007	.907	1,007	.60	.57	.94	1.00
10 <sup>-6</sup> 7	83	-3.70	-2.181	.329	.193	.894	1.007	•55	•53	.94	1.01
# -	119	-3.56		.083	.081	.855	1.017	.47	.46	.91	1.01
Monent c Arte	167	-3.40	-1.971	.352	•553	.959	,985	•59	.70	.97	.99
1 2 3	209	-2.81	-1.754	.252	.466	.939	,998	.49	.64	.96	1.00
Torsion M	275	-2.58	-1.626	,110	.379	.914	1,003	•39	.57	.94	1.00
	346 380	-2.36 615	345	1.003	.689	.620	.479	1.00	.82	.79	.71
Ving About	448	360	174	1.036	.695	.630	.487	1.02	.85	.82	.75
1 5 3	516	165	064	.96A	.581	.551	.427	.99	.84	.82	.87
	83 73	- 666	- 728	.616	.665	1,005	.991	.58	.63	1.01	.99
1 . 5 .	83 RB	- 150	+ 388	.534	.749	.200	010	2.87	1.65	2.87	3.61
1 2 5 E	346 FB	-1350	-1173	.288	.616	.990	1.014	.38	.40	.98	1.01
~ ~ ~ ~	346 RB	- 30	+ 359	.529	.560	167	406	6.64	6.26	14.96	17.82
1	مس سر ا	, - ~	' "	1		1	ł		<u></u>	<u> </u>	L

<sup>\*</sup> Denotes column in Table 11-11

It is because the upper left and lower right quadrants are clearly non-critical that rear beam shear flows could be disregarded in generating the design conditions. In the critical upper right and lower left quadrants, the shear flows due to shear and torsion add in the front beam and subtract in rear beam. Only in the other two quadrants, which have been established as not being critical, do the shear flows due to shear and torsion add in the rear beam.

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TABLE C-13. UPBENDING DESIGN CONDITIONS AT STRESS ANALYSIS STATIONS, N(y) = 10<sup>-5</sup> CYCLES PER HOUR, MODEL 188

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	() E	Condition I Outer Wing Loads)	I Losda)	Col	Condition II (Max. Wing Bending Mom.)	S Mer.	(Par. So With White Par.	Condition III Permissable Torsion Max. Shear-Bending)	II Torston Bending)	() () ()	Condition IV (Max. Wing Torsion)	V ston)
¥, S.	5-31 81	10 <sup>-6</sup> M2 In1b	10 <sup>-6</sup> M, In1b	10 <sup>-3</sup> s. Id	10-6 K	10-6 M	10-3 s	10 <sup>-6</sup> M	10-6 K	10 <sup>-3</sup> 8 <sub>3</sub> Ib	10 <sup>-6</sup> M <sub>k</sub> Im1b	10 <sup>-6</sup> n, 12,-15
\$	En a	4.6.6	-1.148T	50.409	15.039	-2.4537	149.941	14.736	-1.2315	13.611	12.569	6479
럿	\$ 390	8.776	-1.2208	19.300	13.222	-2.4529	19.388	12.938	-1.2112	43.472	20.979	5961
137	26.903	7.15	-1.1932	6w284	n.5n	-8.318t	18.54	11.245	-1.0822	10.223	9.483	4587
<u>k</u>	28.08	6.977	-1.0006	×.€.	10.349	-2.1051	¥0.986	9.983	89et	36.587	8.305	2760
167	27.922	6.977	-1.007t	84.4	10.349	-1.8649	15.80E	9.923	1010.	39.447	8.30%	Mar
273	27.331	6.689	9689	43.803	108.6	-1.79%	15.037	9.361	76tu	\$.6£	7.820	32.39
761	86.115	6.187	9706	<b>₩.40</b> 00	9.067	-1.6839	43.634	8,603	6556	37.26.	7.176	2017
508	24.945	5.841	85k3	11.033	8.523	-1.60h1	12.32T	3.04	5767	36.000	6.693	1235
\$60	30.618	5.041	e4TT	47.980	8.523	-1.4092	16.163	8.0kt	58th	38.276	6.693	2656
638	<b>इ</b> म. जु	1.943	7102	43.04g	7:184	-1.2519	45.647	6.679	4240	35.541	5.553	1197
273	83.999	4.046	TIRT	37.98		-1.1467	38.871	5.234	- 3061	32.843	まず	83t
£	8.3	3.618	6872	34.967	3.012	-1.0645	36.361	1.535	2212	31.135	3.749	+.0483
8	16.969	2.939	6a.8	PT.648	3.911	¥69.	30.991	3.45	0300	26.770	2.733	+.213+
36	14.822	2.668	3567	24.537	3.170	- 7687	28.583	2.941	£ .0603	24.066	8.296	+. 2929
346	19.887	2.668	5113	27.000	3.470	9781	114.69	2,841	a154	21.173	2.296	3227
789	19.621	2,000	1564	27.372	2.537	70T	Pt. 389	1.983	3397	80.892	1.583	2207
<b>30</b> 0	22.376	8,000	- : 443	26.349	2.537	. 13.59	22.953	1.983	Tone	17.703	1.583	619e
<b>1</b>	20.188	1.650	Stote -	25.810	2.00%	- ,6809	19.924	1.635	6897	36.065	1,304	5573
124	15.258	7,086	3037	19.172	1.308	5145	14.929	1.030	- 14805	11.968	.8250	4253
\$65	10.73	.5707	2167	13.566	. 13TR	3692	10,645	.5809	1. サイナ	대	.4532	30T9
<u>\$</u>	6.707	.2651	1365	3.0	. STA	2476	6.855	.2953	9968" -	r.	1622.	8091
333	3.68	1831.	erro	4.72	:1673	1107	3.797	.1372	1363	12, 3	m.	120h
Ŕ	ŝ.	oros.	an	<b>3</b> 6	.0063	021.8	.623	.0072	0803	874.	\$8.	orth
					The state of the s	T						

TABLE C-14. DOWN BENDING DESIGN CONDITIONS AT STRESS ANALYSIS STATIONS N(y) = 10-5 CYCLES PER HOUR, MODEL 188

Loads are with respect to arbitrary load axis at 7 8 573.2

	() See .	Condition V Outer Ving Londs)	V Tonde)	() Park. Will	Condition VI Ving Bending		(Mer. Se	Condition VII Persionable forton Max. Shees-Bending)	VII Le foreson - Bending)	() () () () () () () () () () () () () (	Condition VIII (Nax. Ving Torelo	on VIII Toreion
%. B.	10°3 s.	10-6 Kg IB13	10.0 K	10"3 g.	10 <sup>-6</sup> K	10°6 K	10°3 e.	10° K	10° k In-11	10°3 s	6 4 4 4 4 4	2 4 2 4
æ	- 4.099	-3.70	-8.3670	- 8.605	-5.7dt	-2.1057	- 9.027	-5.765	-3.4620	- 5.454	. b.	-2-7861
<b>5</b> .	- 6.86T	-2.264	-2.0394	-18.32r	-5.427	-1.7303	-13.538	₹.°	-3.1066	18.6 -	P. 200	984-8-
'n	- 5.8n	-3.359	-1.7703	-12.517	-1.96	-1.4761	-14.969	1:02	-2.0mo3	-18.16	.3.616	-3.2747
Ř	- 5.43	-3.191	-1.9961	-12.TC	-h.626	-1.834	-16.803	-4.410	-2.6eor	-14.164	-3.490	-2.96K
191	- 6.130	-3.191	-1.6804	-14.533	-4.616	-1.4883	-15.24	977.1	-2.XE7	-12,000	-3.450	-2.6355
<u></u>	- 7.9%	197.5-	-1.5872	-16.037	-4.149	-1. MOT	-16.957	1.92	-2.4729	-13.906	-3.33	-e. 745;
2	T9.6 -	-2.986	-1.4048	-17.766	-4.104	-1.5701	-18.609	-3.863	-2.3517	-15.250	-3.005	-2.6233
Ş	-10.00	-t. 016	-1.355	-18,967	-3.986	-1.8009	-19.896	\$	-2.2TEL	-16.563	-1.066	あまっ
\$	-11.078	-1.016	-1.3460	-19.8ho	-3.986	-1.3164	-18.83	\$	-2.1167	413.TT	-1.066	たあって
8	-11.307	-t.5%	-1.1kg	-19.431	-3.370	-1.1582	-18.8a	-3.172	-1.9783	-14.940	.2.169	-2.1711
E	-10.94T	-2.116	9tto	-18.109	-2.672	-1.0637	-13.643	-2.476	-1.8539	-15.451	-1.900	-2.0586
8	· 9.23	-1.931	.900	-17.838	-2.37k	-1.0140	-18.361	-2.163	-1.7%	-15.555	-1.60	-1.9879
R	- 7.076	-1.60t	TB	-15.173	-1.765	93%	-17. b19	-1.493	-1.6933	-15.509	-1.055	-1.879
*	- 6.933	-1.47ê	10CT	-14.94	1.24		-16.905	-1.500	-1.64%	-15.390		-1.68%
Ž	-6.9T	-1.476	- ,3946	-10.686	-1.514	630T	- 9.50	-1.700	- SETA	- 7.009	7980	-1.00%
<b>8</b>	-12.40	-1.157	3863	-14.165	1:0%	103	-13.151	0000	. TB03	-10.27	*.50%	gr
ķ	-12,36	-1.157	1966	-11.185	-1:039	ESG	- 6.034	Broo		- 1.567	50%	\$
¥	-17.664	39.6.	8468	-10.436	1606	1994 -	- 7.6%	e.16.	24.53	- b.kT3	4215	. 2669
Ħ,	- 8.658	6122	<b>8</b> 02: -	- 6.062	4909.	- 15kB	- 5.972	600	- 1938	. 2.603	2959	23
Ž	- 6.830	ST36	. 1579	a£0.9 -	arak: -	- 1158	4.54	895	1433	- 2.96	8007	1643
ş	- 1.067		on	- h.214	1981 -	6	- 3.218	1521	1116	- 2.19	1343	1150
ž	- 2.20	0%	· oms	- 2.411	. 0395	80.	- 1.061	047		- 1.863	0837	06TB
Ŕ	- ,700	9000.	0076	\$9	6000.	005T	24.	. cm3	ron.	94.	• .0000	100

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### APPENDIX D

# APPLICATION OF THE MATCHING CONDITION TECHNIQUE TO THE MOJEL 188 FUSELAGE (VERTICAL GUST LOADS)

The procedure for matching statistically defined fuselage loads with discrete design load conditions is basically identical to the method used for the wing. As applied to the fuselage, however, the procedure is very much simpler, as a result of the absence of torsion and also the absence of aerodynamic and inertia loads resulting from elastic deformations.

The statistically defined loads resulting from the Model 188 mission analysis are used in illustrating the matching technique. The level of the statistically defined loads were established at a frequency of exceedance of 10<sup>-5</sup> exceedances per hour. This level is the same as used for the wing in Appendix C. The loads are read from frequency of exceedance curves similar to that of Figure 9-9(d) for each of the ten fuselage loads and the horizontal tail load. Table D-1 summarizes the resulting loads in both the upbending and downbending directions. For the purpose of illustrating the technique, however, only the downbending loads will be matched.

### D.1 Nomenclature.

The nomenclature used to illustrate the method for obtaining Juselage load distributions is basically the same as given for the wing in Appendix C. The following specific definitions differ from those used in Appendix C:

- $\mathbf{E}_{1}$  Elementary distribution for unit translational acceleration
- $\mathbf{E}_{\mathbf{p}}$  Elementary distribution for unit pitching seceleration
- E. Elementary distribution for tail aerodynamic load
- E<sub>h</sub> Elementary distribution for body aerodynemic load
- Ratio of load in translational acceleration elementary distribution to statistically defined load
- $\overline{E}_2$  Ratio of load in pitching acceleration elementary distribution to statistically defined load
- E<sub>3</sub> Ratio of load in tail aerodynamic load elementary distribution to statistically defined load

TABLE D-1. FUSELAGE MISSION ANALYSIS NET LOADS AT N(y) = 10-5 EXCEEDANCES PER HOUR, MODEL 188

Θ	0	<b>©</b>	<b>a</b>	<u>©</u>
	Боипре	Downbending Loads	≑પૂર્વેΩ	Uphending Ioads
Fuselage Station	82 911	w. or got	8 <b>2</b> 41	M 10 <sup>6</sup> InLb
350	-31000	£8°η-∵	10900	1,72
500	0086tt-	-10.75	18200	3.85
57.1	00009-	-14.60	22000	5.25
569	-43700	8.6	2200	3.47
1000	-20100	5.20	-2350	-1,66
Horiz Teil	-28700	ŧ	13800	ı

- $\overline{E}_{l_1}$  Ratio of load in body aerodynamic load elementary distribution to statistically defined load
- $\mathbf{a}_h$  Loading coefficient for elementary distribution  $\mathbf{E}_h$

### D.2 Preliminary Considerations.

As in the development of wing loads, the determination of fuselage design load conditions divides naturally into two distinct parts. First, the "elementary" or "unit" distributions are developed. Second, these are used to generate one or more design load conditions, such as to envelope closely the statistically defined loads resulting from the power-spectral analysis.

Before the elementary distribution can be developed, it must be decided which mission segment or segments these should be based upon. From frequency of exceedance curves similar to that of Figure 9-9(d), it is observed that case 202 is the major contributor to the shear and bending moment at the five fuse lage stations, with the exception only of shear at FS 1000 and bending at FS 695. At these two stations, Case 208 contributes very slightly more than Case 202 to the load exceedances.

Downbending loads for the total mission and separately for mission analysis case 202 are summarized in Table D-2 at the selected frequency of exceedance of 10<sup>-5</sup> cycles per nour. In Table D-2 total mission net loads are shown in Column 3. Loads due to mission analysis case 202 slone, at the same frequency of exceedance of total flight, appear in column 4. Che-g loads for mission analysis case 202 are shown in column 5. The resulting "gust incremental" loads are shown in columns 6 and 7. In column 6 the gust increment is taken as the difference between net load based upon all mission segments and the one-g load for Case 202. In column 7, the gust increment is the increment for the given mission segment alone. Column 8 shows the ratio of gust increment due to segment 202 alone to the total gust increment based on all segments.

In column 8, the ratios for shear and bending are all approximately .95, with only the shear at FS 1000 being slightly less at .92. It can be concluded that if design conditions were to be generated to match the gust incremental loads for condition 202 alone (column ?), these could be "ratioed up" by dividing by .95 and would closely reproduce the column 6 incremental loads. Ther, if the condition 202 one-g loads were to be added, a match of the net loads of column 3 would result. Thus, to obtain a match to the statistically defined net loads, only the gust increment need be considered, and this can be confined to condition 202.

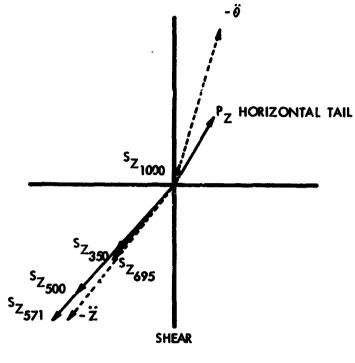
TABLE D-2. MISSION ARALYSIS LOADS AT N(y) = 10-5 EXCEEDANCES
PER HOUR. MODEL 188

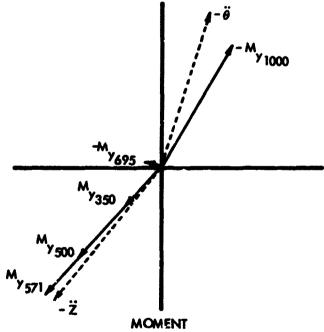
				T			~~			T				
}	@	Retio	8	.952	6ų ₹•	.939	.955	.917	.955	846.	.952	.939	446.	956
	<u>6</u>	Incr 202	<u>ග</u> - ල	-19815	-31930	-38260	-21260	0939 -	-19082	-3.10	-6.88	-9.22	2.35	3.07
	9	Net Massion Load-One G	<b>9-0</b>	-20815	-33630	-40760	-22260	- 7260	-19922	-3.27	-7.23	ag.6-	2, 49	3.21
FER HOUR, MODEL 188	0	One G Load Case 202	23	-10185	-16170	-19240	-21440	-12340	- 8778	-1,601	-3.52	-4.78	7.32	1.99
EK HOUR,	<b>④</b>		K(y)=10 <sup>-2</sup> 1b	-30000	-48100	-57500	-427co	-19500	-27800	oż.4 -	-10,40	-1h.00	99.6	5.06
*	<b>©</b>	Met Loads Mission Analysis	M(y)=10 / Lb	-31000	- 1980o	00009-	-43700	-20100	-28700	- 4.87	-10.75	-14.60	9.80	5.20
	@	Fuselage Station		350	200	57.1	695	1000	Horiz Tail	350	200	577	695	1000
	Θ	Load			(	tī ' <sup>2</sup>	s	-	u tyu:	qunq	971·	·uI	,οτ '	'AH

As a result of the foregoing considerations, it is concluded that gust incremental loads for the total mission may be obtained by utilizing elementary and one-g distributions derived from a consideration of mission onalysis case 202 only.

It has been observed that the net load levels obtained from the mission analysis depend primarily on the rms or A values, which in turn depend upon the total area under each output power spectral density curve. However, in establishing distributions of loads that might actually occur at particular instants of time, consideration must be given to the shapes of the output power spectral density diagrams.

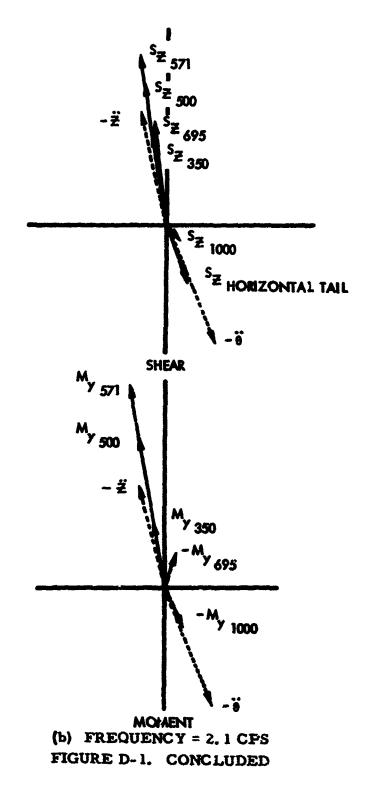
The power-spectral densities for the fuselage loads for Case 202 are shown in Figure 9-4. For the forebody loads, shown in Figure 9-4(a), it is seen that approximately 90% of the area under the curve is due to the response in the 0.4 cps short period mode. The remaining 10% is due to the first wing bending mode response at 2.1 cps. For the aft body loads, except for bending moment at FS 695, Figure 9-4(b) indicates approximately the same breakdown between the short period and wing bending mode contribution. In addition, small contributions are indicated at the wing torsion frequency (4.2 cps) and the elevator flapping frequency (5.6 cps). Bending moment at FS 695 shows a very small response at the short period frequency, due to the offsetting effects of tail airload and the opposing inertia forces. In fact, the characteristic differences between the forebody and aft body responses are due to the fact that the forebody loads are due almost entirely to inertia forces, whereas the horizontal tail serodynamic forces contribute substantially to the aftbody loads. The phase relationships of the transfer functions show this effect quite well. Figure D-1(a) is a vector phase plot of various transfer functions at the short period frequency of 0.4 cps. The vectors represent the magnitude and phase relations of the fuselage loads with respect to a steady state sinusoidal gust input. Also shown are fuselage rigid body accelerations. These are plotted as negative accelerations in order to indicate the phasing of the resulting inertia loads. Looking at the shear plot first, it is apparent that all forebody shears and the shear at FS 695 are approximately in phase with each other but approximately 180° out of phase with horizontal tail load and FS 1000 shear. The forebody and FS 695 shears are obviously influenced predominantly by translational inertia whereas shears on the extreme aftbody are influenced predominantly by the tail airload. This conclusion is confirmed by the moment phase plot. The forebody moments like the shears are seen to be in phase with negative acceleration. The aftbody moments including the roment at FS 695, are seen to be strongly influenced by the tail airload. The bending moment of FS 695 is seen to be small compared to that at FS 1000, reflecting the offsetting effect of





Transfer of

(a) FREQUENCY = .4 CPS
FIGURE D-1. PHASE RELATIONSHIPS OF FUSELAGE LOADS



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inertia and airload noted earlier. The phase plots at the wing frequency of 2.1 cps, shown in Figure D-1(b), show similar relations. The principal difference is in the relative magnitudes of translational inertia, pitching inertia, and tail airload. Vector plots for the other frequencies are not shown since these contributions to net load are relatively small.

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The conclusions which may be drawn from the phase plots may be summarized as follows:

- 1. Forebody loads are predominantly due to inertia.
- 2. Aftbody loads are affected strongly by inertia and tail airloads acting out of phase.
- 3. Pitching inertia loads are relieving on forebody and additive on aftbody.
- 4. It least two matching load conditions will be required to match fuselage downbending loads, one for the forebody and one for the aftbody, since the respective loads are seen to be almost exactly 180° out of phase at the predominant frequencies.
- 5. Bending moment at FS 69, will be difficult to match with the same conditions used to match the other loads because of its unique phase relationship. However, since this load is relatively small, a close matching is not required.

In view of the above, the downbending fuselage loads will be matched by two conditions. In one of these the forebody loads will be matched, in the other, the aftbody loads except at FS 695, will be matched. The shear at FS 695 should be matched by the forebody conditions; bending moment at this location need not be matched, as it is so small as not to contribute significantly to the critical stresses.

### D.3 Elementary Distributions.

It is now possible to proceed to the generation of the elementary distributions.

The method of obtaining fuselage load distributions departs slightly from that used for the wing at this point, partly for simplicity and partly to illustrate a variation in the approach. It will be recalled that, for the wing, three elementary distributions were used - one based upon a static response and two based upon dynamic responses. These

elementary distributions included both inertia and aerodynamic loadings. For a comparable method on the fuselage, the dynamic distribution would not be required since the fuscalage is assumed rigid. However, two or more static distributions would be required in order to account for the relative phasing of translation acceleration, pitching acceleration, and aerodynamic loads on the body and tail. In order to avoid this complication, the elementary distributions were taken simply as unit airload and inertia distributions. The fuselage loads for any condition, gust or otherwise, can be regarded as produced by four parameters - (1) translation acceleration, (2) pitching acceleration, (3) tail and elevator air load, and (4) body air load. The elementary load distributions are simply the fuselage load produced by unit values of each. These exementary distributions are given in Table D-3(a) and D-3(b) for fuselage shear and moment respectively. These are basic unit loads and require ne particular technique to develop. Columns 2 and 3, E1 and E2, depend only on the airplane weight data. Column 4, E3, depends only upon the tail load center of pressure (no balancing inertia being included). Column 5, Eq, depends only upon the original assumption used for distribution of airload along the fuselage (again, no balancing inertia being included). Also shown in Table D-3 are the one-g flight loads for Case 202.

### D.4 Fuselage Downbending Conditions.

With the mission analysis loads of Table D-1, the elementary distributions of Table D-3 and the one-g flight loads of Table D-3 all available, discrete distributions of the fuselage may now be generated. This is accomplished in Tables D-4 and D-5. The procedure is identical to that described for the wing in Appendix C, Section C.4 with the exceptions that four elementary distributions are used instead of three, and only one one-g flight load condition need be used.

In Table D-1, the statistically defined load levels which it is desired to match appear in column 3. These are taken from columns 2 and 3 of Table D-1. As pointed out earlier, in Appendix D, Section D.2, only the Case 202 one-g flight loads need be considered. Thus only the incremental statistically defined loads as given by the Lg in column 5 (the difference of columns 4 and 3) need to be matched by combinations of the elementary distributions.

The elementary distributions given in Tables 0-3 are shown in columns 6-9. These distributions are designated the  $E_1$ ,  $E_2$ ,  $E_3$  and  $E_4$  distributions.

TABLE D-3. FUSELAGE ELEMENTARY LOAD DISTRIBUTIONS
CASE 202
(a) SHEAR

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<b>①</b>	<b>②</b>	3	<b>(</b> 4)	<b>⑤</b>	6				
Inboard Fuselage Station	Unit	Inertia	Unit Tail Airload	Unit Body Airloads	One G Flight Loads				
	E	B <sub>2</sub>	<b>R</b> 3	E <sub>l</sub>					
	S <sub>z</sub> /n <sub>z</sub>	S <sub>z</sub> /6	Sz/PzT	Sz/Pzarwo	s <sub>z</sub> <sub>1-g</sub>				
În.	Lb/G	Rad/Sec <sup>2</sup>	њ/њ	S <sub>z</sub> /P <sub>zAAFT</sub> Lb/Lb	Lb				
			FOREBODY						
42	0	0	0	0	0				
177	4500	- 5580	0	.255	- 4500				
200	5310	- 6417	0	.298	- 5216				
300	8677	- 9 <b>3</b> 68	0	.487	- 8524				
400	12064	-11456	0	.677	-11852				
417	12893	-11842	0	.709	-12670				
500	16439	-13034	O	.868	-16169				
571	19559	-13459	0	1,600	-19242				
AFTBODY									
695	16845	15663	1,000	1,000	-21437				
768	14219	14692	1.000	.825	-19306				
800	13218	14137	1.000	.750	-18430				
900	9731	11832	1,000	.513	-15704				
953	7968	10233	1,000	. 388	-14236				
1000	6118	8420	1,000	.275	-12603				
1117	2470	3946	1,000	0	- 9899				
1158	1890	3119	1,000	0	- 9319				
1186	1500	2528	1,000	0	- 8929				
1292	С	v	0	0	0				
<b>1</b>	<b>.</b>		L						

TABLE D-3. CONCLUDED
(b) MOMENT

<b>①</b>	2	3	<b>(</b> 4)	<b>⑤</b>	6				
Inboard Fuselage Station	Unit Ine	rtia	Unit Tail Airload	Unit Body Airloads	One G Flight Loads				
	E <sub>l</sub>	E <sub>2</sub>	<b>R</b> 3	E <sup>j‡</sup>					
	My/ng	и₃∕0	My/P <sub>ZT</sub>	My/P <sub>ZAFwd</sub> Or My/P <sub>ZAAft</sub>	М <sub>у 1-g</sub>				
În.	10 <sup>6</sup> InId/g	10 <sup>6</sup> In-Lb Rad/Sec <sup>2</sup>	InIb/Ib	InLb/Lb	10 <sup>6</sup> In12/12				
		FORE	BODY						
42	0	0	0	0	0				
177	. <u>3</u> 04	-377	o	17.2	304				
200	.417	515	0	23.6	409				
300	1,116	-1,304	0	62,8	-1,096				
400	2,153	-2.345	0	121.0	-2.115				
417	2 <b>. 3</b> 65	-2.543	0	132.8	-2.323				
500	3.582	-3.575	0	198.2	-3.519				
571	4.860	-4.516	C	264.7	-4.777				
AFTBODY									
695	-4.262	-5.006	-512,8	-210.5	7.317				
768	-3.112	-3.883	-439.8	-144.1	5.810				
800	-2.675	-3.420	-407.8	-118.9	5.205				
900	-1.532	-2.123	-307.8	- 55.7	3,499				
953	-1,065	-1,538	-254.8	- 31,6	2,706				
1000	693	-1,044	-207.8	- 16.1	1,989				
1117 🕝	216	358	- 90.8	0	.728				
1158	127	- ,213	- 49.8	0	. 335				
1186	- ,080	134	- 21,8	0	.080				
1292	0	0	0	0	0				

<sup>\*</sup>Center of pressure to be FS 1207.8 (average of tail and elevator)

TABLE D-4. DETERMINATION OF LOADING COEFFICIENTS FOR FUSELAGE DOWNBENDING DESIGN CONDITIONS, MODEL 188
(a) COLUMNS 1 - 13

Patio	<b>©</b>	pá	xo3	(O)	0e796	02581	02453	O4492 O4492	03788	•	027to	02744	02696	08454	0502
Distributions	<b>©</b>	<b>M</b>	x103	$^{\odot}$ / $^{\odot}$	•	1	•	Oth92	1.15981377	109205020	•	í	•	2059408454	3240 06474 00502
ry Distr	<b>©</b>	<b>194</b>		$\mathfrak{G}/\mathfrak{G}$	. 5001	.3876	.3302	7036	-1.1598	1092	.5566	.4952	.4603	-2.0120	3240
Elementary	<b>9</b>	μď		©/@	498z	4888	€624	7567	8427	0626	1664*-	4564	6464	-1.7116	-,2159
88	<b>©</b>	Ť	5 S	Table 15-3 col (3)	.588 88.	88.	1.000	3.000	.275	1	9680000*	.000198	.0002647	4.02105	00020780000161
Distribution	9	<b>. . .</b>	ğ -",	Con (O)		•	ı	1.0	2.0	1.0	•	1	,	0005128	0002078
Remote of D	0	M	집	e vIng.	-13.	-1303	-13459	15663	<b>6</b> 450	2.76	-1.8	-3.58	-4.52	-5.01	-1.04
ā	9	af	Page "	rable P-3 col (2)	10371	<b>3€</b> ₹91	19555	16845	6118	1248	1.634	3.582	98.4	-4.262	693
Loads	<u>ග</u>	,şº	Case 202	Calculation of the contraction o	-20815	-33630	-40760	-22260	-7260	-19922	-3.27	-7.23	-9.85	2.49	3.21
sion Analysis Loads	@	One G	ನ್ಯು ಕಾಣ	Table D-3 col (6)	-10185	-15170	-19240	-21440	-12840	-8778	-1.601	-3.52	-4.78	7.31	1.99
	<b>©</b>	Net	Mission Analysis	Toble D-1	-31000	-49800	00009-	-43700	-20100	-28700	-4.87	-10.75	-14.60	8.8	5.20
Item		Puselage				88	172	695		Rorix	350	8	77.5	695	1000
	Θ				Į,	Q Q <b>QQ</b>		*S	Ve I		Jnse GI-	ok ai	901 Sur	pua	ei N

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TABLE D-4. CONCLUDED (b) COLUMNS 14 - 19

Retio - Design to	Hission Analysis Loads	<b>ග</b>	Down Gust		@ / @	)		181	352	361	052	1.000	1.019	12£'	- 329	337	. 842	.965
Bat to	Mission An	<b>(9)</b>	Up Gust		ල / මු			\$66.	1.011	1.01	1.000	.413	385	786.	.993	1.001	. 795	095
	Design Net Loads	ക	Down Gust		⊕ ÷ ® ©			26101	17527	21683	2274	-20100	-29260	1,561	3.536	4.922	8.254	5.017
	Design N	<b>ම</b>	Up Gust		(a) + (b)	)		<b>₹80£</b> ~	-50338	-60672	-43700	-8309	9132	908*†−	-10.678	-14.620	7.80	-4.95
	Ratio Incremental Loads	<b>(</b> )	Down Gust	5.5634 ᡚ	æ. ⊕ ‰.	-24396.7 <b>(3</b> )	-4782.4 🕥	616	-1.002	₹00::-	861	1.000	1.028	196*-	976	988	.379	. 943
	Ratio Incres	<b>(1)</b>	Up Gust	<b>Φ</b> ηξ95'2·	v	+21817.3	+4254.4	:665	1.016	1.017	1.000	+.62h	899	186.	o66·	1.002	167.	774
:	Item		Puselage	Station				350	28	22	695	1000	Horis Teil	350	8	11.5	<b>8</b>	1000
	ï							ı			,2 <sub>6</sub>	3.10	A	ans GI-,	nī	9- <sup>0</sup>	t pu	√N ≫E

TABLE D-5. FUSELAGE DESIGN LOADS, MISSION ANALYSIS,  $N(y) = 10^{-5}$  EXCEEDANCES PER HOUR

	Up G	ust	Down	Gust				
Fus	$s_{Z}$	и <sub>Y</sub>	s <sub>Z</sub>	М <sub>Y</sub>				
Sta	Lb	10 <sup>6</sup> InLb	1Jb	10 <sup>6</sup> InLb				
	a <sub>1</sub> = -2.5634	a <sub>2</sub> =3292	a <sub>1</sub> = 2.5634	a <sub>2</sub> = .3292				
	-3- 21817	a <sub>4</sub> = 4254	a <sub>3</sub> = -24397	a <sub>4</sub> = -4782				
		Forebody						
42	С	0	0	0				
177	-13114	<b>~.</b> 886	3979	.269				
200	-15447	·-1.208	4858	.378				
300	-25611	-3.260	8306	1.035				
400	-36125	-6.347	12064	2.053				
417	-38805	<b>-6.</b> 983	13091	2.267				
500	-50325	-10.681	17529	3.538				
571	-60695	-14.622	21633	4.929				
Aftbody								
695	-43703	7.897	-2279	8.261				
768	-35265	4.860	-6363	7.971				
800	-31729	3.785	-8107	7.740				
900	-20544	1.173	-13714	6.649				
953	-14408	.248	-16848	5.830				
1000	-8271	493	-20060	5.015				
1117	4287	581	-26665	2.272				
1158	6626	356	-27844	1.154				
1186	8211	146	-28649	<b>.3</b> 63				
1292	0	0	0	0				
		1-g + a <sub>1</sub> E <sub>1</sub> + a <sub>2</sub>	E <sub>2</sub> + a <sub>3</sub> E <sub>3</sub> + a <sub>4</sub> E <sub>4</sub>					
	Values of one	-G loads and E <sub>1</sub> - E <sub>3</sub>	are given on Table	D-3.				

The statistically defined loads, L<sub>S</sub>, are now to be enveloped by one or more discrete conditions. Each of these conditions will be made up of an appropriate combination of the four elementary distributions. The contribution of each elementary distribution will be defined by a value of its respective coefficient, a<sub>1</sub>, a<sub>2</sub>, a<sub>3</sub> cr a<sub>4</sub>; the complete set of loads comprising the condition is then given by the expression;

$$L_D = a_1 E_1 + a_2 E_2 + a_3 E_3 + a_4 E_4$$

For each additional condition a new set of values of the coefficients is determined.

To facilitate determining appropriate values of the loading coefficients, each load for the elementary distributions is divided by its corresponding design level load, Ig. The resulting ratios are designated  $\overline{E}_1$ ,  $\overline{E}_2$ , and  $\overline{E}_1$  and are listed in columns 10 through 13 respectively. Thus a match of the statistically defined load is obtained if

$$L_D/L_S = a_1\overline{E}_1 + a_2\overline{E}_2 + a_3\overline{E}_3 + a_4\overline{E}_4 = 1.0$$

In generating the conditions it will be remembered that the forebody loads were shown to be closely in phase. Consequently, it should be possible to match these loads very closely. In generating the first condition, the forebody loads will be matched, while a match of the extreme aftbody loads will not be expected. In establishing the coefficients for this condition, the Eq distribution (body airloads) was initially ignored because of its small load contribution; a set of three simultaneous equations was solved to give an LD/LS ratio of 1.0 for shear at stations 350 and 695 and for moment at station 571. This gave approximate values of a<sub>1</sub>, a<sub>2</sub>, and a<sub>3</sub>. These were then modified by trial and error to include a value for a<sub>4</sub> roughly consistent with the angle of attack associated with nz and still give good agreement. The resulting values of coefficients and of the ratio LD/Lg that they produce are shown in column 14 of Table D-4. This condition is designated "up gust" inasmuch as it is characterized by a down inertia load factor and up tail load as indicated by the coefficients a1 and a3 respectively. This condition is seen to match all of the forebody downbending loads very well, since the ratios for these quantities in column 4 are all close to unity. Aftbody loads are not matched, but are in all cases lower than the statistically defined loads, as indicated by ratios arithmetically less than unity in Column 14.

Another set of coefficients is generated similarly to match the shear at FS 1000, horizontal tail load, and moment at FS 1000. These coefficients and load ratios are shown in column 15. This condition is designated "down gust"; it is characterized by an up inertia load factor and down tail load as indicated by the all and all coefficients. It is interesting to note that the moment at 695 is not matched very well, as was predicted, and that the forebody loads have load ratios close to negative unity, indicating an incremental upbending load approximately equal to the downbending load. This seems to be quite reasonable.

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To assure that the excellent match indicated on an incremental basis in columns 14 and 15 is preserved when the one-g loads are added, similar comparisons on a net load basis are shown in columns 18 and 19. These are based on the net loads for each condition indicated in columns 16 and 17. It is seen that the agreement is even better than on the incremental load basis.

The final distributed net loads determined for the fuselage are shown in Table D-5 for a fine panel breakdown. These are calculated by applying the appropriate load coefficient to the elementary distributions of Table D-3 and adding the one-g flight loads. These load distributions are plotted in Figure D-2. For comparison, the statistically determined downbending and upbending loads of Table D-1 are spotted in. The downbending loads show excellent agreement; and even the upbending loads show surprisingly good agreement, even though no specific effort was made to match them. This figure gives an excellent indication of the significance of the terms "upbending" and "downbending" and "up gust" and "down gust", particularly on the aftbody.

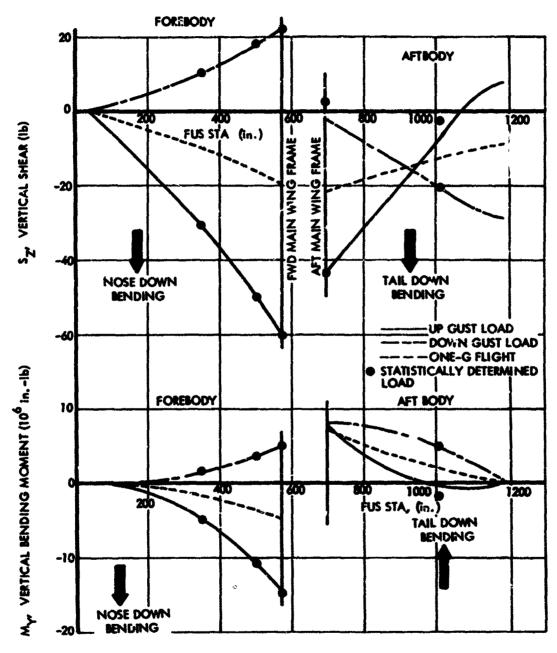


FIGURE D-2. FUSELAGE DESIGN LOAD DISTRIBUTIONS

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### APPENDIX E

# ESTABLISHMENT OF LIMIT-STRENGTH AND ULTIMATE-STRENGTH VALUES OF N(y) AND $\sigma_{\rm W} \eta_{\rm d}$ , MODELS 188 AND 749

## E.1 Model 188 Wing

E.1.1 Mission Analysis, Limit Strength. In Appendix C, a set of eight load conditions was developed for the Model 188 wing such as to envelope closely the statistically defined values of some 31 load quantities. This set of conditions reflected a mission analysis approach and a level of severity defined by a frequency of exceedance of 1.00 x  $10^{-5}$  cycles per hour.

Stress analysis was then conducted for these eight conditions, with the following negative margins of safety resulting:

Wing Station	Panel	Loading Condition	Margin of Safety
101	4	111	05
101	5	II	01
101	5	III	03
137	6	II	<b></b> 05
239	3	II	01
239	3	III	02
239	5	II	02

The negative margins of safety all occurred on the upper surface and resulted from combined compression and shear produced by the upbending conditions. In the table, the panels are numbered from the front beam and are 14" wide; the critical panels are thus seen to be in the deeper part of the box section rather than adjacent to the front or rear beams.

Considering the actual strength of the wing to be reflected by a negative margin of -.04, the frequency of exceedance corresponding to zero margin of safety (i.e., limit strength) is determined as follows. Bending moment at W.S. 119 is taken as representative of the loading in the critical region; its frequency of exceedance is shown in Figure 9-9(b). At  $N(y) = 1.00 \times 10^{-5}$ , where the margin of safety is -.04, the bending moment is 12.1 x  $10^{6}$  in.1b. The zero-margin value is then

 $(1 - .04)(12.1 \times 10^6 \text{ in.lb.}) = 1.6 \times 10^6 \text{ in.lb.}$ 

The value of N(y) corresponding to limit strength is read from the curve at this value of bending moment as 2.1 x  $10^{-5}$  cycles per hour.

It should be remarked that the value obtained for N(y) is not sensitive to the particular frequency of exceedance curve selected, as the shape of the curve doesn't change radically from one load quantity to another.

E.1.2 Mission Analysis, Ultimate Strength. Next, N(y) corresponding to ultimate strength was determined. Based upon the stress analysis for the mission analysis limit conditions, together with an examination of the "unphased" loads at the ultimate level, it could be seen that the phasing of loads reflected by Condition III would be critical for ultimate strength. It was also apparent that only the region of the wing inboard of the outboard nacelle would be critical.

It was estimated that for ultimate strength the exceedance level would be approximately  $N(y) = 5 \times 10^{-9}$ . All wing loads inboard of the outboard nacelle were read from their respective exceedance curves at this level. Phasing ratios were then assumed to be as given by Column 22 of Table C-ll and applied to the unphased loads as read from the exceedance curves.

Stress analysis for the resulting condition led to the following minimum margins of safety:

Wing		Margin of
Station	Panel	Safety
101	14	+.06
239	3	+.07

These both occurred on the upper surface and reflected combined compression and shear.

Again considering bending moment at W.S. 119 to be a representative load quantity and considering the .06 margin to reflect the strength of the wing, the frequency of exceedance corresponding to zero margin, or ultimate strength, is obtained as follows. At  $N(y) = 5 \times 10^{-8}$  cycles per hour,  $M_X = 16.1 \times 10^{8}$  in.lb. (Figure 9-9(b)). The zero-margin value is then

$$(1 + .06)(16.1 \times 10^6) = 17.0 \times 10^6 \text{ in. lb.}$$

The value of N(y) corresponding to ultimate strength is read from the curve at this value of bending moment:  $N(y) = 1.4 \times 10^{-8}$  cycles per hour.

It may be noted that the ratio of ultimate strength to limit-strength values of N(y) is  $(1.4 \times 10^{-8})/(2.1 \times 10^{-5}) = .7 \times 10^{-3}$ .

E.1.3 Design Envelope Criterion. In order to determine the critical design envelope condition for limit strength at  $V_C$ , loads for all of cases 401 through 422 were listed for an estimated limit strength level defined by  $N(y)/N_O = 1.25 \times 10^{-6}$  in Figure 5-8. These were, of course, unphased loads, and were obtained by multiplying the  $\overline{A}$  values listed in Table B-2 by the appropriate  $\sigma_w \eta_d$  values read from Figure 5-8. The  $\sigma_w \eta_d$  values were as follows:

Altitude	o <sub>w</sub> od
0	57
7000 ft.	62
12000 ft.	60
16000 ft.	59
20000 ft.	51

Loads were also listed for the  $V_D$  cases, 423 - 426, at  $\sigma_w \eta_d = (25/50)62 = 31$  and for the  $V_B$  case, 427, at  $\tau_w \eta_d = (4/3)$  62 = 83, where the factor 4/3 is a rounded-off equivalent of 66/50. (Cases 428-431 were not included until later, when it became evident that case 427 would not be the critical  $V_B$  case.) The multiplying factors included in the  $\sigma_w \eta_d$ 's for the  $V_D$  and  $V_B$  cases will be recognized as the ratios of currently specified  $U_{de}$  gust velocities at the respective speeds. On the assumption that the same ratios would be retained in a power-spectral criterion, the loads resulting from these  $\sigma_w \eta_d$ 's are directly comparable as potential critical design conditions.

Spanwise plots of these loads were then made, for comparison with each other and with the loads defined by Conditions I-VIII. These loads were also plotted on shear-torsion, bending-torsion, and shear-bending coordinates at wing stations 83, 207, 346 and 397 for comparison with the design load envelopes and with Conditions II, III, and IV.

As a result of these comparisons, it was evident that Case 417, a  $V_{\rm C}$  case, was critical for upbending and Case 425, a  $V_{\rm D}$  case, for downbending. It was also apparent that for Case 417 the critical location would be inboard of the inboard nacelle and for Case 425, either in this region or between the nacelles. It was also observed that c.g. position would have at most about a 1% effect on the allowable  $\sigma_{\rm W}\eta_{\rm d}$  values; the forward limit was generally the more critical.

In order to properly account for the phasing of shear, bending moment, and torsion, shear flows at W.S. 83 and W.S. 346 were considered.

For Case 417, it was assumed that, at each location,  $S_z$  and  $M_x$  would be in phase. Conditions such as illustrated by points 2 and 3 in Figure 11-1 were then determined. At W.S. 83, to match the front beam shear flow required 98% of the unphased torsion in combination with 100% of the unphased shear and bending moment (Point 2), or 98% of the unphased shear and bending with 100% of the unphased torsion (Point 3). At W.S. 346, the front beam shear flow was matched with 100% of the unphased values of all three load quantities (Points 2 and 3 coinciding at Point 1).

Because of the close proximity of the Point 2 and Point 3 conditions, a single condition corresponding to Point 2 was defined for stress analysis. This condition, designated 417L, was defined only in the potentially critical region inboard of the inboard nacelle. It was obtained by passing smooth curves through the unphased shears and bending moments at W.S. 83, 119, and 167 and 98% of the unphased torsions at the same locations. The shears thus defined were integrated to assure agreement with the statistically defined bending moments.

Case 425 was treated similarly. At W.S. 83, it was found that the front beam shear flow was matched with 100% of the unphased shear and bending moment in combination with 95% of the unphased torsion; or 100% of the unphased torsion with 97% of the unphased shear and bending moment. In defining a condition for stress analysis, points were plotted representing 100% of the unphased shear and bending moment and 96% of the unphased torsion.

In the region between nacelles, examination of Figure 11-2(e) indicated that shear and bending moment should not be considered in phase. Considering 90% of the unphased bending moment to combine with 100% of the unphased shear, it was found that front beam shear flow was matched with 97% of the unphased torsion. Phasing ratios at the other wing stations in the region between nacelles were then estimated based upon the numbers in column 22 of Table C-11; the following ratios resulted:

W.S.	$s_z$	M <sub>x</sub>	M <sub>y</sub>
209	.96	1,00	-97
275	•98	• <b>9</b> 8	•97
346	1.00	.90	•97

The condition thus defined is designated 425L.

Stress analysis for these conditions resulted in the following minimum margins of safety:

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Condition	Wing Station	Location and Description	Margin of Safety
417 <b>L</b>	101	Upper Surface, Panel 4, Compression and Shear	02
417 <b>L</b>	137	Upper Surface, Panel 6 Compression and Shear	0
425L	137-166	Upper Surface, Panel 3, Shear	03
425L	209-239	Lower surface to front beam attachments	02
425L	275-293	Front beam web, tension and shear	02

Limit strength values of  $\sigma_{w}\eta_{d}$  corresponding to these two conditions were obtained as follows:

For condition 417L, the value of  $M_{\rm X}$  at W.S. 83 is 13.61 x  $10^6$  in.1b. The zero margin value is then

$$(1 - .02)(13.61 \times 10^6 \text{ in.lb.}) = 13.34 \times 10^6 \text{ in.lb.}$$

Subtracting the 1-g value and dividing by  $\overline{A}$  (Table B-2) gives

$$\sigma_{\rm W}\eta_{\rm d} = \frac{13.3^{\rm h} \times 10^{\rm 6} - 5.00 \times 10^{\rm 6}}{138800} = 60 \text{ fps (at h = 12000 ft.)}$$

Similarly, for Condition 425L, the zero margin value of  $M_{\chi}$  at W.S. 167 is

$$(1 - .03)(-5.13 \times 10^6 \text{ in.lb.}) = -4.98 \times 10^6 \text{ in.lb.}$$

and the limit strength value of  $\sigma_{\mathbf{w}}\eta_{\mathbf{d}}$  is

$$\sigma_{\rm w}\eta_{\rm d} = \frac{-4.98 \times 10^{-6} - 2.04 \times 10^{-6}}{166700} = 31.1 \text{ fps (at h = 7000 ft.)}$$

To establish the  $\sigma_w \eta_d$  value corresponding to ultimate strength at  $V_C$ , a condition 417U was defined at an estimated  $\sigma_w \eta_d$  level of 95 fps. This condition was identical to 417L except that the incremental loads were increased in the ratio 95/62.

The minimum margin of safety for this condition was found to be + .05, in upper surface panel 4 at W.S. 101, due to combined compression and shear.

The zero margin value of  $M_x$  at W.S. 83 is then

$$(1 + .05)(18.20 \times 10^{6} \text{ in.lb.}) = 19.10 \times 10^{6} \text{ in.lb.}$$

and the ultimate strength value of  $\sigma_{\mathbf{v}}\eta_{\mathbf{d}}$  is

$$\sigma_{\rm w}\eta_{\rm d} = \frac{19.10 \times 10^6 - 5.00 \times 10^6}{138800} = 101 \text{ fps (at h = 12000 ft.)}$$

As a result of the work to this point, it appeared that - for the assumed relative turbulence intensities at  $V_B$ ,  $V_C$ , and  $V_D$  - conditions not yet specifically investigated were not likely to be critical. At this stage, however, it was considered desirable to make an over-all survey by determining approximate allowable  $\sigma_w\eta_d$  values at both limit and iltimate levels, for all available cases, considering both upbending and downbending individually. Such a survey would provide a basis for possible reassessment of the relative turbulence intensities to be specified for design at  $V_B$ ,  $V_C$ , and  $V_D$ . In providing an overall picture it would also constitute a check to assure that critical conditions had not been overlooked.

It was found that a rather reliable survey could readily be made. For the cases so far investigated, critical stresses were seen to result predominantly from combined bending moment and torsion. The most critical regions were found to be near the root and just outboard of the inboard nacelle, and in both regions the appropriate phasing ratios were found to be close to unity. Accordingly, unphased loads were plotted on bending-torsion coordinates at W.S. 83 (upbending and downbending) and at W.S. 209 (downbending only).

Limit and ultimate design load envelopes were then drawn based on the various available airplane design conditions. Inasmuch as the various conditions for which stress analysis was performed in this study (after diustment to zero-margin levels) fell very close to the design load alopes, these envelopes were used directly as limit and ultimate ngth envelopes. (In the region of more-positive torsion charactering by Cases 427-431, an actual-strength line was used; this was defined by stress analysis for Case 430 at  $\sigma_w \eta_d = 94$ , which gave a margin of safety of +.05.) To obtain limit and ultimate  $\sigma_w \eta_d$  values for each condition, a ray was drawn from the one-g point to the net load point and extended to intersect the limit and ultimate strength envelopes. Relative distances along this ray, in conjunction with the known  $\sigma_w \eta_d$  value for which the condition was defined, then determined the limit and ultimate strength values of  $\sigma_w \eta_d$ .

The results of this survey are shown in Table E-1 and Figures E-1 and E-2.

In both the table and the figures, the  $\sigma_w \eta_d$  values have been adjusted to an altitude of 12,000 ft. by moving along one of the family of lines in Figure 5-8. In effect, the allowable  $\sigma_w \eta_d$  at the actual altitude for the condition defines a line of the family shown in Figure 5-8; this line is then designated not by its  $N(y)/N_0$  value but by the  $\sigma_w \eta_d$  value where it intersects the 12,000 ft. altitude.

For the  $V_B$  and  $V_D$  conditions, the adjustment could be either along lines of constant  $N(y)/N_O$  as for the  $V_C$  conditions, or along lines such as to maintain a constant ratio of  $V_B$  to  $V_C$   $\sigma_w \eta_d$  and  $V_D$  to  $V_C$   $\sigma_w \eta_d$ . The latter basis was used.

In the figures, calculated points from Table E-1 are indicated by circles. Where only one calculated point is available for a curve, the estimated trend is indicated by a dash line. The large squares denote the critical conditions for the three speeds respectively.

As a result of the trend with fuel weight shown for the  $V_C$  cases (Figure E-1 (a) , it was obvious that case 427 did not reflect the critical ruel weight at  $V_B$ . It was at this point that cases 428 through 431 were added. These were selected not only to cover the effect of increased fuel weight, but also to confirm that the critical altitude had been included and to provide a basis for review of the  $V_B$  speed selected somewhat arbitrarily in Section 7.

On a limit basis, it is seen that the allowable  $\sigma_w \eta_d$  for  $V_D$  is just 25/50 of that for  $V_C$ . The allowable  $\sigma_w \eta_d$  for  $V_B$  is clearly well in excess of 66/50 of the  $V_C$  value.

TABLE E-1. SUMMARY OF LIMIT STRENGTH AND ULTIMATE STRENGTH  $\sigma_{w} *_{d}$  VALUES (ADJUSTED TO h = 12000 FT), MODEL 188 WING

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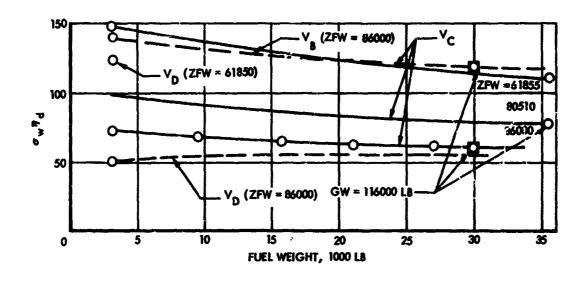
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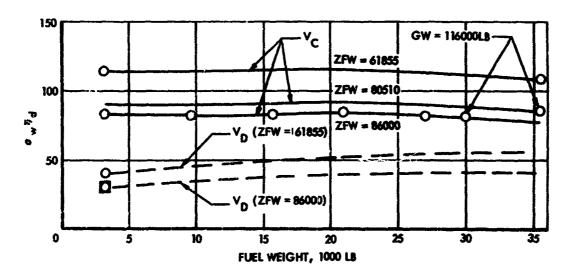
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								17	Limit	Ωt	Ultimete
Case	Cond	Gross	Fuel	Zero Fuel Weight	ი. ი.	Altitude	Equivalent At speed	Up Gust	Down Gust	Up Gust	Down Gust
No		d.	Lb	Lb	% MAC	F.	v, Kts	ow nd	P <sub>L</sub> <sup>M</sup> o	o <sub>w</sub> n <sub>d</sub>	$\sigma_{_{\mathbf{W}}} n_{\mathbf{d}}$
101	>	65000	3145	61855	12.0	72000	324	د∤ د	11.	540	167
403	۶,	97345	35490	61855	16.2	12000	35 <sub>t</sub>	110	108	152	157
405	, > <sub>د</sub>	116000	35490	80510	20.2	12000	35 <sup>†</sup>	77	85	120	119
407	۶, ۲	39145	3145	86000	14.5	12000	32,4	73	83	125	113
604	' > د	95620	9620	96000	15.8	12000	324	89	81	116	110
11.4	۶,	101860	15860	85000	17.2	12000	324	65	83	411	112
413	, > <sub>د</sub>	107000	21000	86200	18.3	12000	324	29	₹	106	113
415	>د	113100	27000	86000	19.6	12000	324	19	88	103	111
417	ے '	116000	30000	86000	20.2	12000	32h	œ	æ.	700	110
419	, > <sub>0</sub>	89145	3145	86000	14.5	20000	275	87	115	777	154
1,20	>	89145	3145	96000	14.5	16000	667	8	101	135	134
121	, > <sub>c</sub>	89145	3145	86000	14.5	2000	324	&	8	141	130
422	· >	89145	3145	86000	14.5	0	324	8	105	164	149
<b>423</b>	·>c	65000	3145	61855	12.0	7000	405	124	01	193	83
425	>°	89145	3145	96000	14.5	7000	405	ርረ	జ	88	ť
427	> <sup>a</sup>	89145	3145	86000	14.5	7000	180	140	231	256	51.6
428	, m	89145	3145	96000	14.5	12000	180	1,10	787 787	£43	<b>%</b>
£23	VB	000911	30000	96000	20,2	12000	180	911	220	220	267
430		000911	30000	96000	20.2	12000	220	83	176	180	233
1431		116000	30000	86000	20.2	27000	220	105	165	171	216

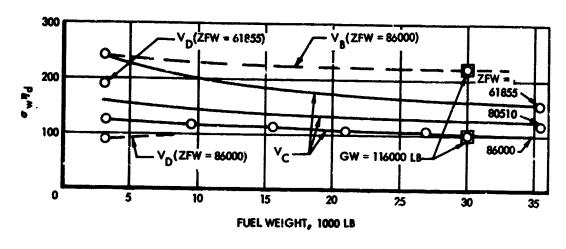


## (a) UPBENDING

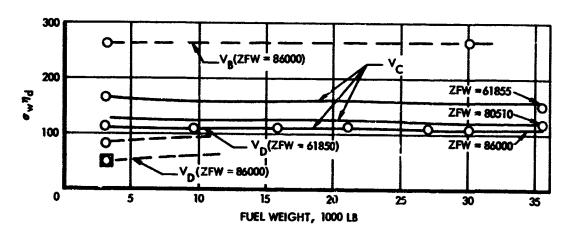


(b) DOWN BENDING

FIGURE E-1. LIMIT STRENGTH VALUES OF FW 1d (ADJUSTED TO h = 12000 FT), MODEL 188 WING



## (a) UPBENDING



# (b) DOWN BENDING

FIGURE E-2. ULTIMATE STRENGTH VALUES OF Gw7d (ADJUSTED TO h = 12000 FT), MODEL 188 WING

On an ultimate basis, the allowable  $\sigma_W \eta_d$  for  $V_D$  again is just 25/50 of the  $V_C$  value, and the allowable for  $V_B$  is again well in excess of 60/50 of the  $V_C$  value.

At  $V_C$ , the ultimate strength value of  $\sigma_W \eta_d$  is 1.67 times the limit strength value. The ratio of ultimate-strength to limit-strength  $N(y)/N_O$  values is  $(2 \times 10^{-8})/(1.3 \times 10^{-6}) = 1.5 \times 10^{-2}$ .

In order to confirm that the VB speed selected in Section 7 is realistic, as well as to indicate how a VB speed might rationally be selected in a power-spectral context, limit-strength, ultimate-strength, and stall values of  $\sigma_{\rm WMd}$  (or y/A) for the Model 188 are plotted vs speed in Figure E-3.

The limit-strength and ultimate-strength values were taken directly from Table E-1 (Cases 417, 429, and 430).

The stall values were obtained as follows:

$$n_{\text{stall}} = \frac{q c_{\text{I}_{\text{max}}}}{(\frac{W}{B})}$$

$$(\sigma_{W} \eta_{\tilde{a}})_{\text{stall}} = \frac{n_{\text{stall}} - 1}{\overline{A}_{\Delta n}}$$

The  $\overline{A}_{\Delta n}$  value is a static-elastic value, inasmuch as the elastic-mode overtravel increment does not reflect airload on the airplane and therefore does not influence stall. In this instance,  $\overline{A}_{\Delta n}$  was obtained by dividing the elastic-airplane values listed in Table B-2(a) - (c) by an estimated dynamic factor of 1.10. Results are shown separately for three different bases for  $C_{I_{max}}$ . The  $C_{I_{max}}$  value of 1.55 was the best-estimate value used in the initial design of the airplane. The "dynamic  $C_{I_{max}}$ " and "start of buffet"  $C_{I_{max}}$  values were based upon later flight tests of a similar airplane and vary with Mach number.

As indicated in Section 15.2.2, an appropriate definition of the VB speed would be the speed at which stall would just occur at a load level given by the VB design value of  $\sigma_{\rm W} \, \eta_{\rm d}$ . On this basis, Figure E-3 indicates a VB speed for the Model 188 (at 116,000 lbs. gross weight) of either 165 or 170 knots depending upon the  $CI_{\rm max}$  value selected. If start of buffet, rather than full stall, were utilized as the criterion, the VB speed would increase to about 200 knots. It is concluded that the VB speed of 180 knots selected in Section 7 is satisfactory for the purpose of the present analysis.

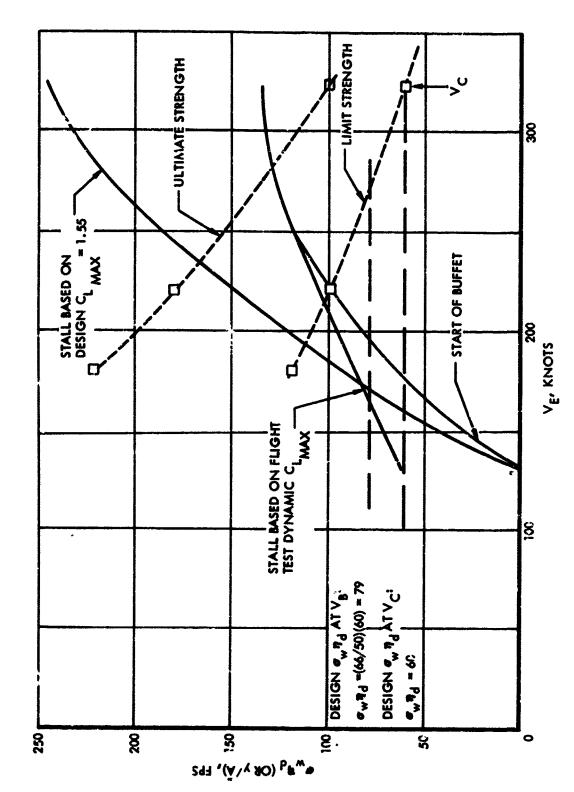


FIGURE E-3. VB SPEED DETERMINATION, MODEL 188 AT 116,000 LB

It is interesting to observe from Figure E-3 that, in order to maintain the greatest margin against both buffet and exceedance of limit strength, a recommended rough air penetration speed for this airplane would be 220 knots. (This is higher than the VB speed because of the excess strength at the VB speed, for this airplane.) If a recommended rough air speed were to be based upon ultimate rather than limit strength, the speed would be much greater still.

## E.2 Model 749 Wing

E.2.1 Design Envelope Criterion. In determining limit and ultimate strength values of N(y) and of  $\sigma_w\eta_d$  for the Model 749 wing, it was considered desirable to first generate a set of enveloping conditions for the critical Vc design envelope case, using generally the technique illustrated for the Model 188 wing in Appendix C. Stress analysis for these conditions would then indicate the most critical regions of the wing, as well as leading to an estimate of the Vc limit-strength value of  $\sigma_w\eta_d$ . It was felt that a set of conditions enveloping a design envelope case would be as useful for this purpose as one enveloping mission analysis loads, and it would be appreciably easier to generate.

Inasmuch as Case 308 appeared to be the critical  $V_C$  case, it was selected as the case to be enveloped. Three upbending conditions were generated, designated I, II, and III. These were roughly comparable to the Model 188 conditions I, II, and IV listed in Table C-11; some indication as to their nature is evident from their locations on the equal probability ellipsoids of Figures 11-3(e) and (f). They were generated at a  $\sigma_W \eta_d$  level of 93, corresponding to an  $N(y)/N_O$  value of 4 x 10-0, which was estimated to be approximately the limit strength level. Downbending loads were also considered; however, as a result of the excess strength in downbending of the Model 749 wing, it became obvious with only limited investigation that downbending gust loads would not be critical.

As in the corresponding Model 188 work, conditions were defined only for phasings of torsion with shear and bending in the upper right and lower left quadrants of the phase plane plot (Figure 11-3(c), for example). This phasing tends to match the statistically defined snear flow in the front beam. Closer scrutiny, however, of the "equal probability ellipses" for the Model 749, shown in Figures 11-3(c) and (f), made it clear that maximum rear beam shear flow conditions might be more critical, and the results of the stress analysis confirmed this conclusion.

Minimum margins of safety obtained for these conditions were:

Station	Condition	Location and Description	Margin of Safety
97	I	Lower surface skin, tension and shear	01
145	I	Rear beam web splice, attachments	03
145	II	Rear beam web splice, attachments	03
145	II	Lower surface cut-out, chordwise compr.	02
191	II	Front beam web splice, attachments	01
191	II	Front beam web, tension and shear	- : O <sup>1</sup> 4

Inasmuch as the critical conditions for the rear beam had not been included, additional work was necessary in order to define a limit strength value of  $\sigma_w n_d$ .

Before proceeding further, however, it appeared desirable to make a systematic survey of all of the design envelope cases in order to establish with greater certainty which ones might be critical. Accordingly, loads for all of cases 301 through 318 were listed for an estimated limit strength level of  $\sigma_{\rm W}\eta_{\rm d} = 93$ . Loads were also listed for the  $V_{\rm D}$  cases, 319-322, at  $\sigma_{\rm W}\eta_{\rm d} = (25/50)(93) = 46.5$  and for the  $V_{\rm B}$  case, 423, at  $\sigma_{\rm W}\eta_{\rm d} = (4/3)(93) = 124$ , where the factor 4/3 is a rounded-off equivalent of 66/50. These were unphased loads and were obtained simply by multiplying the  $\overline{\rm A}$  values listed in Table 9-3 by the given  $\sigma_{\rm W}\eta_{\rm d}$  values. Spanwise plots of these loads were then made, for comparison with each other and with the loads defined as Conditions I - III.

On the basis of these plots, it became clear that only Cases 307, 308, and 317 at  $V_{\rm C}$ , and Case 323 at  $V_{\rm B}$ , were likely to be critical; also, that the region of the wing outboard of the outboard nacelle would not be critical for any of the cases.

In order to determine actual limit-strength values of  $\sigma_{\mathbf{w}}\eta_{\mathbf{d}}$  for these four cases, it was necessary to account for the phasing of the shear, bending moment, and torsion. Phasing factors to be applied to the unphased loads were determined separately for the regions of the wing between nacelles and inboard of the inboard nacelle. Appropriate phasing of the bending moment and shear was estimated with the assistance of the

"equal probability ellipses" in Figures 11-3(b) and (e). Phasing of the torsions relative to the shears and bending moments was then obtained such as to match the shear flows in, alternately, the front and rear beams. The resulting pasing factors are listed in Table E-2. In the "A" and "B" conditions, front beam shear flow was matched; these conditions correspond to points 2 and 3, respectively, in Figure 11-1. In the "C" conditions, rear beam shear flow was matched, with maximum shear and "accord moment and reduced torsion. It is seen that 12 separate conditions with editions was made to assure that the shears thus down and integrated to give the bending moments, since at this stage these conditions were not to be used in actual stress analysis.

The 12 load conditions thus defined were then plotted on bending-torsion, shear-torsion, and shear-bending coordinates at each of wing stations 63,  $1^{14}$ 5, 191, 263, and 337. Both the one-g and the net upbending loads were shown, along with the upbending and downbending loads from Conditions I, II, III.

Although 1 realistic conditions were now defined, they were defined only at a limited number of wing stations and were not necessarily exactly consistent from one wing station to another. It was quite desirable to avoid having to generate conditions that would be consistent over the entire wing, and also to minimize the number of conditions and the regions of the wing for which stress analysis would be required.

Accordingly, four new conditions for stress analysis were now defined, by arbitrarily spotting in four points on each shear-torsion diagram such as to envelope the conditions plotted. Conditions IV, V, and VI were upbending conditions. Shear (and hence bending moment) were comparable for all of these; the torsions, however, varied over a wide range, with Condition IV having the highest positive torsion and Condition VI the highest negative torsion. Condition VII was a conservatively defined downbending condition. In defining these four conditions. consistency of shears and torsions from one wing station to the next was maintained only qualitatively. To determine bending moments, the shears defined on the five shear-torsion plots were plotted vs wing station and integrated to give bending moments. Points representing the four enveloping conditions were then added to the bending-torsion and shearbending plots to assure that the 12 conditions were adequately enveloped with respect to bending moment as well as shear and torsion. Spanwise plots of all three load quantities were made for use in the stress analysis.

Stress analysis for Conditions IV through VII led to the following minimum margins of safety:

TABLE E-2. PHASING FACTORS, MODEL 749 DESIGN ENVELOPE CONDITIONS

Condition	Where Shear		Phasing Factors						
	Flow Was Matched	s <sub>z</sub>	мх	Мұ					
307A	Front Beam, WS103	1.000	1.000	.824					
	Front Beam, WS337	1.000	.950	•935					
30729	Front Beam, WS103	.801	.801	1.000					
	Front Beam, WS337	.821	.53 <sup>h</sup>	1.000					
<b>36</b> 70	Rear Deam, WS103	1.000	1.000	.200					
	Rear Beam, WS337	.800	1.000	095					
308A	Front Beam, WS103 Front Beam, WS337	1.000	1.000 .950	.690 .890					
308B	Front Beam, WS103	.702	.702	1.000					
	Pront Beam, WS337	.755	.491	1.000					
308c	Rear Beam, WS103	1.000	1.000	.042					
	Rear Beam, WS337	.950	1.000	228					
31.7A	Front Beam, WS103 Front Beam, WS337	1.000	1.000 .950	.618 .8µ					
31.7B	Front Beam, WS103	.674	.674	1.000					
	Front Beam, WS337	.694	.451	1.000					
317c	Rear Beam, WS103	1.000	1,000	0					
	Rear Beam, WS337	.800	1.000	324					
323A	Front Beam, WS103	1.000	1.000	.571					
	Front Beam, WS337	1.000	.950	.8 <b>3</b> 9					
323B	Front Beam, WS103	.619	.619	1.000					
	Front Beam, WS337	.729	.474	1.000					
323C	Rear Beam, WS103	1.000	1,000	089					
	Rear Beam, WS337	.800	1,600	231					

Loading Condition	Wing Station	Location and Description	Margin of Safety
Jonaz Jaon	50401011	Location and Description	Dared
IA	115	Lower surface door, attachments	~,06
	145	Front beam web splice, attachments	01
	145	Lower surface cut-out, chordwise compr.	O +
	191	Front beam web splice, attachments	07
	191	Front beam web, tension and shear	11
	<b>2</b> 89	Front beam web, tension and shear	09
A	97	Lower surface skin, tension and shear	03
	97 145	Rear beam web splice, attachments	01
	168	Lower surface cut-out, spanwise tension	03
	191	Front beam web splice, attachments	04
	191	Front beam web, tension and shear	07
VI	97	Lower surface skin, tension and shear	03
	145	Rear beam web splice, attachments	04

No negative margins were found for Condition VII, confirming that downbending would not be critical.

Based on these margins, Conditions IV, V, and VI were adjusted in level, independently over various regions of the wing, such that zero margins of safety would result. Strength envelopes on bending-torsion and shear-torsion coordinates were thus defined at wing stations 103, 145, 191, 263, and 337.

It was now possible to go back to the 12 conditions, 307 A - C, 308 A - C, 317 A - C, and 323 A - C and obtain for each case a good approximation to the limit strength value of  $\sigma_w \eta_d$  and the critical location in the structure. This limit-strength value of  $\sigma_w \eta_d$  was determined separately at each wing station and separately based on the bending-torsion and shear-torsion envelopes. For each  $\sigma_w \eta_d$  determination, a ray was drawn from the one-g point to the net load point and extended if necessary to intersect the strength envelope. Relative distances along this ray, in conjunction with the known  $\sigma_w \eta_d$  value for which the condition was defined, then determined the limit strength value of  $\sigma_w \eta_d$ .

The resulting limit strength values of  $\sigma_w N_d$  are shown in Table E-3(a). Each number is the minimum for the three subconditions A,B, and C. The lowest value in each column is the critical value and is underlined.

Approximate ultimate strength values of  $\sigma_{v}\eta_{d}$  were obtained similarly and are shown in Table E-3(b).

TABLE E-3. PRELIMINARY LIMIT STRENGTH AND ULTIMATE STRENGTH VALUES OF  $\sigma_{\mathbf{w}} *_{\mathbf{d}}$ , MODEL 749 DESIGN ENVELOPE CONDITIONS

## (a) LIMIT

ws	Case (h = 16	307 1000 ft)	Case (h = 16		Case (h = 70		Case 323 (h = 7000 ft)		
	SZ-NY NY-NY		N-N Sz-N Sz-N		s <sub>z</sub> -M <sub>Y</sub>	HH.	.Sz-M	M <sub>Z</sub> -H	
103	93.0 (A,C)	92.2 (c)	95•5 (C)	92.3 (A,C)	88.7 (c)	88,2 (A,C)	97:0 (A,C)	91.6 (A,C)	
145	77.8 (c)	88.3 (c)	80.5 (c)	87.0 (c)	78.6 (c)	82.5 (c)	92.0 (c)	69.3 (c)	
191	81.5 (A)	85.3 (A)	83.6 (A)	86.2 (A)	80.2 (A)	83.6 (A)	80.5 (A)	80.3 (A)	
263	87.8 (A)	93.0 (A)	93.0 (A)	93.0 (A)	93.0 (A)	93.0 (A,C)	83.7 (A)	84.0 (A)	
337	(A)	(A)	(A)	(A,C)	(A)	(A)	85.3 (A)	87.0 (A)	

NOTE:  $\sigma_{ab}$   $\eta_{d}$  values for Case 323 have been multiplied by .75 for comparison. Letters A, B, and C denote critical condition. Values for critical WS in each column are underlined.

## (b) ULTIMATE

Case	30	77	30	8	31	7	323		
WS	S <sub>Z</sub> -M <sub>Y</sub>	NNY	S <sub>Z</sub> -M <sub>Y</sub>	K <sub>x</sub> -N <sub>y</sub>	S <sub>Z</sub> -M <sub>Y</sub>	N'-N'	s <sub>z</sub> -n <sub>y</sub>	K-N	
103	168.5 (A,C)	173.2 (A,C)	172,8 (A,C)	172.0 (A,C)	162.0 (A,C)	163.0 (A,C)	170.3 (A,C)	166.3 (A,C)	
145	1.660 (c)	173.9 (C)	165.6 (c)	165.5 (C)	161.8 (c)	158.5 (c)	169.1 (c)	165.6 (c)	
191	146.0 (A)	156.2 (A)	147.1 (A)	156.1 (A)	143.2 (A)	151.0 (A)	144.5 (A)	148.2 (A)	
263	149.5 (A)	160.0 (A)	156.7 (A)	159.6 (A)	157.0 (A)	159.6 (A)	146.0 (A)	150.0 (A)	
337	152.1 (A)	169.6 (A)	160.8 (A)	166.1 (A)	168.0 (A)	159.8 (A)	149.0 (A)	153.8 (A)	

NOTE:  $\sigma_{\rm eff} \, \eta_{\rm d}$  values for Case 323 have been multiplied by .75 for comparison. Letters A, B, and C denote critical phasing. Values for critical WS in each column are underlined.

It was now possible to select critical conditions and locations for stress analysis of specific conditions. Stress analysis for Conditions IV, V, and VI had indicated that the critical stress generally resulted from combinations of bending and torsion moments; consequently, more weight was given to the results in the  $M_X-M_y$  column than in the  $S_Z-M_y$  column in Table E-3.

It was not entirely certain from Table E-3(a) which of the 4 cases would be critical. It was clear, however, that the actual limit strength values of  $\sigma_{\rm W}\eta_{\rm d}$  corresponding to each case could be determined by examining only cases 307C, 308C, and 317C at WS 145, and Cases 307A, 308A, 317A, and 323A at WS 191. Further, it was clear from the above listing of margins of safety that the critical element for the "C" conditions at WS 145 was the rear beam web splice, and for the "A" conditions at WS 191, the front beam web.

Similarly, in Table E-3(a), it was clear that the ultimate strength values of  $\sigma_w \eta_d$  could be determined by examining only the front beam web at WS 191 for each of the "A" conditions.

As a result, only very limited stress analysis would suffice to finally determine the limit and ultimate strength values of  $\sigma_w \eta_d$ .

Before performing this stress analysis for the potentially critical conditions, two refinements were made in the definition of the loads. First, since one of the critical regions was found to be between the ribs supporting the inboard nacelle, the nacelle loads, which previously had been brought into the wing arbitrarily at the nacelle centerline, were redistributed to the two ribs. Second, it had become apparent from the stress analysis that axial stress, far more than shear flow, was governing the wing strength. Consequently, in selecting the relative phasing of shear and bending moment for the "A" conditions in Table E-2, it appeared that  $S_z$ , rather than  $M_x$ , should have been assigned the .950 phasing factor. Further, examination of the complete spanwise distributions available for Conditions I, II, and III indicated that for both the "A" and "C" conditions,  $S_z$  and  $M_x$  should be more nearly in phase at WS 191 than at WS 337. Consequently, revised phasing factors were defined, as shown in Table E-4. The phasing factors for My were not recomputed, as they were expected not to change significantly. In addition, in the stress analysis, the basis for the web shear-tension margin of safety was changed from the maximum tension maximum shear criterion used in the original design analysis to a circular interaction criterion now generally considered more realistic.

Consideration of the probable effects of these changes on the  $\sigma_w \eta_d$  values given in Table E-3 indicated that the critical locations would not change.

TABLE E-4. REVISED PHASING FACTORS, MODEL 749 DESIGN ENVELOPE AND MISSION ANALYSIS CONDITIONS

			Cc aditions		"C" Conditions				
		W8103, 145	W8191	WS337	WS103, 145	WS191	W5337		
s <sub>Z</sub>		1.000	1.000	1.000	1.000	.900#	.800		
	X	1.000	1.000#	.950	1.000	1.000	1.000		
	Case 307	.624	-935	-935	-200	095	095		
	Case 308	.690	.890	.890	.042	228	228		
	Case 317	.618	.844	.844	0	324	~.324		
ž	Case 323	-571	.839	.839	089	231	231		
	Mission Anal. Limit	.697	.854	.854	257	295	295		
Mission Anal. Ult		.712	.872	.875	198	281	581		

<sup>\*</sup> The corresponding values in Table E-2 were .83 and .95 for  $S_{\chi}$  and  $M_{\chi}$  respectively.

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Accordingly, the pertinent conditions were redefined, at the necessary wing stations, at revised  $\sigma_w \eta_d$  levels as follows:

Limit conditions: Cases 307, 308, and 317  $\alpha_{3}\eta_{d} = 83$ 

Case 323  $\sigma_{W} \eta_{d} = \frac{66}{50} 83 = 109.6$ 

Ultimate conditions: Cases 307 and 308  $\sigma_{\rm w}\eta_{\rm d} = 155$ 

Case 317  $\sigma_{\mathbf{w}} \eta_{\mathbf{d}} = 146$ 

Case 323x  $\sigma_{\text{wd}} = \frac{66}{50} \text{ 155} = 205$ 

The ultimate  $\sigma_W\eta_d$  values of 155 and 146 reflected a constant value of N(y)/No in Figure 5-8 as the altitude varies. Case 323x is identical to Case 323 except for an increase in altitude from 7000 to 16000 ft. The 16000 ft. altitude became more critical for the  $V_F$  speed at the ultimate load level because of the opposite slope of the farily of lines in Figure 5-8 at the ultimate as contrasted to the limit level. Loads were obtained for Case 323x from those of Case 323 by retaining the leg loads and decreasing the  $\overline{A}$  values 5%, in accordance with the relations indicated by comparison of the corresponding  $V_C$  cases, 308 vs 317.

The resulting margins of safety are shown in Table E-5. The limit-strength or ultimate strength values of  $\sigma_{\rm w}\eta_{\rm d}$  were then computed as

$$\frac{(1 + MS)(\text{Net shear at given } \sigma_{W}\eta_{d}) - (\text{One-g shear})}{\overline{A}_{\text{Shear}}}$$

and are also shown in the table. Values underlined are at the altitude listed for the case. The other value for each case is an adjusted value obtained by moving along one of the family of lines in Figure 5.8. For the  $V_B$  conditions, the adjustment was along lines such as to maintain a constant ratio of  $V_B$  to  $V_C$   $\sigma_w\eta_d$ . In other words, the underlined  $\sigma_w\eta_d$  was divided by 66/50, the adjustment made to the new altitude, and the resulting value multiplied by 66/50.

TABLE E-5. FINAL LIMIT STRENGTH AND ULTIMATE STRENGTH VALUES OF  $\sigma_{\rm w} \, \eta_{\rm d}$ , MCDEL 749 WING

Condition	Assumed	Margin	Altitude	Lim : Strength o, na				
And Location	$\sigma_{\rm W} \eta_{\rm d}$	Of Safety	Ft	h = 7000 Ft	h = 16000 Ft			
307C W8145	83	.06						
307 <b>A. W</b> S191	83	.04	16000	90.0	89.2			
308C W8145	83	.06	16000	92.2	92.0			
308a. WS191	83	.06			, —,—			
317C. WS145	83	.03	7000	87.5	86.1			
317 <b>A. W</b> 8191	83	.05						
323A, W8191	109.6	0	7000	109.6	106.9			
				Ultimate Strength Gw 7				
				h = 7000 Ft	h = 16000 Ft			
307A. WS191	155	0	16000	145.5	155.0			
308a. WS191	155	.01	16000	146.2	157.2			
317A. WS191	146	.05	7000	156.2	164.4			
323A, WS191	205	.01	16000	194.8	207.9			

It is seen that, for limit strength, Case 317, at h = 7000 ft., is slightly more critical than the 16,000 ft. cases. The effect of c.g. location is indicated by a comparison of Cases 307 and 303. The effect of c.g. location on  $\sigma_w \eta_d$  is slightly greater than indicated in Table E-3, but still only about 3%. The forward c.g. case (307) is the more critical, contrary to earlier indications that led to omitting the forward c.g. cases at h = 7000 ft. A forward c.g. case at 7000 ft. would presumably be slightly more critical than Case 317. The difference is so small, however, that further refinement of the limit strength  $\sigma_w \eta_d$  is not considered justified.

For ultimate strength, the 16000 ft. cases are critical, and the effect of c.g. location is less than 2%.

As a result of the work to this point, it became apparent that, for the assumed relative turbulence intensities at  $V_B$ ,  $V_C$ , and  $V_D$ , cases other than the four specifically investigated were not likely to be critical. As in the Model 188 investigation, however, it was considered desirable at this stage to make an overall survey by determining, at least roughly, allowable  $\sigma_w \eta_d$  values at both limit and ultimate levels, for all cases, considering upbending and downbending individually.

For this purpose, wing bending moment at WS 191 was used as the measure of strength. For all the cases investigated, WS 191 either was the critical location, or missed being critical by only a few percent. And at the critical location in the structure, the net stress was produced predominantly by the bending moment. Values of the WS 191 bending moment corresponding to limit and ultimate strength were taken as follows, based on the margins of safety shown in Table E-5:

	Limit	<u>Ultimate</u>
V <sub>B</sub> , upbending	12.6 $\times 10^6$ in.1b.	18.4 x 106 in.1b.
$v_c$ and $v_p$ , upbending	13.2 x 10 <sup>6</sup> in.1b.	19.1 x 10 <sup>6</sup> in.1b.
$V_B$ , $V_C$ , and $V_D$ , downbending	7.90 x 10 <sup>6</sup> in.1b.	11.85 x 10 <sup>6</sup> in.1b.

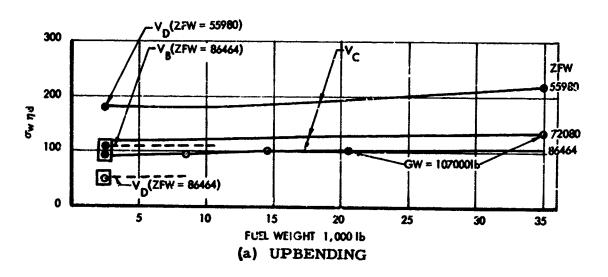
The downbending limit value is taken as 60% of the higher of the two upbending values, and the downbending ultimate value as 1.5 times the limit.

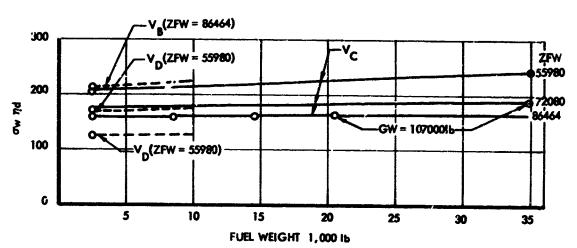
The results of this survey are shown in Table E-6 and Figures E-4 and E-5.

SUMMARY OF LIMIT STRENGTH AND ULTIMATE STRENGTH VALUES (ADJUSTED TO h = 16000 FT), MODEL 749 WING TABLE E-6.

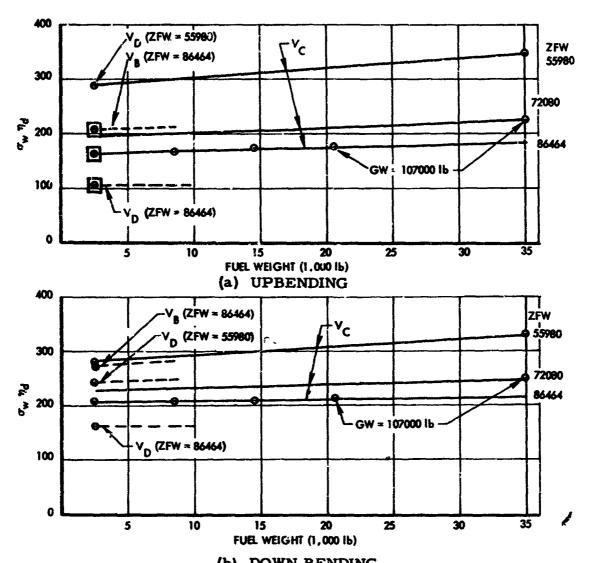
	Ultimate	Down Gust	P4 A0	280	331	5ħ3	<b>30</b> 6	207	808	212	222	₹ <b>0</b> 2	<b>†</b> 17	24.1	191	<b>5</b> 86	275
	nr.	Up Gust	P4 A0	288	349	225	157	165	173	176	168	158	191	503	305	าเล	208
(1)	Limit	Down Gust	Pu Ao	205	110	188	159	1.59	160	163	찬	157	167	179	125	112	208
1), MO	អ	Up Gust	P <sub>U</sub> A <sub>D</sub>	180	219	135	8	ま	700	102	%	88	88	756	เร	107	911
1d VALUES (ADJUSTED TO n = 19000 F 1), MODED 1=7 MING	Rand was and	Airspeed	Ve, Kts	235	235	235	235	235	235	235	218	235	235	313	313	175	175
10 I		Altitude	¥	16000	16000	16000	16000	15000	16000	16000	20000	12000	7000	7000	7000	7000	7000
T SO FC		¥.0.		32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0	32.0
A) 6301.	Zero Biel	Weight	៨.	08655	55980	72080	19198	19198	1791798	19198	19198	19198	19198	55980	<del>19198</del>	19198	19198
	T. C.	Weight	di di	2500	34920	34920	2500	8536	14536	20536	2500	2500	2500	2500	2500	2500	2500
A C	3	Weight	ជ	58480	90900	37.70	19688	95000	101000	107000	<del>19688</del>	£896	<del>19688</del>	58480	19688	19688	49688
		Cond		۸ ۲	, <sub>&gt;</sub> , ¢	, >,	, > ر	, > <sub>c</sub>	> د	, >,	۰ ۲	, >,	> د	, <sub>2</sub> ,	شر ا	, > <sub>a</sub>	, m
		Case	2	305	₹ 2000	306	308	310	315	317	31.5	316	31.7	320	325	323	323X

;;





(b) DOWN BENDING
FIGURE E-4 LIMIT STRENGTH VALUES OF  $\sigma_{w} \tau_{d}$  (ADJUSTED TO h = 16000 FT), MODEL 749 WING



(b) DOWN BENDING
FIGURE E-5 ULTIMATE STRENGTH VALUES OF  $\sigma_{w} r_{d}$  (ADJUSTED TO h = 16000 FT), MODEL 749 WING

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Where values obtained by the approximate method differ from those shown in Table E-5, the latter are substituted. In no case, however, did the difference amount to over 3%, and for the limit conditions it was less than 1%.

In both the table and the figures, the  $\sigma_W \eta_d$  values were adjusted to an altitude of 16,000 ft. by moving along one of the family of lines in Figure 5-8. For the  $V_B$  and  $V_D$  conditions, the adjustment was along lines such as to maintain a constant ratio of the  $V_B$  or  $V_D$   $\sigma_W \eta_d$  value to the  $V_C$  value.

The figures are directly comparable to those for the Model 188, Figures E-1 and E-2. Calculated points are indicated by circles. Where only one calculated point is available for a curve, the estimated trend is indicated by a dash line. The large squares denote the critical conditions for the three speeds respectively.

On a limit basis, it is seen that the allowable  $\sigma_{w\eta d}$  for  $V_D$  is somewhat greater than 25/50 of that for  $V_C$ . The allowable  $\sigma_{w\eta d}$  for  $V_B$  is somewhat greater than that at  $V_C$ , but not by the full 66/50 ratio. The downbending conditions are clearly much less critical than the upbending conditions.

On an ultimate basis, the allowable  $\sigma_w\eta_d$  for  $V_D$  is well in excess of 25/50 of that for  $V_C$ . The allowable  $\sigma_w\eta_d$  for  $V_B$  is just 66/50 of that for  $V_C$ .

At  $V_C$ , the ultimate-strength value of  $\sigma_w \eta_d$  is 1.82 times the limit strength value. The ratio of ultimate-strength to limit strength  $N(y)/N_O$  values is 1.0 x  $10^{-10}/8$  x  $10^{-8}$  = 1.2 x  $10^{-3}$ .

E.2.2 <u>Mission Analysis Criterion</u>. By entering the mission analysis exceedance curves with limit-strength and ultimate-strength values of bending moment at WS 191 obtained from the work described above, it was possible to make good preliminary estimates of limit and ultimate frequencies of exceedance. The following values were thus selected at which to define load conditions for stress analysis.

Limit:  $N(y) = 1.0 \times 10^{-5}$  exceedances per hour

Ultimate:  $N(y) = 3.0 \times 10^{-9}$  exceedances per hour

A set of loads at each of these two levels was read from the exceedance curves. Inasmuch as Case 106 was generally among the predominent

contributors to the exceedances, its one-g loads were considered representative. These were subtracted from the net loads to give a set of incremental loads to which phasing factors could be applied.

At each of two levels, limit and ultimate, two conditions were defined. There corresponded to the "A" and "C" conditions defined for the design envelope cases, and were similarly designated. Phasing factors were obtained in the same way as for the design envelope conditions. The resulting values have been included in Table E-4. The corresponding loads are listed in Table E-7.

Critical locations were known from the design envelope analyses. As a result, stress analysis was performed only for the front beam at WS 191 ("A" conditions) and the rear beam at WS 145 ("C" conditions). The following margins were obtained:

Limit Condition A (front beam, WS 191) -. C2
Limit Condition C (rear beam, WS 145) +. 01
Ultimate Condition A (front beam, WS 191) +. 02
Ultimate Condition C (rear beam, WS 145) +. 10

The corresponding limit and ultimate frequencies of exceedance were obtained from the exceedance curve for bending moment at WS 191. The curves were entered with allowable bending moments equal to (1 - .02) and (1 + .02) times the values at  $1.0 \times 10^{-5}$  and  $3.0 \times 10^{-9}$  respectively; the corresponding frequencies of exceedance were found to be:

Limit:  $N(y) = 1.8 \times 10^{-5}$  cycles per hour

Ultimate:  $N(y) = 4.2 \times 10^{-9}$  cycles per hour

The ratio of ultimate to limit frequencies of exceedance is 2.3 x  $10^{-4}$ , or  $10^{-3}$ .

#### E.3 Model 188 Fuselage and Tail, Vertical Gust

E.3.1 Mission Analysis, Limit Strength. In Appendix D, load conditions were developed for the Model 188 fuselage such that statistically defined loads were matched. This set of conditions reflected a mission analysis approach and a level of severity defined by a frequency of exceedance of 1.00 x 10<sup>-5</sup> cycles per hour. Preliminary comparison of these loads with Model 188 limit design fuselage loads indicated that at no point in the fuselage were the limit design loads exceeded. At this

TABLE E-7. MISSION ANALYSIS LOAD CONDITIONS, MODEL 749 WING

Cond   Cond				Limit, N	Limit, N(y) = 1.0 x 10 <sup>-5</sup>	10-5			Ultimate, $N(y) = 3.0 \times 10^{-9}$	(y) = 3.0 s	c 10 <sup>-9</sup>	
Station         Loads         (case 106)         Cond		Wing	Umphased	One-g	Increment	Phees Lon	d Net de	Unphased	One-g Loads	Increment	Phase Los	ā Net ds
103         48.1         18.12         29.379         48.100         67.5         18.721         48.179         67.5         18.721         48.100         67.5         18.350         46.100         67.5         16.350         42.00         42.00         58.3         16.350         41.950         58.3         41.950         58.35         41.950         58.35         41.950         58.34         41.950         58.35         58.36         42.00         42.00         58.30         42.00         42.35         42.350         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.950         58.35         41.550         41.550         41.550         58.35         41.550         58.35         41.550         58.35         41.550         58.35         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550         41.550		Station	Loads	(case 106)		Cond A	Cond	Loads	(case 106)		Cond	Cond F
145         42.0         16.350         25.550         42.00         42.00         58.3         16.350         41.950         58.3         41.950         41.950         58.3           191         55.7         20.542         35.158         55.700         52.184         78.7         20.542         58.158         78.7           337         35.1         12.180         22.920         17.400         17.400         24.35         6.850         17.500         22.35         17.400         24.35         6.850         17.500         22.75         17.75         17.500         22.75         17.75         17.500         17.500         17.500         1	•	103	1.84	18.721	29.379	48,100	48,100	67.5	18.721	48.779	67.5	67.5
191         55.7         20.542         35.156         55.700         52.184         78.7         20.542         58.156         78.7         20.542         58.156         78.7         20.542         58.156         78.7         20.542         58.156         78.7         20.542         58.156         78.7         20.542         58.35         78.15         20.545         17.400         17.400         24.35         6.853         17.400         17.400         24.35         6.853         17.400         17.400         24.35         6.853         17.400         17.400         24.35         6.853         17.500         24.35         21.75         6.843         17.500         24.35         21.75	z <sub>s</sub>	145	42.0	16.350	25.650	42.000	12.00v	58.3	16.350	41.950	58.3	58.3
337         35.1         12.180         22.920         -         49.6         12.180         37.420         -           103         17.40         6.850         10.550         17.400         24.35         6.850         17.500         24.35           145         15.50         6.041         9.509         15.550         13.75	-O	161	55.7	20.542	35.158	55. Too	52.184	78.7	20.542	58.158	78.7	72.884
103         17.40         6.850         17.400         17.400         24.35         6.43         6.43         17.500         24.35           145         15.50         6.041         9.599         15.550         15.550         21.75         6.041         15.709         21.75           191         13.30         5.223         8.107         13.330         13.35         13.427         18.65         5.223         13.427         18.65           103         4.59         2.885         4.075         -         -         9.59         2.885         18.65         -           103         4.5         -         -         9.59         -1.237         2.689        675         -           104        1         -         -         -         -         9.59        159        596        1537         1.594         -	[	337	35.1	12.180	22.920	•	ı	76.6	12,180	37.420	ı	
145         15.50         6.041         9.509         15.550         13.30         6.041         15.709         13.779         21.75           191         13.30         5.223         8.107         13.330         13.330         18.65         5.223         13.427         18.65           337         6.90         2.825         4.075         -         -         9.58         6.755         -           103         .41         -1.237         1.647        089         -1.660         1.45         -1.237         2.687         6.755         -           145         .27         -1.237         1.647        089         -1.830         1.31         -1.237         2.689         .568         .568           191         .27         -1.667         -1.830         1.536        676         -1.369        693         2.516        594           103 RB         .286         -1.166         1.93        896         2.516        594         1.594           103 RB         -186         -1.166         -1.96         -2.896         -2.166         -2.166         -2.166         -2.166         -2.166         -2.166         -2.166         -2.166         -2.166		103	04.71	6.850	10.550	17.400	17.400	24.35	6.850	17.500	£4.35	24.35
191         13.30         5.223         8.107         13.330         13.330         18.65         5.223         13.427         18.65           337         6.90         2.825         4.075         -         -         9.58         5.223         13.427         18.65           103         .41         -         -         -         -         9.58         5.755         -           103         .41         -	ž	145	15.50	6.041	9.509	15.550	15.550	21.75	6.041	15.709	21.75	21.75
337       6.90       2.825       4.075       -       -       9.58       2.825       6.755         103       .41       -1.237       1.647      089       -1.660       1.45       -1.379       2.687         145       .27       -1.379       1.647      230       -1.830       1.31       -1.379       2.689       1         191       .91      693       1.603       +.676       -1.166       1.93      693       2.623       1         103 FB       .94      896       1.536      996       4.36      996	9-0	161	13.30	5.223	8.107	13.330	13.330	18.65	5.223	13.427	18.65	18.65
103         .41         -1.237         1.647        089         -1.650         1.45         -1.237         2.687           145         .27         -1.379         1.646        230         -1.36         1.31         -1.379         2.689         1.689           191         .91        693         1.603         +.676         -1.166         1.93        693         2.623         1           103 FB         .94        866         1.536         896        896         2.516           103 FB         -416         -370           996         -416         -582           337 FB         640         -115         755           996         -416         -582           337 FB         -820         -435         -385           996         -415         1245	τ	337	6.90	2.825	4.075	•	1	9.58	2.825	6.755	1	e
145       .27       -1.379       1.646      230       -1.830       1.31       -1.379       2.689         191       .91      693       1.603       +.676       -1.166       1.93      693       2.523       1         103 FB       .94      866       1.536         630      896       2.516         103 FB       -786       -416       -370         998       -416       -582         337 FB       640       -115       755        1130       -115       1245         337 FB       -820       -435       -385        -       -996       -415       1245		303	14.	-1.237	1.647	680*-	-1.660	1.45	-1.237	2.687	929.	691.1-
191       .91      693       1.603       +.676       -1.166       1.93      693       2.623         103 FB       .94       1.536       -       -       96      896       2.516         103 FB       -786       -416       -370       -       998       -416       -582         337 FB       640       -115       755       -       1130       -115       1245         337 FB       -820       -435       -385       -       -1050       -435       -615	X,	145	.27	-1.379	1.649	230	-1.830	1.31	-1.379	2.689	.536	11.911
337         .b4        896         1.536         -         1.62        896         2.516           103 FB         339        99         4,38         -         -         99         729         729           103 FB         -786         -4,16         -370         -         -         998         -4,16         -582           337 FB         640         -115         755         -         130         -115         1245           337 FB         -820         -435         -385         -         -         -1050         -435         -615	9-0	161	16.	693	1.603	+.676	-1.166	1.93	693	2.623	1.594	-1.430
103 FB 339 - 99 438 - 630 - 99 103 RF -786 -416 -370 - 998 -416 - 115 1 130 -115 1 130 -115 1 130 -135 - 135 - 1050 -435 - 1050	τ	337	\$	9i8	1.536		1	1.62	896	2.516	_	
103 RB -786 -416 -370 998 -416 337 FB 640 -115 755 1130 -115 337 RB -820 -435 -385 1050 -435		103 FB	339	66 -	438		1	630	8.	729	•	•
337 FB 640 -115 755 1130 -115 337 FB -820 -435 -385 1050 -435	1	103 RF	-786	-416	-370	,	ı	- 998	914-	-582	1	1
-820 -435 -385 - 1050 -435		337 FB	9	-115	755	•	•	1130	-11.5	1245	•	ı
		337 RP	-820	-435	-385	1	•	-1050	-435	-615	ı	1

Note: Torsions are with respect to elastic axis (FS 561.2).

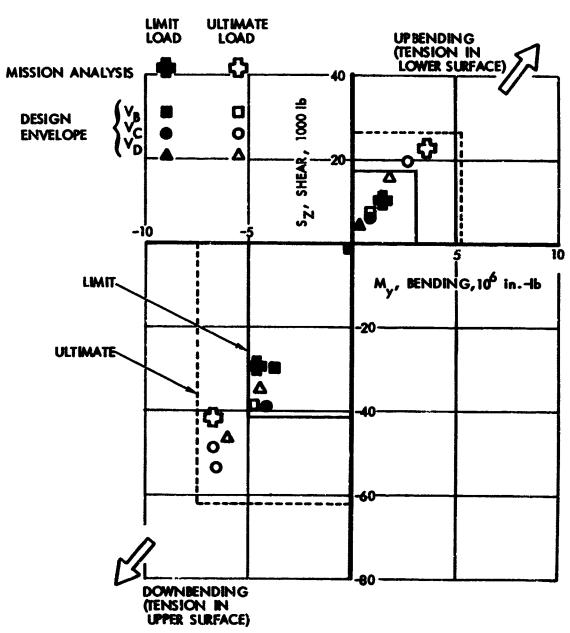
frequency of exceedance the Model 188 wing, on the other hand, actually showed slight negative margins of safety. Hence it was clear that the fuselage would be less critical than the wing and therefore would not influence the vertical gust design level.

However, in order to obtain a clearer picture of the critical regions of the fuselage, as well as a direct measure of how much less critical the fuselage is than the wing, this comparison was now made on a more formal basis.

In Figures E-6(a) through (?), design load envelopes are shown for the Model 188 ruselage at the various locations where load outputs were obtained from the ten-degree-of-freedom analysis. These locations, it will be recalled, were potentially critical locations as indicated by the design stress analysis. In all cases, the envelopes are shown as rectangles. These are defined by design conditions at or very close to the upbending and downbending corners. The rectangular shape is believed to approximate closely the shape of the actual strength envelopes, since the stress analysis indicated relatively little interaction between shear and berding moment. For the design downbending conditions, design margins of safety were rather low and the design load envelopes are believed to be fairly good approximations to actual strength envelopes. For the upbending conditions, considerably greater strength was available than indicated by the envelopes.

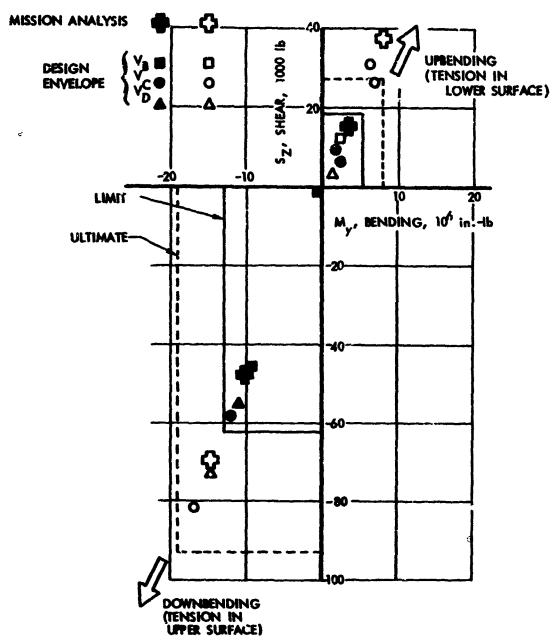
The mission analysis limit points shown on the figures were read from load exceedance curves, such as given in Figures 9-8 and 9-9, at a frequency of exceedance of 2.4 x 10-5 cycles per hour. This level corresponds approximately to the limit strength of the Model 188 wing, as established in Appendix E. The plotted points reflect unphased values of shear and bending moment in all cases. As can be inferred from the results given in Appendix D, actual phasing factors are generally close to unity. Also, because of the absence of significant interaction between shear and bending moment, the validity of the comparison does not depend upon the shear and bending moment being exactly in phase.

It is seen that at all locations the mission analysis limit load is well below the design limit load given by the solid line in the figures. Based on downbending strength - upbending being found less critical when account is taken of the higher margins of safety for the upbending design conditions - the critical location is F.S. 350; and the limit strength value of N(y) at this location, as read from the exceedance curve for bending moment at the limit design load level of -5.0 x  $10^{\circ}$  in lb., is 6 x  $10^{\circ}$ 0 exceedances per hour. This is considerably lower than the value of 2.1 exceedances per hour for the wing.



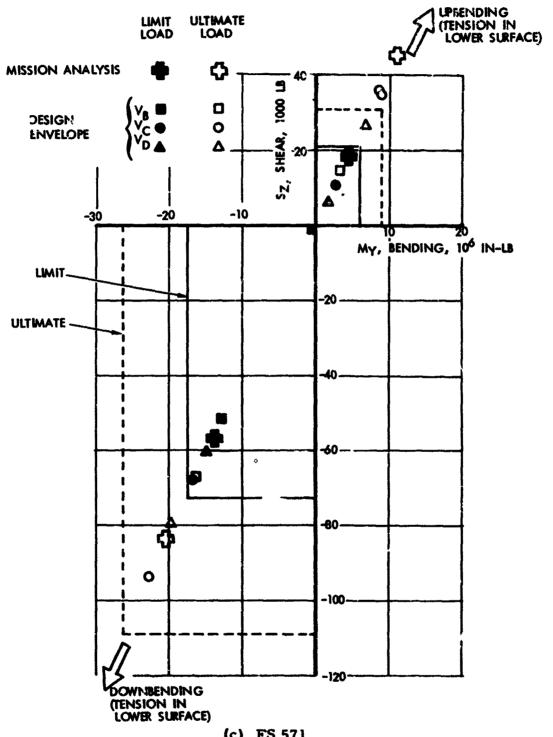
(a) FS 350
FIGURE E-6 COMPARISON OF APPLIED FUSELAGE LOADS WITH
DESIGN STRENGTH - MISSION ANALYSIS AND
DESIGN ENVELOPE CRITERIA - MODEL 188

LIMIT ULTIMATE

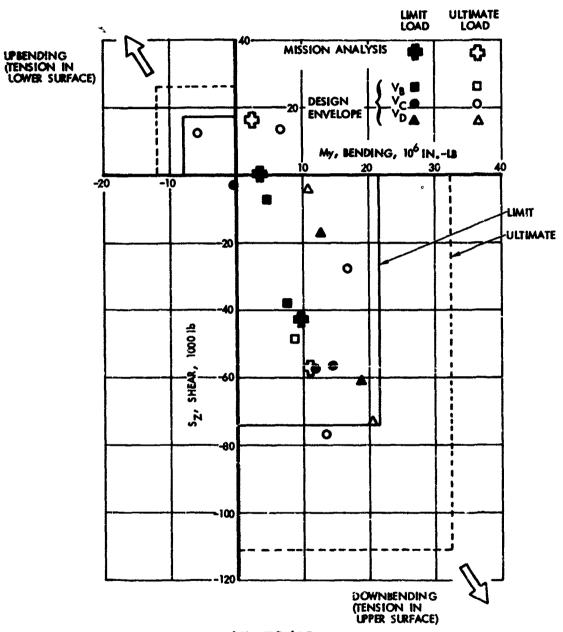


(b) FS 500 FIGURE E-6 CONTINUED

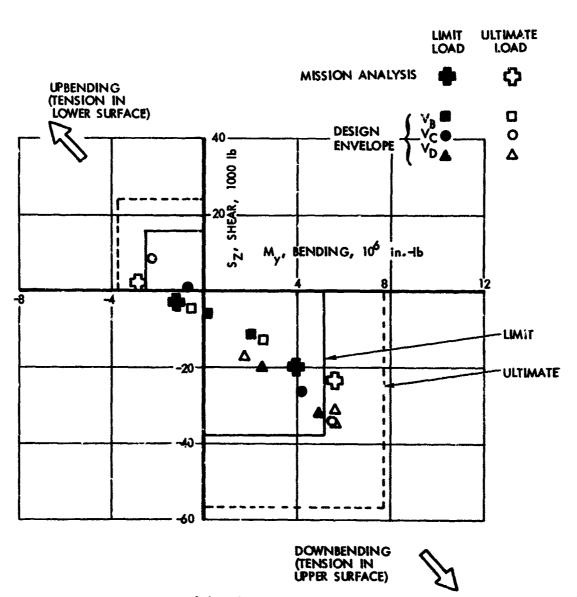
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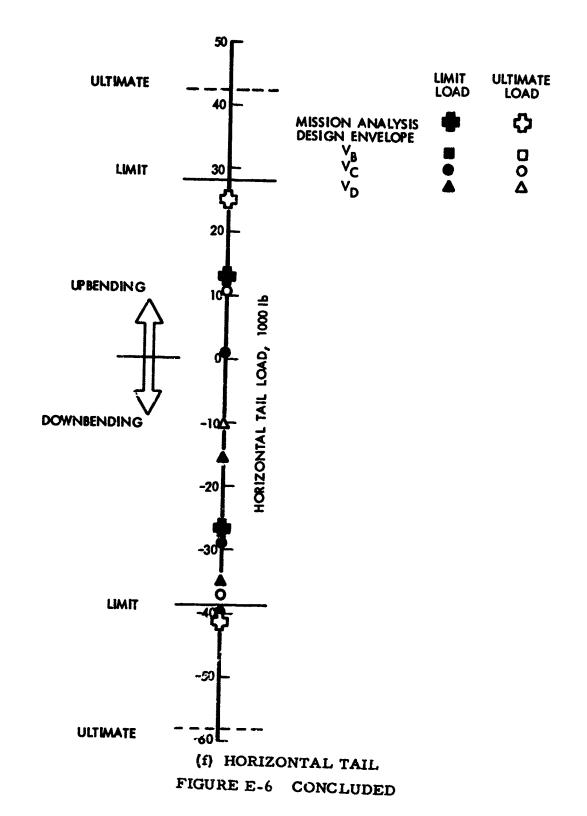
(c) FS 571 FIGURE E-6 CONTINUED



(d) FS 695 FIGURE E-6 CONTINUED



(e) FS 1000 FIGURE E-6 CONTINUED



E.3.2 <u>Mission Analysis</u>, <u>Ultimate Strength</u>. As in the above investigation of the limit strength level, statistically defined loads were also obtained for the Model 188 fuselage and horizontal tail at an appropriate ultimate strength frequency of exceedance; these were then added to Figures E-6(a) through (f). The frequency of exceedance was taken as that corresponding to ultimate strength of the Model 188 wing, or 1.4 x 10<sup>-8</sup> cycles per hour.

The statistically defined loads are larger than the design ultimate loads only for upbending at FS 500 and FS 571. However, as noted above, the design loads for upbending have large positive margins of safety due to the inherent strength resulting from the high downbending loads. The allowable shear is essentially the same in upbending as in downbending. An indication of the allowable bending moment in upbending is given by the minimum margin of safety for the design upbending conditions at FS 500 and FS 571. This was + .37 (at FS 571), due to buckling of an upper longeron due to bending moment alone. As a result, it became clear that the ultimate strength value of N(y), like the limit-strength value, is governed by downbending, and that again the fuselage is less critical than the wing. The critical fuselage location is FS 350, and the ultimate strength value of N(y) is approximately  $1 \times 10^{-9}$ .

E.3.3 Design Envelope Criterion. Statistically defined loads based on design envelope cases are also shown on Figures E-6(a) through (f). In obtaining these loads, the limit and ultimate strength values of  $\sigma_w \eta_d$  were taken as defined by Model 188 wing strength, at 60 and 100 fps respectively. The loads are then given by

Load = (one-g value) 
$$\pm$$
 ( $\overline{A}$ ) ( $\sigma_W \eta_d$ )

Factors of 66/50 and 25/50 were applied to  $\sigma_w\eta$ . For the  $V_B$  and  $V_D$  conditions respectively. As noted in Appendix E, we factors are the ratios of currently specified  $U_{de}$  gust velocities at the respective speeds. On the assumption that the same ratios would be retained in a power-spectral criterion, the loads resulting from these  $\sigma_w\eta_d$ 's are directly comparable as potential critical design conditions.

Each plotted point represents the most critical of the various cases. A variety of cases were critical, as indicated by Table E-8.

Again bearing in mind the conservatism of the upbending design load envelopes, it is seen that in all cases, both limit and ultimate, the statistically defined loads are well within the fuselage strength. Therefore it is concluded that the fuselage is not critical and will not influence the selection of design  $\sigma_{\mathbf{w}}\eta_{\mathbf{d}}$  levels.

Approximate limit-strength and ultimate-strength values of  $\sigma_{\rm c} \eta_{\rm d}$ , adjusted to an altitude of 12,000 ft. (in the same manner described in Appendix E) are as follows:

	Case	Aitiinde	Location	Limit	<b>Ultima</b> te
v <sub>B</sub>	427		FS 350 downbending	141 rps	270 fps
v <sub>c</sub>	407	12000 ft.	FS 571 downbending	67 fps	120 fps
v <sub>D</sub>	426	7000 ft.	FS 350 downbending	38 fps	73 fps

The critical cases and locations noted above are also indicated by underlining in Table E-8. It is seen that the  $V_{\rm B}$  values are far greater "than 66/50 of the corresponding  $V_{\rm C}$  values, and that the  $V_{\rm D}$  values are greater than 25/50 of the  $V_{\rm C}$  values. Consequently, the  $V_{\rm B}$  and  $V_{\rm D}$  conditions are less critical than the  $V_{\rm C}$  conditions.

## E.4 Model 749 Fuselage and Tail, Vertical Gust

A comparison of statistically defined loads for the Model 749 fuselage and tail with the corresponding design loads (as approximate measures of limit and ultimate strength) is given in Figures E-7(a) through (c).

As in the corresponding Model 188 comparison presented in Appendix E, Section E.3 the design load envelopes are shown as rectangles. The maximum shear and maximum bending moment conditions defining the envelopes were the same, in all cases.

The statistically defined loads also are obtained in the same way as in the Model 188 comparison.

The mission analysis points are plotted at frequency of exceedance levels, for the limit and ultimate conditions respectively, of  $2.4 \times 10^{-5}$  and  $1.4 \times 10^{-8}$  cycles per hour. These are the same values used in the Model 188 comparison in Appendix E, Section E.3.

The design envelope points are plotted at limit and ultimate  $\sigma_v \eta_d$  values of 60 and 100 fps, as in the Model 188 analysis. Factors of 66/50 and 25/50 were again applied to  $\sigma_w \eta_d$  for the  $V_B$  and  $V_D$  conditions respectively.

In all cases, the statistically defined loads are far below the design loads. As a result, the Model 749 fuselage and tail strength will not influence the selection of design levels of K(y) or of  $\sigma_{x}M_{d}$ .

TABLE E-8. CRITICAL FUSELAGE CASES, MODEL 188
(a) DOWN BENDING

	Critical Case ·										
Location		Limit		•	Ultimate						
	v <sub>B</sub>	A <sup>C</sup>	AD .	v <sub>B</sub>	v <sub>g</sub>	, D					
FE 350	427	407	426	427	410	426					
500	<u>427</u>	407	426	427	407	426					
571	427	407	425	427	407	426					
695	427	8c#	425	427	408	425					
1000	427	402	425	427	402	423					
Boriz, Tail	~	401	423	-	402	423					

## (b) UPBENDING

Location			Critics	1 Case		
		limit			Ultimte	
	v <sub>B</sub>	A <sup>C</sup>	ď	v <sub>B</sub>	A <sup>C</sup>	<b>v</b> <sub>D</sub>
FS 350	427	410	426	427	410	426
500	427	408	426	426	408	426
571	427	410	426	427	407	426
695	427	418	425	421	407	425
1000	427	418	424	427	418	424
Horiz, Tail	402	424	<b>19</b> 0	-	- 402	424

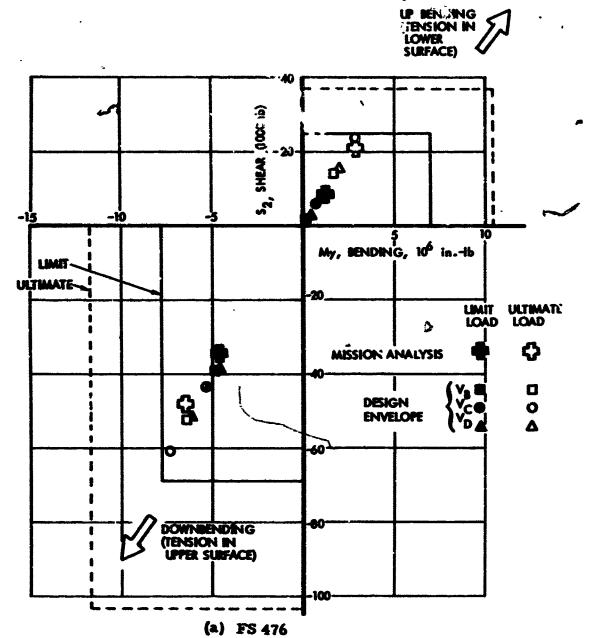
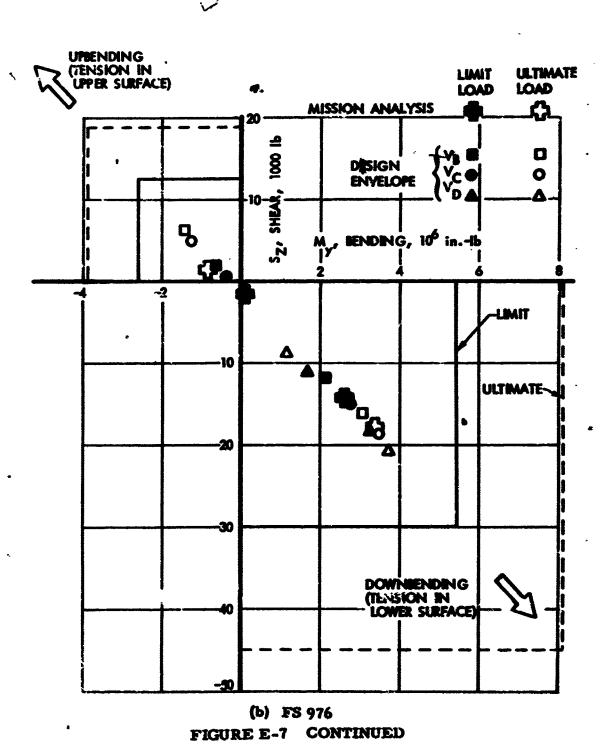
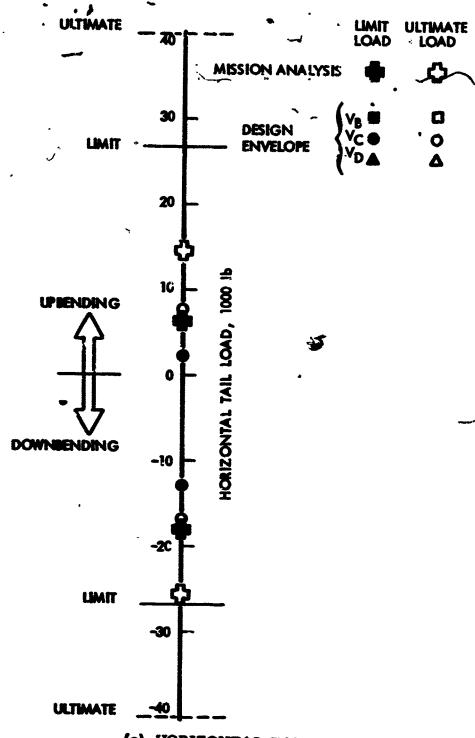


FIGURE E-? COMPARISON OF APPLIED FUSELAGE LOADS WITH DESIGN STENGTH - MISSION ANALYSIS AND DESIGN ENVELOPE CRITERIA - MODEL 749



E-41



(c) HORIZONTAL TAIL FIGURE E-7. CONCLUDED

Approximate limit and ultimate strength values of K(y), based on the design load envelopes shown are:

Limit:  $N(y) = 4.5 \times 10^{-9}$  exceedances per hour

-Ultimate:  $N(y) = 1.7 \times 10^{-14}$  exceedances per hour

The critical location in both cases is the horizontal tail in downbending.

Approximate limit and ultimate strength values of  $\sigma_{\rm W} \eta_{\rm d}$ , adjusted to an altitude of 16,000 feet as described in Appendix E, are:

	Case	Altitude	Limit	Ultimate
v <sub>B</sub>	323	7000 .	185 : ps	310 fps
ν <sub>C</sub>	302	16000	110 fps	186 fps
$\mathbf{v}_{\mathbf{D}}$	320	7000	71 fps	120 fps

The critical location in both cases is the forebody in downbending.

It should be remarked that the  $\sigma_{v} n_{d}$  values shown would have been materially higher if realistic payload running loads had been assumed, in accordance with present-day practice. The values used were taken from the original design loads determination of the airplane and were roughly 50% higher than would be used today.

## E.5 Model 188 Fuselage and Tail, Lateral Gust

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In establishing the limit and ultimate strength values of M(y) and and for lateral gust for the Model 188, major attention was given to the fin. The fin loading is measured by a single quantity, namely fin side load, and its limit and ultimate strength, in terms of allowable side load, can readily be determined. For the fuselage, on the other hand, many locations throughout the aftbody are potentially critical. At any given location, the stresses arise from airloads on the vertical tail and the fuselage, relieving inertia forces due to the lateral and yawing accelerations, balancing airloads on the horizontal tail, and the one-g level flight gravity forces. Variations in gross weight, c.g. position, and payload never affect all of these loads sources in the same way. As a result, it is virtually impossible to eliminate potential design conditions by inspection. To find the critical fuselage conditions would require generating design conditions and performing stress analysis for a multitude of combination-:.g. position (forward and aft limit),

gross weight, and payload-fuel quantities. The original design analysis, however, encompassed such lateral loading conditions as discrete lateral gust, yaw maneuver, and engine failure. For these conditions, the fuse-lage was not significantly more limiting than the fin. Also, there was some indication that if the fuse-lage were to be found critical, it would be in the far aft region, close to the tail, where the amount of aftbody payload would have a negligible effect.

Consequently, it was decided that a thorough investigation of all potentially critical aftbody conditions was not justified. It did appear desirable, however, to make at least a cursory fuselage stress analysis. For this purpose, three conditions were defined.

Inasmuch as the original limit design side load on the vertical tail had been 24000 lb., all three conditions were defined at this level. Each condition, however, was at a different speed, since equivalent airspeed has  $\epsilon$  large effect on the balancing tail load and hence on the one-g flight loads upon which the lateral gust increment superimposes. The three conditions selected were:

Mission analysis Case 202, 282 knots EAS at 11000 ft.  $V_C$  324 knots EAS at 12000 ft.  $V_D$  405 knots EAS at 8000 ft.

Aftbody payload was rather arbitrarily assumed to be zero, inaspuch as this condition appeared to be critical in the original design analysis. Balancing tail loads were arbitrarily based on a gross weight of 113,000 lb. for the  $V_{\rm D}$  condition and 77500 lb. for the  $V_{\rm C}$  condition. Fuselage torsions due to unsymmetrical horizontal tail load in one-g flight were based on flight load measurements instead of the arbitrary percentages specified in FAR 25. Lateral accelerations and body airloads consistent with the 24000 lb. side load on the vertical tail were approximated by use of the appropriate transfer functions; values of  $\beta$ , ny. and  $\psi$  in phase with the side load on the vertical tail, at the Dutch roll natural frequency, were used for this purpose. The side loads were calculated for the mission analysis case only, and the same ratios to the tail side load were assumed to apply for the  $V_{\rm C}$  and  $V_{\rm D}$  cases. Fuselage torsions due to the dissymmetry of horizontal tail load produced by induction affects from the vertical tail were obtained theoretically.

For each of the three conditions, the minimum aftbody margin of safety was determined by alress analysis. Also determined was the amount that the vertica tail site load would have to be reduced to give a zero margin of safety. The resulting margins of safety and allowable side loads were as follows:

		Speed,		Margin of	Allowable Load,	
Case		Knots EAS		Safety	Pactor	Load
I		282		02	•94	22500
II	•	35 <sub>1</sub> +		08	.81	19400
III		- 405	A	25	<b>- 57</b>	13700

The critical location in the structure in each care was found to be the upper forward corner of the aft passenger door, at FS 800. Inasmuch as this was relatively far forward, the actual payload present could have a substantial effect on the margins of safety.

For the fin itself and the frames that transmit its load into the fuselage shell, the minimum margin of safety was + .05. Accordingly, the limit allowable fin load is (1.05)(24000 lb.) = 25200 lb.

In view of the probably sizeable effect of payload on the fuselage margins of safety in the vicinity of FS 800, any results based on the margins of safety tabulated would have to be considered as only very roughly indicative. Within this limitation, approximate limit and ultimate values of N(y) and of  $\sigma_{\rm w}\eta_{\rm d}$  were computed.

The variation in allowable side load,  $P_y$ , for the three conditions was due almost exclusively to variation of the balancing load on the horizontal tail,  $P_z$ . Consequently, it was possible to plot allowable  $P_y$  vs balancing tail load,  $P_z$ , and read from the curve the allowable value of  $P_y$  corresponding to intermediate values of  $P_z$ . For ultimate conditions,  $P_z$  was divided by 1.5, the corresponding value of  $P_y$  was read, and this was multiplied by 1.5 to reconvert to an ultimate basis. For aft c.g. conditions, the down balancing tail load was reduced appropriately.

Before proceding further, the effect of cabin pressure on the margins of safety was examined. It was found that at the critical location the cabin pressure contributed significantly to the stresses. The maximum differential pressure was used in the analysis; at the pertinent altitudes, on the other hand, even if full sea level cabin pressure were maintained, the differential pressure would have been much lower. Elimination of this conservatism appeared to permit a sizeable increase in the tail side load. However, other locations would then become critical. One such location, where the cabin pressure did not contribute to the stress, showed a + .03 margin with the reduced P<sub>y</sub> indicated. It was estimated that the P<sub>y</sub> values tabulated above could probably be increased by about 5% before zero margins would be developed at these locations. Accordingly, the allowable P<sub>y</sub> values tabulated above were all multiplied by 1.05 before plotting vs P<sub>Z</sub>.

The various cases of interest are listed in Table E-9. The allowable  $P_y$  values shown were read from the curve. The limit and ultimate strength values of  $\sigma_w\eta_d$  were then computed as shown. The  $\overline{A}$  values used were taken from the critical cases for tail side load and are not necessarily consistent with the gross weights and payloads used in the fuselage loads determination. The limit and ultimate strength values of N(y) were read from Figure 9-13.

For the fin itself and the frames that transmit its loads into the fuselage shell, the limit allowable side load was indicated above to be 25200 lb. This value provides a cut-off for those conditions for which consideration of fuselage strength alone would result in a high allowable side load.

As noted in Section 7, preliminary analysis, based on tail load alone, had indicated the  $V_B$  loads to be appreciably lower than the  $V_C$  loads, on the basis of a ratio of  $V_B$  to  $V_C$   $\sigma_M$  is of 66/50. It is clear from Table E-9 that consideration of fuselage strength would not reverse this conclusion.

As noted above, detailed analysis of a sufficient number of design envelope conditions to establish a firm set of limit and ultimate strength σ,η, values for the Model 188 aftbody did not appear justified. It did appear, however, that a realistic set of aftbody loads could be derived readily for the mission analysis segment giving the highest fin side load, and that these loads would be quite representative of loads for the mission analysis as a whole. As a result, a more refined set of mission analysis loads was now defined. Actual aftbody payload was included. A more realistic cabin differential pressure, of 3.9 psi, was used, corresponding to a 2000 ft. cabin altitude at an airplane altitude of 11000 ft. Stresses due to cabin pressure, as before, were neglected where they acted to relieve the stresses due to the flight loads. This condition was defined with lateral loads corresponding to a fin side load of 24000 lb. The minimum margin of safety was found to be +.14. It was clear, therefore, mat the full limit-strength fin side load of 25200 lb could be carried without exceeding limit strength anywhere in the aftbody. As a result, the limit and ultimate strength N(y) values for lateral gust, for the Model 188, became:

Limit:  $N(y) = 6 \times 10^{-5}$  cycles per hour

Ultimate:  $N(y) = 5 \times 10^{-7}$  cycles per hour

TABLE E-9. CALCULATION OF LIMIT AND ULTIMATE STRENGTH VALUES OF N(y) AND °w\*d, LATERAL GUST, MODEL 188

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9		Altitude	£	. 0001	2002	7000	2000	2000	7000	7000	7000						
<b>©</b>	0 v n	. O	<b>@</b> .@	33.7	36.5	65.4	6.9	50,5	64.2	18	103					4-01 × 0	5 × 10-7
9		K	क्ता/दा	6.924	443.8	126.9	8-644	337.4	345.7	337.4	345.7					и(у) = 1.	N(y) = 5.5 × 10 <sup>-7</sup>
9		Py Ultimate	প্য			27300	23700			33900	35600			39300	-		37400
<b>@</b>		Py Limit	3	००५५र	76200	18600	19800	00†08	52200	CO)STE	23700	\$25800	27,800 1	*00292	\$00898	23700	24900
0		P. (idmit)	क्ष	00692-	-24600	-19200	-16400	-15100	-10900	-10100	- 7300	0098 -	1600	. 1700	1100	- 7400	- 14900
@		5		129	88	621	909	617	602	617	809	•	•	•	•		
0				V <sub>D</sub> LEM PRD 00	APT CG	V <sub>D</sub> ULL PAD CG	APT 00	V <sub>G</sub> LIDK PWD CG	APT CG	V <sub>G</sub> ULA FWD CG	APT 00	V <sub>R</sub> LIDK PND CG	SO ELTY	V ULT PRO CO	APT CO	MY LIN	MA ULA

Use 25200 lb as limited by tail.

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## E.6 Model 749 Fuselage and Tail, Lateral Gust

Based on the original stress analysis of the Model 749 outboard fins, the limit strength value of the side load on one fin is 6270 lb. The actual distribution of load amongst the three fins was later determined by loads measurements in flight. It was found that .45 of the total load was developed on the leading outboard fin. The resulting limit strength value of total side load for the three fins is therefore (6270 lb.)/.45 = 14000 lb. The corresponding ultimate strength is 21,000 lb.

Based on these strength values, the limit and ultimate strength N(y) values are read from Figure 9-15:

Limit:  $N(y) = 2.4 \times 10^{-4}$  exceedances per hour

Ultimate:  $N(y) = 5 \times 10^{-6}$  exceedances per hour

Limit and ultimate strength values of  $\sigma_w \eta_d$  were obtained utilizing the  $\overline{A}$  values from Table B-8:

Speed	Case	Altitude	Limit or Ultimate	Allowable P <sub>y</sub>	Ā	σ <sub>w</sub> n <sub>d</sub> =P <sub>y</sub> /k
7 <sub>C</sub>	501 <b>,</b> 503	7000 ft.	Limit	14000 1ь.	218 lr/fps	64.6
$\mathbf{v}_{\mathbf{D}}$	502, 54	7000 ft.	Limit	14000 1ь.	291 lb/fps	48.3
v <sub>c</sub>	501, 503	7000 ft.	Ultimate	21000 lb.	218 lb/fps	96.8
$\mathbf{v_{D}}$	502, 504	7000 ft.	<b>Ultimate</b>	. 21000 lb.	291 lb/fps	72.4

It is seen that the  $V_D$  values are in both cases well in excess of 25/50 of the corresponding  $V_C$  values. As indicated in Section 7,  $V_B$  cases were not included, as it appeared that the resulting allowable  $\sigma_w \eta_d$  values would be greater than 66/50 of the corresponding  $V_C$  values.

Lateral gust conditions based on power-spectral analysis were not defined for the Model 749 fuselage. It appeared, however, that the fuselage would probably be found to be less critical than the tail. The original design analysis showed the fuselage to be no more critical than the outboard fin; and with the more adverse distribution of load amongst the three fins used in the present analysis, the fuselage should become

relatively less critical. It is believed, moreover, that the relative severity of loading on the fuselage and tail should be about the same for a power-spectral gust condition as for the discrete gust and yaw maneuver conditions to which the airplane was originally designed. As a result, the substantial effort that would be required for present personnel to perform meaningful stress analysis of the Model 749 fuselage (bearing in mind that the original stress analysis is now nearly 20 years old) did not appear justified.

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